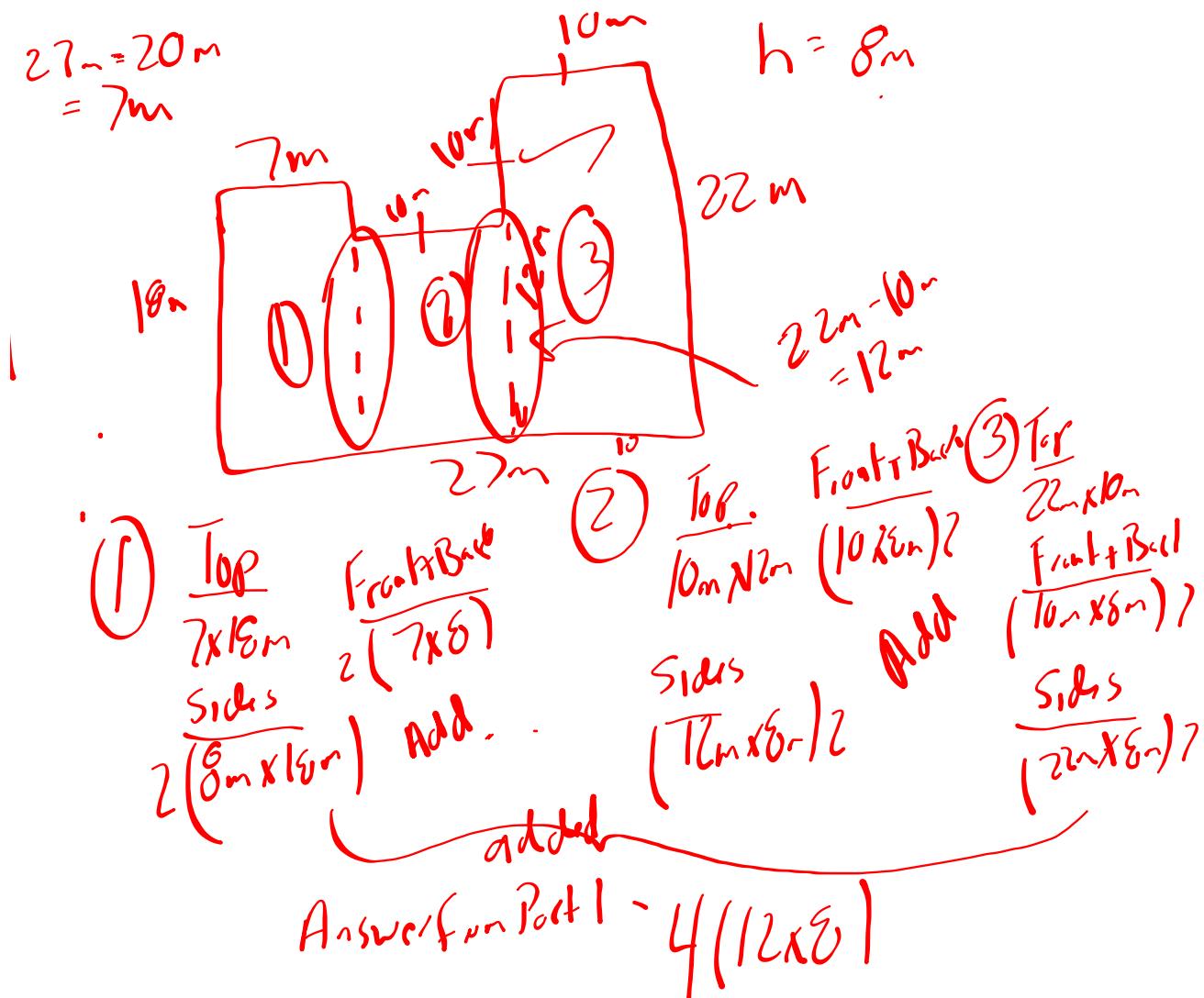




Section 14

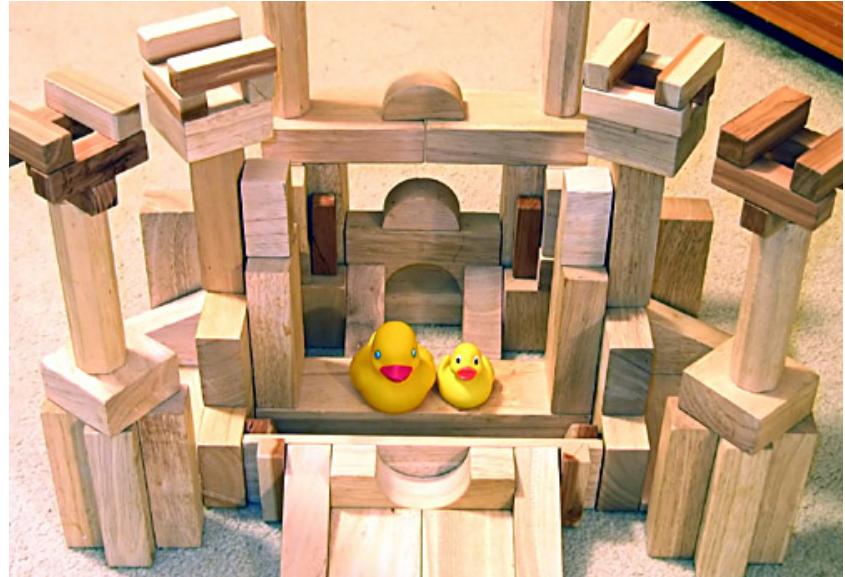


Surface Area Of Other Composite Objects





Surface area????



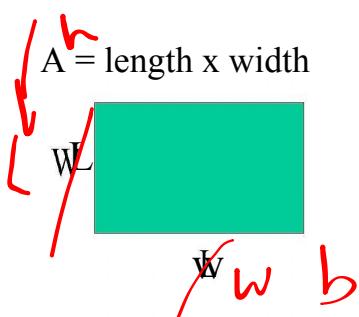
Other Composite Shapes

3-D shapes sitting on other 3-D shapes (This will cause an overlap meaning that the entire two or more shapes are not exposed to the surface)



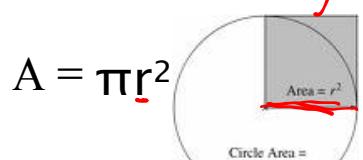
Area of Shapes

Area of a Rectangle



$$A = \text{length} \times \text{width}$$

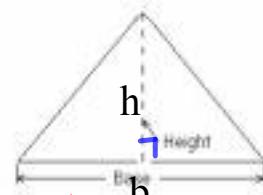
Area of a Circle



$$A = \pi r^2$$

Area of Triangle

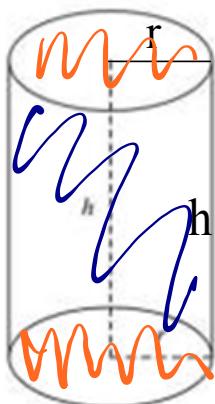
$$A = \frac{1}{2} (\text{base} \times \text{height})$$



