

# Physics 122/121

## Unit 1

### Dynamics Extension

***definition of equilibrium:** the state of an object when the vector sum of all the forces acting on it is zero.*

If an object is at *rest* and is in *equilibrium*, then we say that it is in a state of "*static equilibrium*."

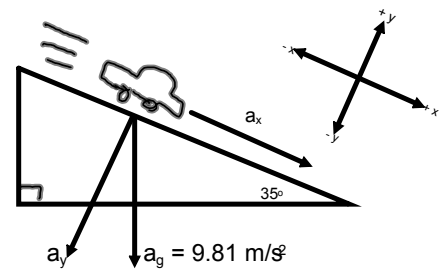
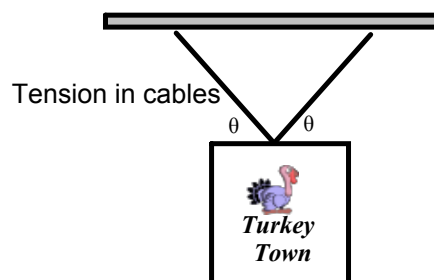
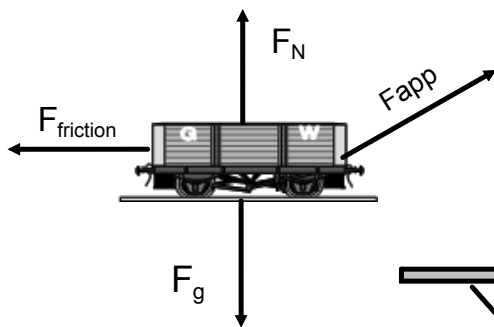
**Equilibrant: is the one vector, when added to 2 or more other vectors produces a state of equilibrium. It is equal to the resultant but opposite in direction.**

Try - Three forces act simultaneously on point P. The first force is 10 N east. The second force is 15 N south. The third force is 28 N, E46S . Find the resultant force. (46 N, E50°S ). Find the equilibrant.(46N, W50N)

## Three Types of Force Problems

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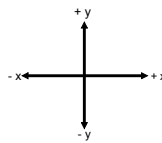
- 1 - Pushing or pulling an object along a horizontal surface.
- 2 - Tension and hanging signs.
- 3 - Objects on an incline.



## Force Problems - Type I

A 55 kg snow blower is pushed along the ground at an angle of 35° to the horizontal with an applied force of 175 N.

- Find the  $F_{ax}$  and  $F_{ay}$ .
- Calculate  $F_N$ .
- Find the force of friction if  $\mu = 0.19$ .
- Find the  $F_{netx}$ .
- Find  $a_x$ .



$$\begin{aligned} a) F_{ax} &= F \cos \theta \\ &= 175 \cos 35 = 143 \text{ N} \end{aligned}$$

$$F_{ay} = -175 \sin 35 = -100 \text{ N}$$

$$b) F_N = ?$$

$$F_{nety} = \sum \text{Forces vertically}$$

$$F_{nety} = F_{ay} + F_g + F_N$$

$$0 = -100 + (55 \text{ kg})(-9.81) + F_N$$

$$0 = -100 - 540 + F_N$$

$$\boxed{640 \text{ N} = F_N}$$

$$\begin{aligned} c) F_f &= \mu F_N \\ &= (0.19)(640) \\ F_f &= 122 \text{ N} \leftarrow \text{magnitude} \end{aligned}$$

$$\begin{aligned} d) F_{netx} &= F_{ax} + F_f \\ &= 143 + (-122) \end{aligned}$$

$$F_{netx} = 21 \text{ N}$$

$$e) a_x = ?$$

$$F_{netx} = ma_x$$

$$21 = 55a_x$$

$$\boxed{0.38 \text{ m/s}^2 = a_x}$$

A 35 kg wagon is pulled along the ground at an angle of  $25^\circ$  to the horizontal with an applied force of 97 N.

