

## ANSWERS $\rightarrow$ Completing the Square Worksheet

①  $x^2 + 14x + 50$

$\hookrightarrow y = x^2 + 14x + 50$

$y - 50 = (x^2 + 14x)$

$y - 50 + 49 = (x^2 + 14x + 49)$

$y - 1 = (x + 7)^2 \{TF\}$

OR

$y = (x + 7)^2 + 1 \{SF\}$

②  $x^2 - 4x + 6$

$\hookrightarrow y = x^2 - 4x + 6$

$y - 6 = (x^2 - 4x)$

$y - 6 + 4 = (x^2 - 4x + 4)$

$y - 2 = (x - 2)^2 \{TF\}$

OR

$y = (x - 2)^2 + 2 \{SF\}$

③  $x^2 + 30x + 250$

$\hookrightarrow y = x^2 + 30x + 250$

$y - 250 = (x^2 + 30x)$

$y - 250 + 225 = (x^2 + 30x + 225)$

$y - 25 = (x + 15)^2 \{TF\}$

OR

$y = (x + 15)^2 + 25 \{SF\}$

④  $x^2 - 6x$

$\hookrightarrow y = x^2 - 6x$

$y + 9 = (x^2 - 6x + 9)$

$y + 9 = (x - 3)^2 \{TF\}$

OR

$y = (x - 3)^2 - 9 \{SF\}$

$$\textcircled{5} \quad x^2 + 7x$$

$$\hookrightarrow y = x^2 + 7x$$

$$y + \frac{49}{4} = (x^2 + 7x + \frac{49}{4})$$

$$y + \frac{49}{4} = (x + \frac{7}{2})^2 \quad \{\text{TF}\}$$

OR

$$y = (x + \frac{7}{2})^2 - \frac{49}{4}$$

$$\textcircled{6} \quad x^2 + 5x + 4$$

$$\hookrightarrow y = x^2 + 5x + 4$$

$$y - 4 = (x^2 + 5x)$$

$$y - 4 + \frac{25}{4} = (x^2 + 5x + \frac{25}{4})$$

$$y - \frac{16}{4} + \frac{25}{4} = (x + \frac{5}{2})^2$$

$$y + \frac{9}{4} = (x + \frac{5}{2})^2 \quad \{\text{TF}\}$$

OR

$$y = (x + \frac{5}{2})^2 - \frac{9}{4}$$

$$\textcircled{7} \quad y = 2x^2 + 12x + 15$$

$$y - 15 = 2(x^2 + 6x)$$

$$y - 15 + 18 = 2(x^2 + 6x + 9)$$

$$y + 3 = 2(x + 3)^2$$

$$\frac{1}{2}(y + 3) = (x + 3)^2 \quad \{\text{TF}\}$$

OR

$$y = 2(x + 3)^2 - 3 \quad \{\text{SF}\}$$

$$\textcircled{8} \quad y = 4x^2 - 16x + 30$$

$$y - 30 = 4(x^2 - 4x)$$

$$y - 30 + 16 = 4(x^2 - 4x + 4)$$

$$y - 14 = 4(x - 2)^2$$

$$\frac{1}{4}(y - 14) = (x - 2)^2$$

OR

$$y = 4(x - 2)^2 + 14$$

$$\begin{aligned}
 \textcircled{9} \quad y &= 3x^2 + 12x + 11 \\
 y - 11 &= 3(x^2 + 4x) \\
 y - 11 + 12 &= 3(x^2 + 4x + 4) \\
 y + 1 &= 3(x + 2)^2 \\
 \left[ \begin{array}{l} \frac{1}{3}(y + 1) = (x + 2)^2 \{TF\} \\ \text{OR} \end{array} \right. \\
 \rightarrow y &= 3(x + 2)^2 - 1 \{SF\}
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{10} \quad y &= -x^2 + 4x + 5 \\
 y - 5 &= -(x^2 - 4x) \\
 y - 5 - 4 &= -(x^2 - 4x + 4) \\
 y - 9 &= -(x - 2)^2 \\
 \left[ \begin{array}{l} -(y - 9) = (x - 2)^2 \{TF\} \\ \text{OR} \end{array} \right. \\
 \rightarrow y &= -(x - 2)^2 + 9 \{SF\}
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{11} \quad y &= -x^2 + 6x + 5 \\
 y - 5 &= -(x^2 - 6x) \\
 y - 5 - 9 &= -(x^2 - 6x + 9) \\
 y - 14 &= -(x - 3)^2 \\
 \left[ \begin{array}{l} -(y - 14) = (x - 3)^2 \{TF\} \\ \text{OR} \end{array} \right. \\
 \rightarrow y &= -(x - 3)^2 + 14
 \end{aligned}$$

$$\begin{aligned}
 \textcircled{12} \quad y &= -2x^2 + 12x - 9 \\
 y + 9 &= -2(x^2 - 6x) \\
 y + 9 - 18 &= -2(x^2 - 6x + 9) \\
 y - 9 &= -2(x - 3)^2 \\
 \left[ \begin{array}{l} -\frac{1}{2}(y - 9) = (x - 3)^2 \{TF\} \\ \text{OR} \end{array} \right. \\
 \rightarrow y &= -2(x - 3)^2 + 9 \{SF\}
 \end{aligned}$$