$$\frac{b \times h}{2}$$

$$\begin{aligned} & 2\pi r^2 \\ & 2\pi(3)^2 \\ & 2\pi(9) \end{aligned}$$

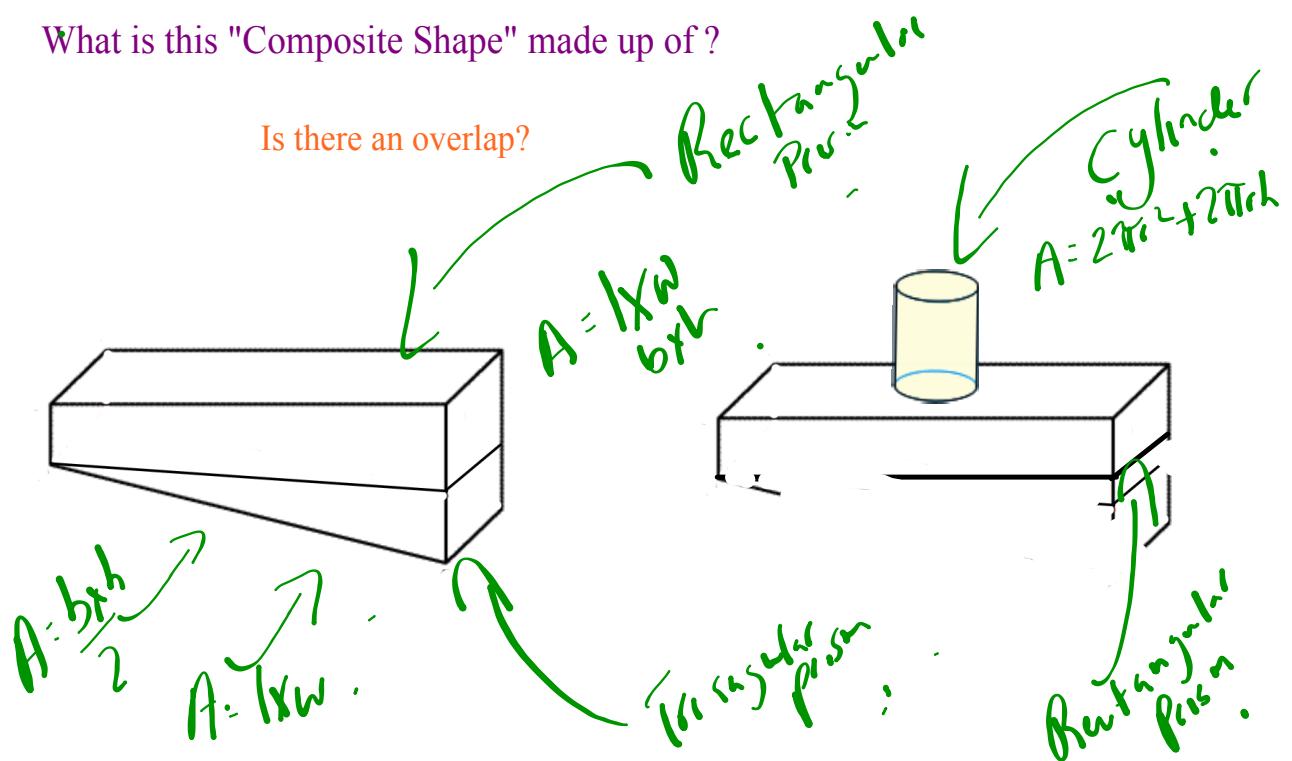
Handwritten notes: $2\pi r^2$, $2\pi(3)$, $2\pi(9)$, 3.14 , point value , radius height .



2 circles + rectangle

$$\text{Surface Area of Cylinder} = 2\pi r^2 + 2\pi rh$$

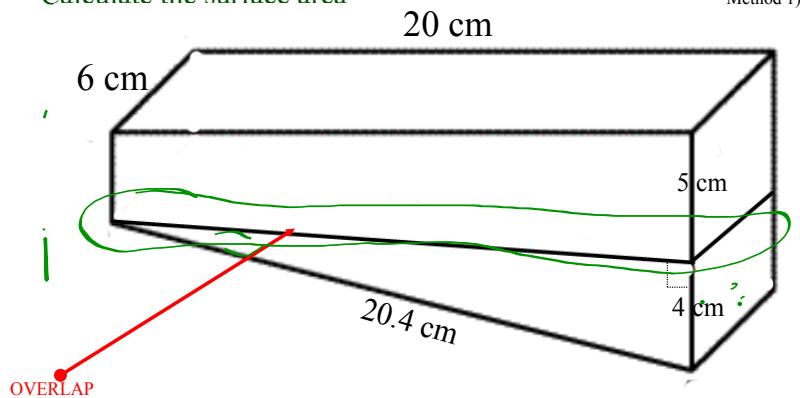
What is this "Composite Shape" made up of?



rectangle

Answer: Area of (both faces) - Area you can't see (two rectangles)

Calculate the surface area



Step 1) Calculate the overlap area BUT remember 2 faces are involved

$$\begin{aligned}
 A &= 6 \text{ cm} \times 20 \text{ cm} \\
 &= 120 \text{ cm}^2 \\
 &\xrightarrow{\quad \times 2 \quad} \text{Double overlap} \\
 &= 240 \text{ cm}^2 \quad \text{total overlap}
 \end{aligned}$$

Step 2) Calculate the Surface area of each Prism INDIVIDUALLY

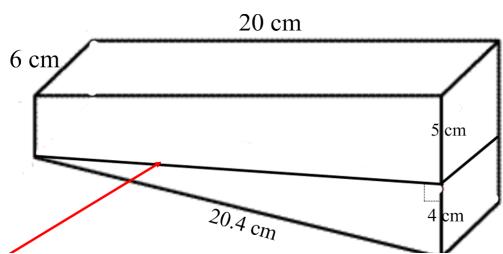
Rectangular prism (Surface exposed)

