

Quadratics #2 – Review #1

1. Which **quadrant** is the vertex of $(y + 3) = (x - 2)^2$ located in?
 a) I b) II c) III d) IV

Vertex:

$(2, -3) \Rightarrow$ QUADRANT IV

2. Which **quadrant** is the vertex of $\frac{1}{3}(y - 2) = (x + 3)^2$ located in?
 a) I b) II c) III d) IV

3. Rewrite the following equation in standard form: $-4(y - 1) = x^2$

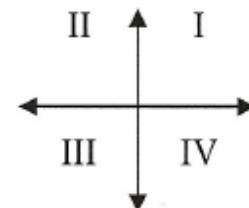
- a) $y = -4x^2 + 1$ b) $y = -\frac{1}{4}x^2 + 1$ c) $y = 4x^2 - 1$ d) $y = \frac{1}{4}x^2 + 1$

$$-4(y-1) = x^2 \text{ (TF)}$$

$$y-1 = -\frac{1}{4}x^2$$

$$y = -\frac{1}{4}x^2 + 1 \text{ (SF)}$$

Solutions



Vertex:

$(-3, 2) \Rightarrow$ QUADRANT II

4. Rewrite the following equation in transformational form: $y = \frac{1}{3}(x - 2)^2 + 1$

- a) $3(y - 1) = (x - 2)^2$ b) $\frac{1}{3}(y + 1) = (x - 2)^2$ c) $\frac{1}{3}(y - 1) = (x + 2)^2$ d) $3(y + 2) = (x - 1)^2$

$$y = \frac{1}{3}(x - 2)^2 + 1 \text{ (SF)}$$

$$3(y - 1) = 3(x - 2)^2 \text{ (TF)}$$

5. Rewrite the following equation in general form: $y = 2(x - 1)^2 + 3$

- a) $y = 2x^2 - 2x + 5$ b) $y = 2x^2 + 5$ c) $y = 2x^2 - 3$ d) $y = 2x^2 - 4x + 5$

$$y = 2(x - 1)^2 + 3 \text{ (SF)}$$

$$y = 2(x - 1)(x - 1) + 3$$

$$y = (2x - 2)(x - 1) + 3$$

$$y = 2x^2 - 2x - 2x + 2 + 3$$

$$y = 2x^2 - 4x + 5 \text{ (GF)}$$

6. Where is the axis of symmetry located in the following parabola: $2(y - 1) = (x - 3)^2$

- a) $x = 2$ b) $x = 1$ c) $x = 3$ d) $y = 1$

Vertex: $(3, 1)$

Axis of Symmetry: $x = 3$

7. What would be the range of the following quadratic function: $-2(y - 1) = (x + 1)^2$

- a) $\{y | y \geq -2, y \in \mathbb{R}\}$ b) $\{x | x \leq -1, x \in \mathbb{R}\}$ c) $\{y | y \leq 1, y \in \mathbb{R}\}$ d) $\{x | x \geq 1, x \in \mathbb{R}\}$

Range: $\{y | y \leq 1, y \in \mathbb{R}\}$

* Opens Downward.

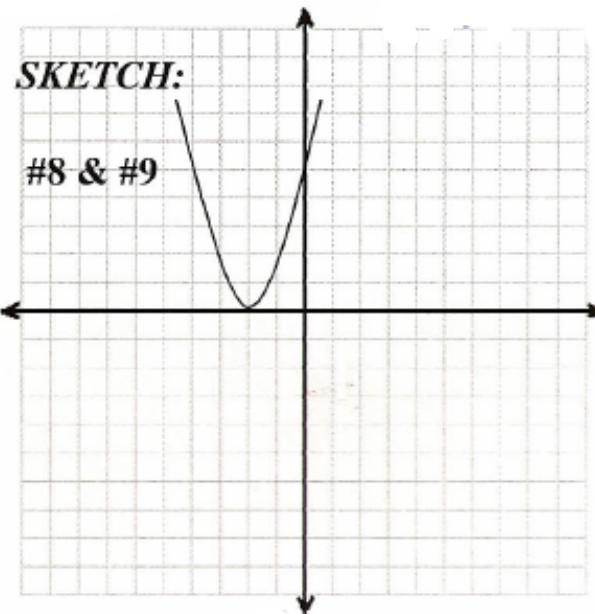
8. Given this graph and its equation: $\frac{1}{a}(y - k) = (x - h)^2$

