

Questions From Homework

① h) $3x^4 + 7x^3 + 2x^2$

$x^2(3x^2 + 7x + 2)$ Trinomial
Decomposition

$x^2(3x^2 + 6x)(x + 2)$

$x^2(3x(x + 2) + 1(x + 2))$

$x^2(3x + 1)(x + 2)$

② d) $y^3 - 9y$

$y(y^2 - 9)$ Difference
of Squares

$y(y + 3)(y - 3)$

② f) $x^6 + 8$

$(x^2 + 2)(x^4 - 2x^2 + 4)$

② h) $r^8 - 1$

$(r^4 + 1)(r^4 - 1)$

$(r^4 + 1)(r^2 + 1)(r^2 - 1)$

$(r^4 + 1)(r^2 + 1)(r + 1)(r - 1)$

$$\textcircled{3} \text{ a) } (x^3 - x^2) \div (16x + 16)$$

$$x^2(x-1) - 16(x-1)$$

$$(x-1)(x^2 - 16)$$

$$(x-1)(x-4)(x+4)$$

$$\text{b) } x^3 - 7x + 6 \quad \text{or} \quad x^3 + 0x^2 - 7x + 6$$

$$(1)^3 - 7(1) + 6$$

$$1 - 7 + 6$$

$$0$$

$(x-1)$ is a factor

$$\begin{array}{r} \underline{\underline{x-1}} \overline{) \begin{array}{l} x^3 + 0x^2 - 7x + 6 \\ - (x^3 - x^2) \\ \hline \end{array}} \end{array}$$

$$\begin{array}{r} x^2 - 7x \\ - (x^2 - x) \\ \hline \end{array}$$

$$\begin{array}{r} -6x + 6 \\ - (-6x + 6) \\ \hline \end{array}$$

$$0$$

$$\frac{(x-1)(x^2 + x - 6)}{(x-1)(x+3)(x-2)}$$

Synthetic Substitution

Factor using synthetic substitution $x^3 - 7x^2 - 4x + 28$

$$\begin{array}{r} (2)^3 - 7(2)^2 - 4(2) + 28 \\ 8 - 28 - 8 + 28 \\ 0 \end{array}$$

Find a value of x that makes it equal 0

(x-value)

$$\begin{array}{r} 2 \\ \hline \end{array}$$

(Coefficients of the polynomial)

$$\begin{array}{cccc} 1 & -7 & -4 & 28 \end{array}$$

$$\begin{array}{r} 1 \\ \hline \end{array}$$

① Bring down the first coefficient

(x-value)

$$\begin{array}{r} 2 \\ \hline \end{array}$$

(Coefficients of the polynomial)

$$\begin{array}{cccc} 1 & -7 & -4 & 28 \end{array}$$

$$\begin{array}{r} 2 \\ \hline 1 \quad -5 \end{array}$$

② Multiply the first coefficient by the x-value and place under the second coefficient. ADD.

(x-value)

$$\begin{array}{r} 2 \\ \hline \end{array}$$

(Coefficients of the polynomial)

$$\begin{array}{cccc} 1 & -7 & -4 & 28 \end{array}$$

$$\begin{array}{r} 2 \quad -10 \quad -28 \\ \hline 1 \quad -5 \quad -14 \quad \emptyset \end{array}$$

③ Repeat the steps. The coefficients of the other factor are in the bottom row.

$$(x-2)(x^2-5x-14)$$

$$(x-2)(x+2)(x-7)$$

$$x^3 + 5x^2 - 2x - 24$$

Find a value of x that makes it equal 0

$$(2)^3 + 5(2)^2 - 2(2) - 24$$

$$8 + 20 - 4 - 24$$

0

(x-value)

2

(Coefficients of the polynomial)

1 5 -2 -24

 2 14 24

1 7 12 0

$$(x-2)(x^2 + 7x + 12)$$

$$(x-2)(x+3)(x+4)$$

Homework

③③ $(x+2)$ is a factor of x^3+2x^2+kx+6

$$(-2)^3 + 2(-2)^2 + k(-2) + 6 = 0$$