

## Exercise 1

$$3. \{(1, 3), (2, 6), (3, 12), (4, 24), \dots\}$$

$$\begin{array}{l} \text{y-values: } 3, 6, 12, 24 \\ \quad \quad \quad \downarrow \downarrow \downarrow \\ \quad \quad \quad \times 2 \times 2 \times 2 \end{array} \quad \text{x-values: increase by 1.}$$

This is an exponential function with a common ratio of 2.

$$4. \{(1, 3), (3, 1.5), (5, 0.75), (7, 0.375), \dots\}$$

$$\begin{array}{l} \text{y-values: } 3, 1.5, 0.75, 0.375 \\ \quad \quad \quad \downarrow \downarrow \downarrow \\ \quad \quad \quad \times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} \end{array} \quad \text{x-values: increase by 2}$$

$$* \div 2 = \times \frac{1}{2}$$

This is an exponential function with a common ratio of  $\sqrt{\frac{1}{2}}$ . {since the x-values increase by 2.}

$$7. \{(2, 8), (5, 12), (8, 18), (11, 27), \dots\}$$

$$y\text{-values: } 8, 12, 18, 27.$$

$\swarrow \quad \swarrow \quad \swarrow$   
 $\times 1.5 \quad \times 1.5 \quad \times 1.5$

This is an exponential function with a common ratio of  $\sqrt[3]{1.5}$  or  $\sqrt[3]{\frac{3}{2}}$ .

{ Since the  $x$ -values increase by 3 }

9.  $\{(-1, 40), (0, 8), (1, 1.6), (2, 0.32), \dots\}$

y-values: 40, 8, 1.6, 0.32      x-values: increase by 1.  
                   $\underbrace{\quad} \times 0.2$      $\underbrace{\quad} \times 0.2$      $\underbrace{\quad} \times 0.2$

This is an exponential function with a common ratio of 0.2.

10.  $\{ 5, 15, 45, \frac{135}{1}, \frac{405}{1}, \frac{1215}{1} \}$  common ratio is 3.

$\xrightarrow{\times 3} \xrightarrow{\times 3} \xrightarrow{\times 3} \xrightarrow{\times 3} \xrightarrow{\times 3}$

11.  $\{ -4, 16, -64, \frac{256}{1}, \frac{-1024}{1}, \frac{4096}{1} \}$  common ratio is -4.

$\xrightarrow{\times -4} \xrightarrow{\times -4} \xrightarrow{\times -4} \xrightarrow{\times -4} \xrightarrow{\times -4}$

12.  $\{ \frac{5}{7}, \frac{5}{14}, \frac{5}{28}, \frac{5}{56}, \frac{5}{112}, \frac{5}{224} \}$  common ratio is  $\frac{1}{2}$ .

14.  $y = 4^x$

Common ratio = 4

15.  $y = 1.8^x$

Common ratio = 1.8

16.  $y = 0.3^x$

Common ratio = 0.3.

17.  $y = 2700(2.6)^x$

Common ratio = 2.6.

18. Joe borrows \$250 from Tom  
Tom charges 2% interest per day.  
\* (At the end of 1 day, he will owe 102%)

EQUATION:

$$y = \text{initial amount} (\text{common ratio})^x$$
$$= \$250 (1.02)^x$$

After 5 days:

$$y = \$250 (1.02)^5$$
$$= \$250 (1.104080803)$$
$$= \$276.02$$

After 20 days:

$$y = \$250 (1.02)^{20}$$
$$= \$250 (1.485947396)$$
$$= \$371.49$$

After 100 days:

$$y = \$250 (1.02)^{100}$$
$$= \$250 (7.244646118)$$
$$= \$1811.16$$

This function is an example of exponential growth!

19. Samantha buys a car for \$24000  
The vehicle depreciates by 18% each year.

a) Time (x)	0	1	2	3	4
Amount (y)	24000	19680	16137.60	13232.83	10850.92

b) Common Ratio = 0.82  
(100% - 18% = 82%)

c) This function is an example of exponential decay.

d) EQUATION:  $y = 24000(0.82)^x$

Initial Amount

Common Ratio