

If $A = 28 \text{ m } [E75^\circ N]$, $B = 35 \text{ m } [E24^\circ S]$, $C = 22 \text{ m } [W50^\circ N]$, and $D = 40 \text{ m } [W30^\circ S]$ Find:

b. $4C + 3D \quad \{160 \text{ m } [W2.6^\circ N]\} \quad - + +$

$$R_E = 4C_E + 3D_E \quad | \quad R_N = 4C_N + 3D_N$$

$$\begin{aligned} C_E &= -22 \cos 50^\circ \\ &= -14.1 \text{ m} \end{aligned} \quad \left| \begin{array}{l} D_E = -40 \cos 30^\circ \\ = -34.6 \text{ m} \end{array} \right.$$

$$\begin{aligned} C_N &= +22 \sin 50^\circ \\ &= +16.9 \text{ m} \end{aligned} \quad \left| \begin{array}{l} D_N = -40 \sin 30^\circ \\ = -20 \text{ m} \end{array} \right. \quad - - - - -$$

$$\begin{aligned} R_E &= 4(-14.1) + 3(-34.6) \\ &= \underline{-160.2 \text{ m}} \end{aligned}$$

$$\begin{aligned} R_N &= 4(16.9) + 3(-20) \\ &= \underline{7.6 \text{ m}} \end{aligned}$$

$$|R| = \sqrt{R_E^2 + R_N^2} = \sqrt{(160.2)^2 + (7.6)^2}$$

$$|R| = 160.4 \text{ m} \quad \theta = \tan^{-1} \left| \frac{R_y}{R_x} \right|$$

$$\theta = \tan^{-1} \left| \frac{7.6}{160.2} \right| = 2.7^\circ$$

$$R = 160.4 \text{ m } [W2.7^\circ N]$$

$$d. \quad 2D-C \quad \{79.2 \text{ m [W}46^{\circ}\text{S]}\}$$

$$D_E = -34.6 \text{ m} \quad | \quad C_E = -14.1 \text{ m}$$

$$D_N = -20 \text{ m} \quad | \quad C_N = 16.9 \text{ m}$$

$$R_E = 2D_E - C_E \quad R_N = 2D_N - C_N$$

$$= 2(-34.6) - (-14.1)$$

$$= 2(-20) - (16.9)$$

$$= -69.2 + 14.1$$

$$= -40 - 16.9$$

$$R_E = \underline{-55.1 \text{ m}}$$

$$R_N = \underline{-56.9 \text{ m}}$$

$$2D-C \rightarrow |R| = \sqrt{R_E^2 + R_N^2}$$

$$= \sqrt{(-55.1)^2 + (-56.9)^2}$$

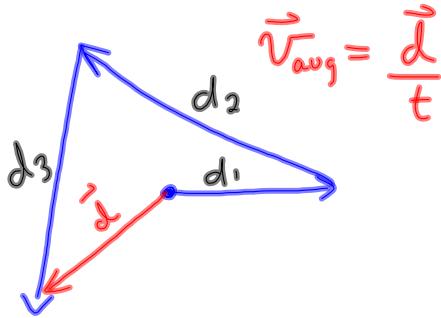
$$= 79.2 \text{ m}$$

$$\theta = \tan^{-1} \left| \frac{R_N}{R_E} \right| = \tan^{-1} \left| \frac{-56.9}{-55.1} \right|$$

$$\theta = 46^{\circ}$$

$$R = 79.2 \text{ m [W}46^{\circ}\text{S]}$$

1. What is the average velocity of a car that drives 66 km [E], 52 km [W 33° N], and 45 km [W 73° S] in 3.1 hours?



$$d_{1E} = \underline{66 \text{ km}} \quad d_{2E} = -52 \cos 33 = \underline{-43.6 \text{ km}} \\ d_{IN} = \underline{0 \text{ km}} \quad d_{aN} = 52 \sin 33 = \underline{28.3 \text{ km}}$$

$$d_{3E} = -45 \cos 73 = \underline{-13.2 \text{ km}}$$

$$d_{3N} = -45 \sin 73 = \underline{-43 \text{ km}}$$

$$\begin{aligned} \vec{d}_E &= d_{1E} + d_{2E} + d_{3E} & \vec{d}_N &= d_{IN} + d_{aN} + d_{3N} \\ &= 66 - 43.6 - 13.2 & &= 0 + 28.3 - 43 \\ d_E &= \underline{9.2 \text{ km}} & d_N &= \underline{-14.7 \text{ km}} \end{aligned}$$

$$|\vec{d}| = \sqrt{d_E^2 + d_N^2} = \sqrt{(9.2)^2 + (-14.7)^2}$$

$$|\vec{d}| = 17.3 \text{ km}$$

$$\theta = \tan^{-1} \left| \frac{d_N}{d_E} \right| = \tan^{-1} \left| \frac{-14.7}{9.2} \right|$$

$$\theta = \tan^{-1}(1.5978) = 58^\circ$$

$$\underline{\underline{\vec{d} = 17.3 [\text{E} 58^\circ \text{S}]}}$$

$$\overrightarrow{v_{avg}} = \frac{\vec{d}}{t} = \frac{17.3 [\text{E} 58^\circ \text{S}]}{3.1}$$

 .

Physics 122: Application of Vectors Examples

2. What is the acceleration of a glider that goes from 10 m/s [N] to 10 m/s [E] in 2.5 seconds?

$$\vec{a} = \frac{\vec{v}_f - \vec{v}_o}{t}$$

$$|a| = \sqrt{a_E^2 + a_N^2} \quad a_E = \frac{v_{fE} - v_{oE}}{t}$$

$$\theta = \tan^{-1} \left| \frac{a_N}{a_E} \right| \quad a_N = \frac{v_{fN} - v_{oN}}{t}$$