

Examples

*converging*  
A convex lens has a focal length of 12 cm. How far from the lens should an object be to produce a real image 4 times larger than the object?

$$d_o = ?$$

$$M = -4$$

*↑*  
*real image*

$$f = 12 \text{ cm}$$

$$12 < d_o < 24 *$$

$$\frac{1}{d_o} + \frac{1}{d_i} = \frac{1}{f}$$

$$M = \frac{-d_i}{d_o}$$

$$-4 = \frac{-d_i}{d_o} \quad * \text{ solve for } d_i$$

$$-4d_o = -d_i$$

$$4d_o = d_i \quad * \text{ Sub into lens eq.}$$

$$\frac{1}{d_o} + \frac{1}{4d_o} = \frac{1}{12}$$

$$\frac{4}{4d_o} + \frac{1}{4d_o} = \frac{1}{12}$$

$$\frac{5}{4d_o} = \frac{1}{12}$$

$$(5)(12) = 4d_o$$

$$60 = 4d_o$$

$$\boxed{15 \text{ cm} = d_o}$$

A convex lens has a focal length of 8.0 cm and is used as a magnifying glass. How far from the lens should an object be to produce a virtual image 3 times larger than the object?

$$d_o = ?$$

$$0 < d_o < 8$$

$$f = 8 \text{ cm}$$

$$M = +3$$

*↑*  
*virtual*

$$\frac{1}{d_o} + \frac{1}{d_i} = \frac{1}{f}$$

$$M = \frac{-d_i}{d_o}$$

$$+3 = \frac{-d_i}{d_o}$$

$$3d_o = -d_i$$

$$-3d_o = d_i$$

$$\frac{1}{d_o} + \left(\frac{1}{-3d_o}\right) = \frac{1}{8}$$

$$\frac{1}{d_o} - \frac{1}{3d_o} = \frac{1}{8}$$

$$\frac{3}{3d_o} - \frac{1}{3d_o} = \frac{1}{8}$$

$$\frac{2}{3d_o} = \frac{1}{8} \rightarrow \boxed{5.3 \text{ cm} = d_o}$$