

61 [W66°N], and $C = 50$ m [E76°S]

d. $2B - 3C = \vec{F}$



$$B_E = -61 \cos 66$$

$$= \underline{-25 \text{ m}}$$

$$B_N = 61 \sin 66$$

$$= \underline{56 \text{ m}}$$

$$C_E = 50 \cos 76$$

$$= \underline{12 \text{ m}}$$

$$C_N = -50 \sin 76$$

$$= \underline{-49 \text{ m}}$$

$$F_E = 2B_E - 3C_E$$

$$= 2(-25) - 3(12)$$

$$= -50 - 36$$

$$= -86 \text{ m}$$

$$F_N = 2B_N - 3C_N$$

$$= 2(56) - 3(-49)$$

$$= 112 + 147$$

$$= 259 \text{ m}$$

$$|\vec{F}| = \sqrt{(F_E)^2 + (F_N)^2} = \sqrt{(-86)^2 + (259)^2}$$

$$= 273 \text{ m}$$

$$\theta = ? \quad \tan \theta = \left| \frac{F_N}{F_E} \right|$$

$$\theta = \tan^{-1} \left| \frac{259}{86} \right| = 72^\circ$$

$$\vec{F} = 273 \text{ m [W } 72^\circ \text{ N]}$$

Physics 122: Application of Vectors Examples

5. An object initially has a velocity of 25 m/s [E62°N] and accelerates at 5.5 m/s² [E12°N] for 15 seconds. What is the displacement in that time?

$$\vec{v}_0 = 25 \text{ m/s [E } 62^\circ \text{ N]} \quad \vec{a} = 5.5 \text{ m/s}^2 \text{ [E } 12^\circ \text{ N]} \quad \begin{matrix} \uparrow \text{ N} \\ \rightarrow \text{ E} \end{matrix}$$

$$t = 15 \text{ s} \quad \vec{d}_f = ? \quad \vec{d}_0 = 0 \text{ m}$$

$$v_{0E} = 25 \cos 62$$

$$= \underline{11.7 \text{ m/s}}$$

$$v_{0N} = 25 \sin 62$$

$$= \underline{22.1 \text{ m/s}}$$

$$a_E = 5.5 \cos 12$$

$$= \underline{5.4 \text{ m/s}^2}$$

$$a_N = 5.5 \sin 12$$

$$= \underline{1.1 \text{ m/s}^2}$$

$$\vec{d}_f = \vec{d}_0 + \vec{v}_0 t + \frac{1}{2} a t^2$$

$$d_{fE} = v_{0E} t + \frac{1}{2} a_E t^2 \quad \left| \quad d_{fN} = v_{0N} t + \frac{1}{2} a_N t^2 \right.$$

$$= (11.7)(15) + \frac{1}{2} (5.4)(15)^2 \quad \left| \quad = (22.1)(15) + \frac{1}{2} (1.1)(15)^2 \right.$$

$$= 175.5 + 607.5 \quad \left| \quad = 331.5 + 123.8 \right.$$

$$= \underline{783 \text{ m}} \quad \left| \quad = \underline{455.3 \text{ m}} \right.$$

$$|d_f| = \sqrt{(d_{fE})^2 + (d_{fN})^2}$$

$$= \sqrt{(783)^2 + (455.3)^2}$$

$$= \underline{906 \text{ m}}$$

$$\theta = \tan^{-1} \left| \frac{d_{fN}}{d_{fE}} \right| = \tan^{-1} \frac{455.3}{783} = \tan^{-1}(0.58)$$

$$\theta = 30^\circ$$

$$\boxed{\vec{d}_f = 906 \text{ m [E } 30^\circ \text{ N]}}$$