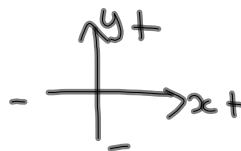
a) Find the  $F_{ax}$  and  $F_{ay}$ .

b) Calculate  $F_N$ .

c) Find the force of friction if  $\mu = 0.22$ .

d) Find the  $F_{netx}$ .

e) Find  $a_x$ .



$$a) \bar{F}_{ax} = 97 \cos 25^\circ = 88 \text{ N}$$

$$F_{ay} = 97 \sin 25^\circ = 41 \text{ N}$$

$$b) F_N = ? \quad \Sigma \text{ Forces in } y\text{-direction}$$

$$F_{nety} = F_N + F_{ay} + F_g$$

$$0 = F_N + 41 + (35)(-9.81)$$

$$0 = F_N - 302.4$$

$$\boxed{302 = F_N}$$

$$c) \bar{F}_f = \mu F_N$$

$$= (0.22)(302) = 66 \text{ N}$$

$$d) F_{netx} = ?$$

$$F_{netx} = \Sigma \text{ Forces in } x\text{-dir}$$

$$= F_{ax} + F_f$$

$$= 88 + (-66) = \boxed{22 \text{ N}}$$

$$e) a_x = ?$$

$$F_{netx} = m a_x$$

$$22 = 35 a_x$$

$$\frac{22}{35} = a_x$$

$$\boxed{\frac{22}{35} \text{ m/s}^2}$$

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Force Problems - Type I

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17. A student pushes a 25 kg lawn mower with a force of 150 N. The handle makes an angle of  $35^\circ$  to the horizontal.

- (a) Find the vertical and horizontal components of the applied force.
- (b) Calculate the normal force supporting the lawn mower while it is being pushed.
- (c) Calculate the net force propelling the mower if a frictional force of 85 N exists.
- (d) Calculate the horizontal acceleration of the lawn mower. (Remember: Only part of the  $F_{\text{applied}}$  is parallel to the direction of horizontal acceleration.)

- a) 86 N, down  
1.2 x 10<sup>2</sup> N, right
- b) 3.3 x 10<sup>2</sup> N, up
- c) 38 N, right
- d) 1.5 m/s<sup>2</sup>, right

24. A toboggan with a mass of 15 kg is being pulled with an applied force of 45 N at an angle of  $40^\circ$  to the horizontal. What is the acceleration if the force of friction opposing the motion is 28 N?

0.43 m/s<sup>2</sup>, right

25. A grocery cart is being pushed with a force of 450 N at an angle of  $30.0^\circ$  to the horizontal. If the mass of the cart and the groceries is 42 kg,
- (a) Calculate the force of friction if the coefficient of friction is 0.60.
  - (b) Determine the acceleration of the cart.

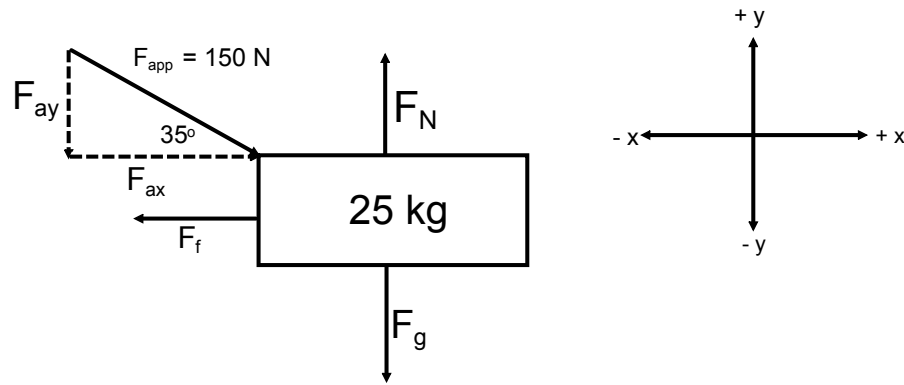
- a) 3.8 x 10<sup>2</sup> N, left
- b) 0.23 m/s<sup>2</sup>, right

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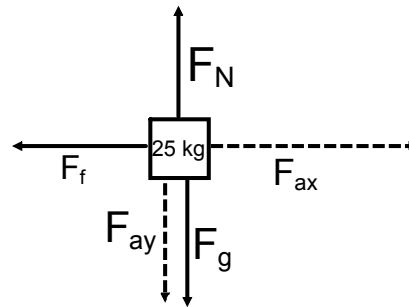
36. A 45.0 kg box is pulled with a force of 205 N by a rope held at an angle of  $46.5^\circ$  to the horizontal. The velocity of the box increases from 1.00 m/s to 1.50 m/s in 2.50 s. Calculate
- (a) the net force acting horizontally on the box.
  - (b) the frictional force acting on the box.
  - (c) the horizontal component of the applied force.
  - (d) the coefficient of kinetic friction between the box and the floor.