What would happen if "h" was changed? The graph would:

- a) move sideways
- b) move up or down
- c) be reflected in the x-axis
- d) be stretched

9. What would happen if "k" was changed? The graph would:

- a) move sideways
- b) move up or down
- c) be reflected in the x-axis
- d) be stretched



10. Sketch the graph of: $y = 2(x - 1)^2 - 10$

x	y
-2	8
-1	-2
0	-8
1	-10
2	-8
3	-2

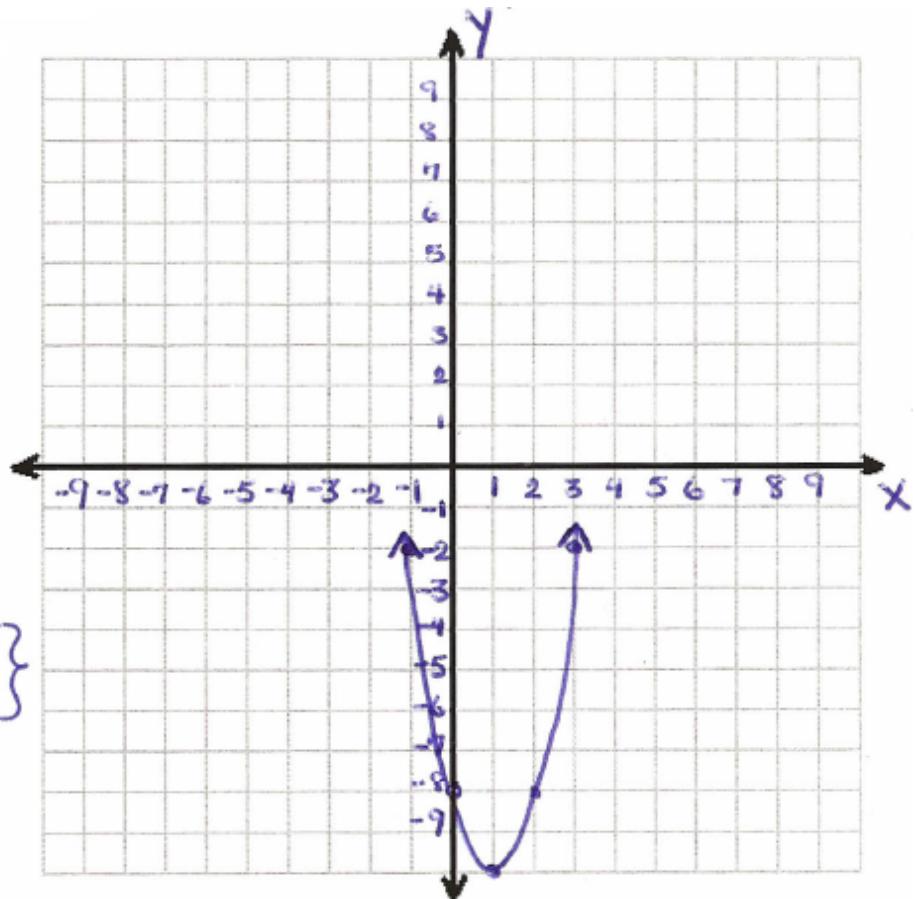
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What is the Domain?

$$\{x | x \in \mathbb{R}\}$$

What is the Range?

$$\{y | y \geq -10, y \in \mathbb{R}\}$$



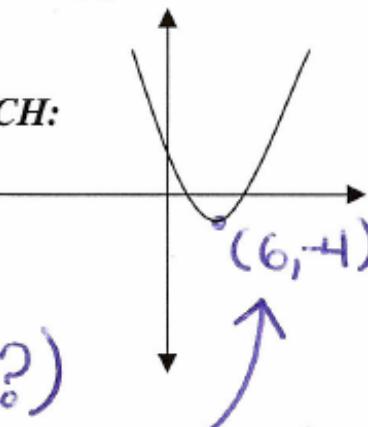
11. The x-intercepts of a parabola are (2, 0) and (10, 0). Which of the following points could be the vertex?

- a) (12, 0)
- b) (6, -4)
- c) (6, 4)
- d) (8, -4)

* Since the vertex will be half way in between the x-intercepts:

Average of x-values: $\frac{2+10}{2} = \frac{12}{2} = 6$

\Rightarrow Vertex: (6, ?)



