Mathematical Equations: Modeling the Universe!

Position of a moving object:
$$\vec{d}_f = \vec{d}_o + \vec{v}_o t + \frac{1}{2} \vec{a} t^2$$

Max speed to take a corner:
$$v = \sqrt{rg\mu_s}$$

Current decay:
$$I(t) = I_0 e^{\frac{-t}{\tau}}$$

Force of gravity:
$$\vec{F}_g = G \frac{m_1 m_2}{r^2}$$

Focal point
$$\frac{1}{f} = \left(\frac{n_{lens}}{n_o} - 1\right) \left(\frac{1}{R_1} + \frac{1}{R_2}\right)$$

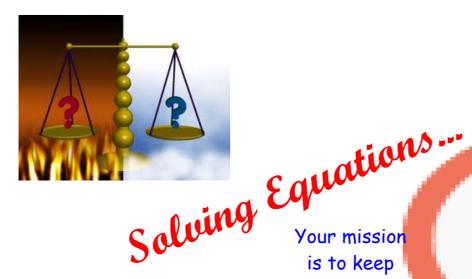
Shapes: $V = \pi r^2 h$

Triangles: $b = \frac{c}{\theta}$ Angle θ is contained between sides θ and

The cosine law states $c^2 = a^2 + b^2 - 2ab \cos\theta$.

 $\frac{dR}{dM_r} = \frac{1}{4\pi R^2 \rho} \;,$ Reason why $\frac{dL_r}{dM_r} = \epsilon - T \frac{dS}{dt} \;,$ we are alive: $\frac{dP}{dM_r} = -\frac{GM_r}{4\pi R^4} \;,$ $\frac{dT}{dM_r} = -\frac{GM_rT}{4\pi R^4 P} \nabla \;,$ Coronal Hole Coronal Hole

We will learn the general ways to setting up and solving equations.



is to keep everything in balance!!

What ever you do to one side... you must do to the other!!

Example 1

Modelling Equations with Variables on Both Sides

- a) Solve: 6x + 2 = 10 + 4x
- **b)** Verify the solution.

(22+2=10+42)

A Solution

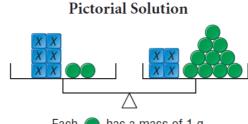
a) Rearrange the equation so that both terms containing the variable are on the same side of the equation. Then isolate the variable to solve the equation.

Draw balance scales. On the left pan, draw masses to represent 6x + 2.

On the right pan, draw masses to represent 10 + 4x.

Remove four x masses from each pan.

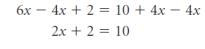
Remove two 1-g masses from each pan.

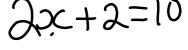


Each has a mass of 1 g.

Algebraic Solution

$$6x + 2 = 10 + 4x$$

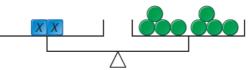




$$2x + 2 - 2 = 10 - 2$$
$$2x = 8$$



Divide the masses in each pan into 2 equal groups. Each x-mass in the left pan corresponds to a group of 4 g in the right pan.



$$2 = \frac{\cancel{8}}{\cancel{3}}$$

b) Check: Substitute x = 4 in each side of the equation.

Left side =
$$6x + 2$$

= $6(4) + 2$
= $24 + 2$
= 26

Right side =
$$10 + 4x$$

= $10 + 4(4)$
= $10 + 16$
= 26

Since the left side equals the right side, x = 4 is correct.

$$\frac{2x = 8}{2}$$

$$3C = 4$$

Equations in the form ax + b = c

$$5x + 723 = 15$$

$$5x + 723 - 723 = 15 - 723$$

$$5x = -708$$

$$5x = -708$$

$$5x = -141.6$$

Warm up Challenge



What number, when multiplied by 3 and then subtracted from 13 is the same as 42 taken away from 2 times the number?

$$|3-3x-2x=2x-42|$$

$$|3-3x-2x=2x-42|$$

$$|3-5x=-42|$$

$$|3-13-5x=-42-13|$$

$$-5x=-55$$

$$-5x=-11$$

1.
$$-2x + 51 = -3$$

 $-2x + 51 - 51 = -3 - 51$
 $-2x = -54$
 $-2 = 27$

2.
$$17 = 17 - 32p$$

 $|7 - 17 = 17 - 32p - 17$
 $0 = -32p$
 -32
 $0 = P$

3.
$$-39 = -18w - 21$$

 $-39 + 21 = -18w - 21 + 21$
 $-18 = -18w$
 -18
 -18

4.
$$-14t + 7 = 49$$
 $-14t + 7 = 49$
 $-14t = 42$
 $-14t = 42$
 -14
 $t = -3$