$$\begin{aligned}
 &\text{Front Face: } 20\text{cm} \times 6\text{cm} \quad \text{Times 2} \quad \text{Back Face: } 20\text{cm} \times 6\text{cm} \quad \text{Times 2} \quad \text{Side Face: } 6\text{cm} \times 5\text{cm} \quad \text{Times 2} \\
 A &= 6\text{cm} \times 20\text{cm} \\
 &= 120 \text{ cm}^2 \\
 A &= 5\text{cm} \times 20\text{cm} \\
 &= 100 \text{ cm}^2 \\
 A &= 5\text{cm} \times 6\text{cm} \\
 &= 30 \text{ cm}^2 \\
 \text{Area of rectangular prisms} &= 2(120) \text{ cm}^2 + 2(100 \text{ cm}^2) + 2(30 \text{ cm}^2) \\
 &= 240 \text{ cm}^2 + 200 \text{ cm}^2 + 60 \text{ cm}^2 \\
 &= 500 \text{ cm}^2
 \end{aligned}$$

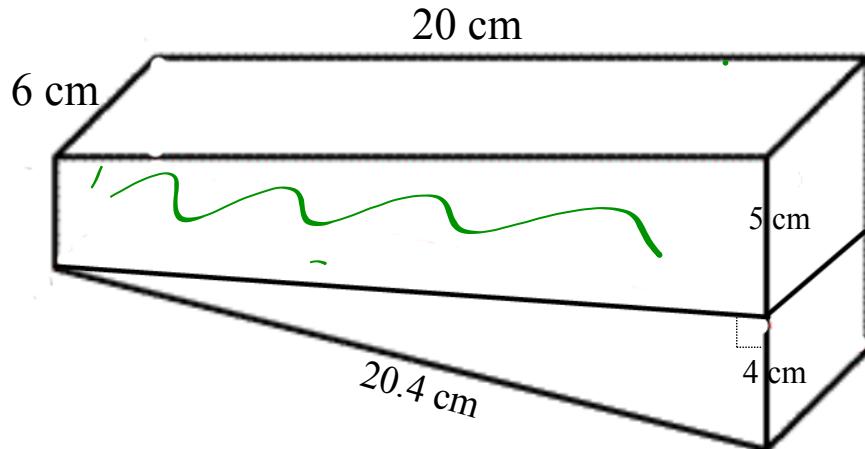
Multiply Then Add

$$\begin{aligned}
 &\text{Triangular Prism: } \text{Base: } 20\text{cm} \times 4\text{cm} \quad \text{Times 2} \quad \text{Sides: } 6\text{cm} \times 20\text{cm} \quad \text{Times 2} \quad \text{Back: } 20.4\text{cm} \times 6\text{cm} \quad \text{Times 2} \quad \text{Top: } 20.4\text{cm} \times 6\text{cm} \quad \text{Times 2} \quad \text{Bottom: } 20\text{cm} \times 6\text{cm} \quad \text{Times 2} \\
 A &= (20\text{cm} \times 4\text{cm}) / 2 \\
 &= (80 \text{ cm}^2) / 2 \\
 &= 40 \text{ cm}^2 \\
 A &= 4\text{cm} \times 6\text{cm} \\
 &= 24 \text{ cm}^2 \\
 A &= 20.4 \text{cm} \times 6\text{cm} \\
 &= 122.4 \text{ cm}^2 \\
 \text{Area of triangular prism} &= 2(40 \text{ cm}^2) + 24 \text{ cm}^2 + 122.4 \text{ cm}^2 + 120 \text{ cm}^2 \\
 &= 80 \text{ cm}^2 + 24 \text{ cm}^2 + 122.4 \text{ cm}^2 + 120 \text{ cm}^2 \\
 &= 346.4 \text{ cm}^2
 \end{aligned}$$

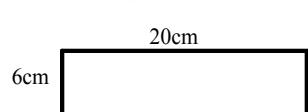
$$\begin{aligned}
 \text{Total Surface Area} &= \text{Rectangular prism} + \text{Triangular Prism} - \text{OVERLAP} \\
 &= (500 \text{ cm}^2) + 346.4 \text{ cm}^2 - 240 \text{ cm}^2 \\
 &= 606.4 \text{ cm}^2
 \end{aligned}$$



Calculate the surface area

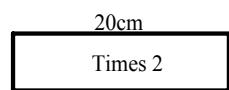


Rectangular prism (Surface exposed)