- a) 9.0 N, right
- b) 132 N, left
- c) 141 N, right
- d) 0.451

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Free Body Diagram



$$(a) F_{ax} = +150\cos(35) \\ = 123\text{ N}$$

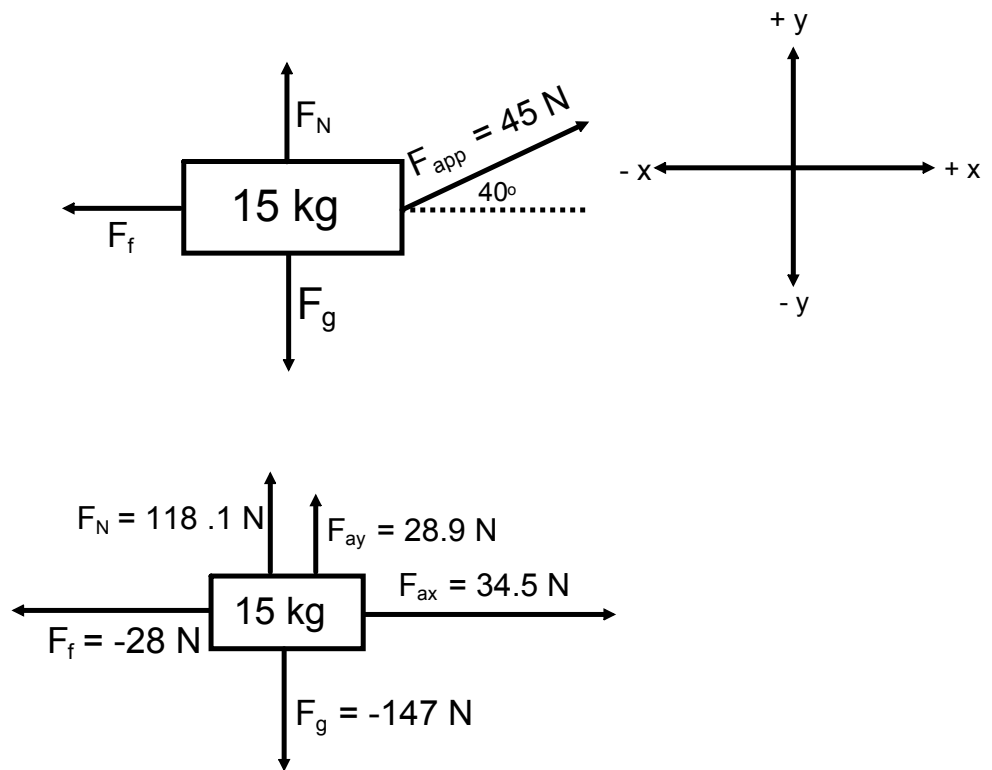
$$F_{ay} = -150\sin(35) \\ = -86\text{ N}$$

$$(b) F_{nety} = F_{ay} + F_g + F_N \\ 0 = -86\text{ N} - mg + F_N \\ 0 = -86 - 25(9.81) + F_N \\ 0 = -86 - 245.25 + F_N \\ 0 = -331.25 + F_N \\ +330\text{ N} = F_N$$

$$(c) F_{netx} = \text{Sum of horizontal forces} \\ = F_{ax} + F_f \\ = 123 + -85 \\ = +38\text{ N}$$

$$(d) F_{net} = ma \\ a = \frac{F_{net}}{m} \\ a = \frac{+38\text{ N}}{25\text{ kg}} \\ a = +1.5\text{ m/s}^2$$

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$$\begin{aligned}
 F_{netx} &= F_{ax} + F_f \\
 &= 34.5 + (-28) \\
 &= +6.5 \text{ N}
 \end{aligned}$$

