

## Questions from Homework

$$\textcircled{4} \text{ a) } \log_2 5 + \log_2 6.4 + \log_2 4$$

$$= \log_2 (5 \times 6.4 \times 4)$$

$$= \log_2 128$$

$$= 7$$

$$2^y = 128$$

$$2^y = 2^7$$

$$y = 7$$

$$8 \text{ c) } \log_3 (x+y) + \log_3 (x-y) - (\log_3 x + \log_3 y)$$

$$= \log_3 \underline{(x+y)} + \log_3 \underline{(x-y)} - \log_3 xy$$

$$= \log_3 (x^2 - y^2) - \log_3 xy$$

$$= \log_3 \left( \frac{x^2 - y^2}{xy} \right)$$

# Logarithms

exponential form

$$x = a^y$$

Say "the base  $a$  to the exponent  $y$  is  $x$ ."

logarithmic form

$$y = \log_a x$$

*Handwritten annotations:*  
- "exponent" with an arrow pointing to  $y$   
- "Base" with an arrow pointing to  $a$   
- "answer" with an arrow pointing to  $x$

Say " $y$  is the exponent to which you raise base  $a$  to get the answer  $x$ ."

$$x = a^y \longleftrightarrow y = \log_a x$$

## Law of Logarithms for Powers

$$\log_a(N^p) = p \log_a N$$

$$N \in R, a > 0, a \neq 1$$

Since  $p$  can be expressed as a whole number or a fraction, this law can be expressed as follows.

## Law of Logarithms for Roots

$$\log_a(N^{\frac{p}{q}}) = \frac{p}{q} \log_a N$$

$$N \in R, a > 0, a \neq 1$$

## Example 1

$$\begin{aligned} \text{a) } & \log_{10} \sqrt[4]{1000} \\ &= \log_{10} (1000^{\frac{1}{4}}) \\ &= \frac{1}{4} (\log_{10} 1000) \\ &= \frac{1}{4} (3) \\ &= \frac{3}{4} \end{aligned}$$

$$\begin{aligned} \text{b) } & \log_2 32^{\frac{1}{3}} \\ &= \frac{1}{3} (\log_2 32) \\ &= \frac{1}{3} (5) \\ &= \frac{5}{3} \end{aligned}$$

## Example 2 Combining Laws

Express each of the following as a single logarithm.

a)  $3\log_3 2 + \log_3 4$   
 $\log_3 2^3 + \log_3 4$   
 $\log_3 8 + \log_3 4$   
 $\log_3 32$

b)  $2\log_2 9 + \log_2 6 - 3\log_2 3$   
 $\log_2 9^2 + \log_2 6 - \log_2 3^3$   
 $\log_2 81 + \log_2 6 - \log_2 27$   
 $\log_2 \left( \frac{81 \cdot 6}{27} \right)$   
 $\log_2 18$

# Homework