** 2 possible solutions \rightarrow check sketch!

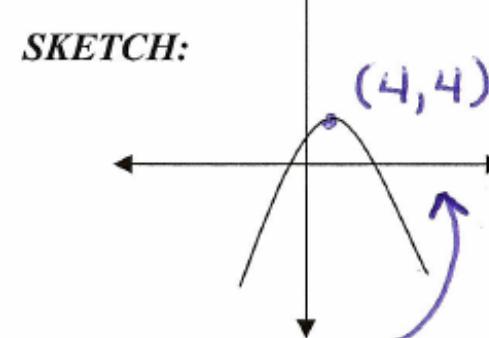
12. The x-intercepts of a parabola are (-3, 0) and (11, 0). Which of the following points could be the vertex?

- a) (8, -4)
- b) (7, 3)
- c) (4, 4)
- d) (4, -4)

Average of x-values:

$$\frac{-3+11}{2} = \frac{8}{2} = 4$$

\Rightarrow Vertex: (4, ?)



* 2 possible solutions \rightarrow check sketch!

13. Rewrite the following equation in transformational form: $y = 3(x - 1)^2 + 2$

- a) $(y + 2) = 3(x - 1)^2$ b) $\frac{1}{3}(y - 2) = (x - 1)^2$ c) $3(y - 2) = \frac{1}{3}(x - 1)^2$ d) $3y - 2 = (x - 1)^2$

$$y = 3(x - 1)^2 + 2 \text{ (SF)}$$

$$y - 2 = 3(x - 1)^2$$

$$\frac{1}{3}(y - 2) = (x - 1)^2 \text{ (TF)}$$

14. Rewrite the following equation in transformational form: $y = 3x^2 - 12x + 5$

- a) $\frac{1}{3}(y + 7) = (x - 2)^2$ b) $3(y - 7) = (x - 2)^2$ c) $-\frac{1}{3}(y - 7) = (x + 2)^2$ d) $3(y + 2) = (x - 7)^2$

$$y = 3x^2 - 12x + 5 \text{ (GF)}$$

$$y - 5 = 3x^2 - 12x$$

$$y - 5 = 3(x^2 - 4x)$$

$$y - 5 + 12 = 3(x^2 - 4x + 4)$$

$$y + 7 = 3(x - 2)^2$$

$$\frac{1}{3}(y + 7) = (x - 2)^2 \text{ (TF)}$$

15. Place the following functions in both standard and transformational form:

a) $y = x^2 + 12x + 40$

b) $y = -2x^2 + 8x - 10$

$$y - 40 = x^2 + 12x \quad y + 10 = -2x^2 + 8x$$

$$y - 40 + 36 = (x^2 + 12x + 36) \quad y + 10 = -2(x^2 - 4x)$$

$$y - 4 = (x+6)^2 \quad y + 10 - 8 = -2(x^2 - 4x + 4)$$

$$(SF) \quad y = (x+6)^2 + 4 \quad (SF) \quad y = -2(x-2)^2 - 2$$

$$(TF) \quad (y-4) = (x+6)^2 \quad (TF) \quad \underline{-1}(y+2) = (x-2)^2$$

c) $y = 3x^2 + 12x$ d) $y = -2x^2 + 14x - \frac{1}{2}$

$$y = 3(x^2 + 4x)$$

$$y + \frac{1}{2} = -2x^2 + 14x$$

$$y + 12 = 3(x^2 + 4x + 4) \quad y + \frac{1}{2} = -2(x^2 - 7x)$$

$$y + 12 = 3(x+2)^2 \quad y + \frac{1}{2} - \frac{98}{4} = -2(x^2 - 7x + \frac{49}{4})$$

$$y + 12 = 3(x+2)^2 - 12 \quad y + \frac{2}{4} - \frac{98}{4} = -2(x - \frac{7}{2})^2$$

$$(SF) \quad y = 3(x+2)^2 - 12 \quad y - \frac{96}{4} = -2(x - \frac{7}{2})^2$$

$$(TF) \quad \underline{\frac{1}{3}}(y+12) = (x+2)^2 \quad \left. \begin{array}{l} (SF) \quad y = -2(x - \frac{7}{2})^2 + 24 \\ (TF) \quad \underline{-\frac{1}{2}}(y-24) = (x - \frac{7}{2})^2 \end{array} \right\} \text{lowest terms!}$$