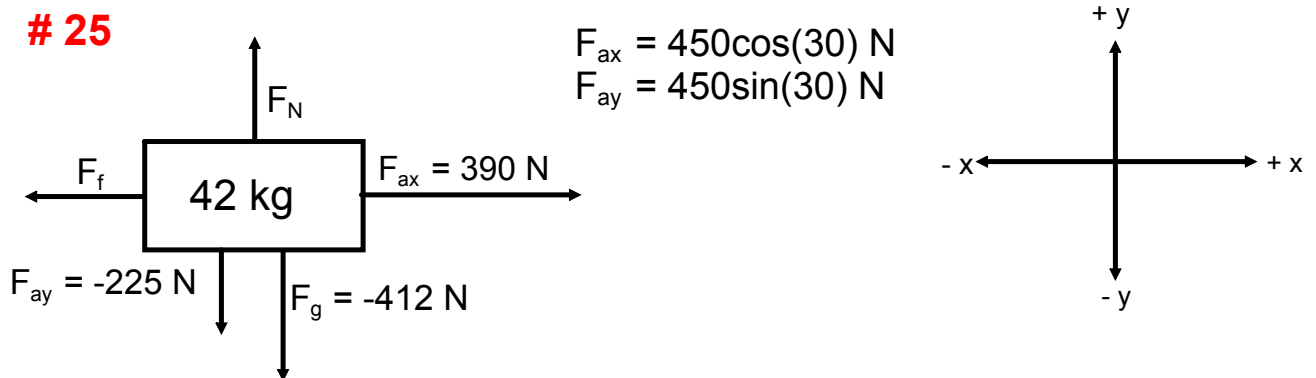
$$F_{net} = ma$$

$$a = \frac{F_{net}}{m}$$

$$a = +6.5 \text{ N}/15 \text{ kg}$$

$$a = +0.43 \text{ m/s}^2$$





(a)  $F_f = \mu F_N, \mu = -0.60$

$$F_{nety} = F_{ay} + F_g + F_N$$

$$0 = -412 \text{ N} + -225 \text{ N} + F_N$$

$$F_N = + 637 \text{ N}$$

$$F_f = 0.60(637 \text{ N})$$

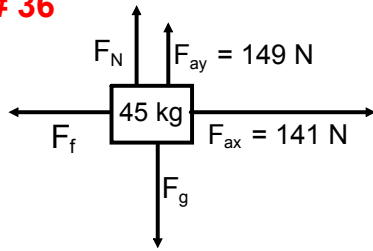
$$F_f = 380 \text{ N [left]}$$

(b)  $a = \frac{F_{net}}{m} = F_{ax} + F_f$

$$a = (389.7 \text{ N} + -382 \text{ N}) \div 42 \text{ kg}$$

$$a = +0.19 \text{ m/s}^2$$

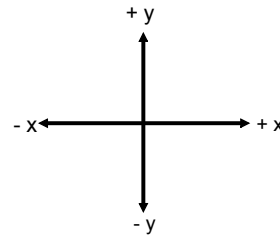
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$$F_{\text{app}} = 205 \text{ N @ } 46.5^\circ$$

$$F_{\text{ax}} = 205 \cos(46.5)$$

$$F_{\text{ay}} = 205 \sin(46.5)$$



(a)  $F_{\text{net}} = ma$  *find acceleration*

$$a = \frac{\Delta v}{\Delta t}$$

$$a = \frac{1.50 \text{ m/s} - 1.00 \text{ m/s}}{2.50 \text{ s}}$$

$$a = 0.20 \text{ m/s}^2$$

$$F_{\text{net}} = (45 \text{ kg})(0.20 \text{ m/s}^2)$$

$$= 9.0 \text{ N}$$

(c)  $F_{\text{ax}} = 141 \text{ N}$

(d)  $F_{\text{kf}} = \mu F_{\text{N}}$

$$F_{\text{nety}} = F_{\text{ay}} + F_{\text{g}} + F_{\text{N}}$$

$$0 = -441 \text{ N} + 149 \text{ N} + F_{\text{N}}$$

$$F_{\text{N}} = +292 \text{ N}$$

$$\mu = \frac{F_{\text{f}}}{F_{\text{N}}}$$

$$\mu = \frac{+132 \text{ N}}{292 \text{ N}}$$

$$\mu = 0.451$$

*can use "+132" as the formula implies the magnitude of  $F_{\text{f}}$ .*