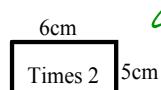
$$A = 6\text{cm} \times 20\text{cm} \\ = 120\text{cm}^2$$

Not Top



$$A = 5\text{cm} \times 20\text{cm} \\ = 100\text{cm}^2$$

Flat Back

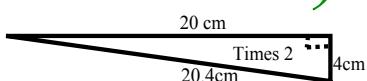


$$A = 5\text{cm} \times 6\text{cm} \\ = 30\text{cm}^2$$

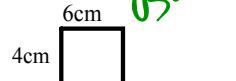
Sides

$$\text{Area of rectangular prisms exposed} = 120\text{cm}^2 + 2(100\text{cm}^2) + 2(30\text{cm}^2) \\ = 120\text{cm}^2 + 200\text{cm}^2 + 60\text{cm}^2 \\ = 380\text{cm}^2$$

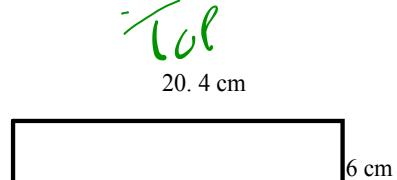
Triangular Prism (Surface Exposed)



$$A = (20\text{cm} \times 4\text{cm}) / 2 \\ = (80\text{cm}^2) / 2 \\ = 40\text{cm}^2$$



$$A = 4\text{cm} \times 6\text{cm} \\ = 24\text{cm}^2$$



$$A = 20.4\text{cm} \times 6\text{cm} \\ = 122.4\text{cm}^2$$

Not Top Base

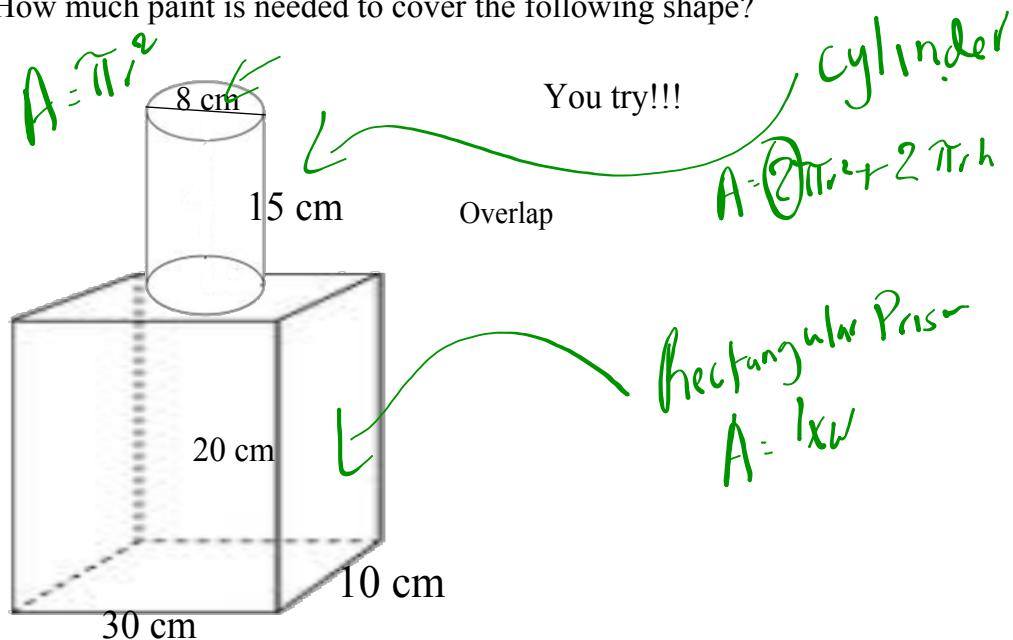
$$\text{Area of triangular prism exposed} = 2(40\text{cm}^2) + 24\text{cm}^2 + 122.4\text{cm}^2 \\ = 80\text{cm}^2 + 24\text{cm}^2 + 122.4\text{cm}^2 \\ = 226.4\text{cm}^2$$

$$\text{Total Surface Area} = \text{Rectangular prism exposed} + \text{Triangular Prism Exposed}$$

$$= \underline{(380\text{cm}^2)} + \underline{226.4\text{cm}^2}$$

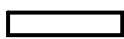
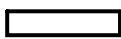
$$= 606.4\text{cm}^2$$

How much paint is needed to cover the following shape?



Cylinder

Rectangular Prism



Total Surface Area =