

Math 10

**GEOMETRY
AND
PACKAGING**

Math 10





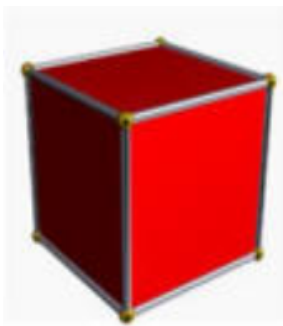
Background Information

Toys, foods and clothing all are packaged into boxes. These packages can be any shape or size.

Sometimes the shape and dimensions (width, depth, and height) are determined by the shape and dimension of the product. But sometimes the shape and dimensions depends on the most economical container.

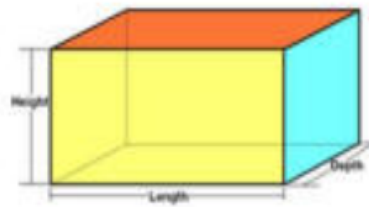
Contents that have no shape (Cereal, oil)

The naming game :)



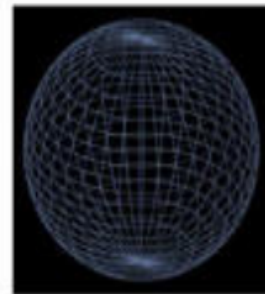
Cube

1



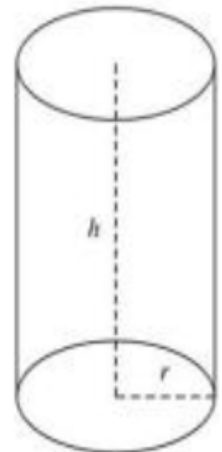
Rectangular Prism

2



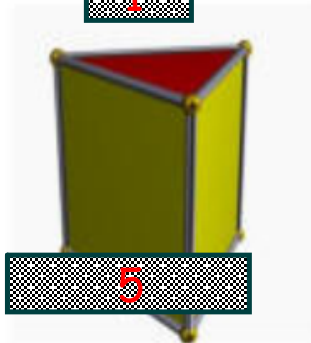
Sphere

3



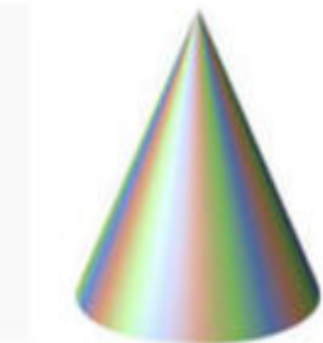
Cylinder

4



Triangular Prism

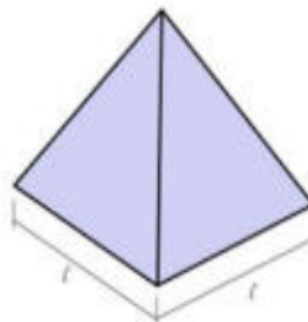
5



Cone

6

7

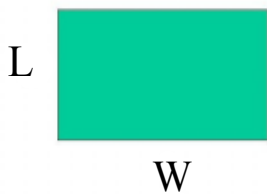


Pyramid

Area of Shapes

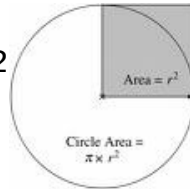
Area of a Rectangle

A = length x width



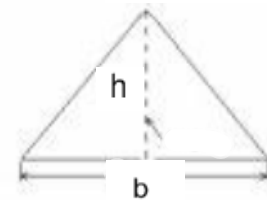
Area of a Circle

$$A = \pi r^2$$



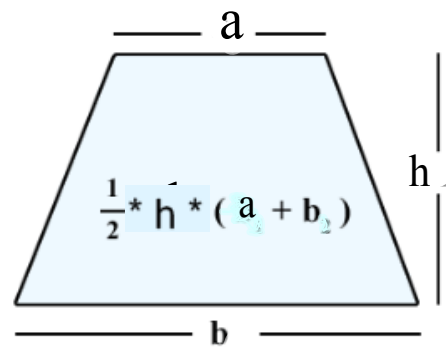
Area of Triangle

$$A = \frac{1}{2} (\text{base} \times \text{height})$$



Area of Trapezoid

$$A = \frac{1}{2} \text{height} (a + b)$$



Volume of Containers

To save money volume should be close as possible to the volume of the product



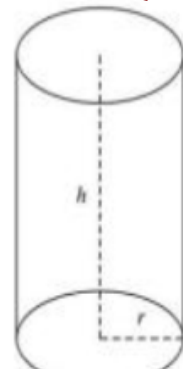
Triangular Prism

Prisms



Rectangular Prism

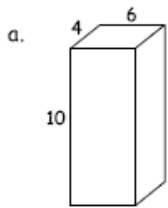
We have to use cross-sections to help determine the area and volume of a container



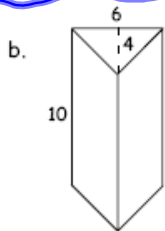
Cylinder

$$\text{Volume} = (\text{Area of the base}) \times \text{Height}$$

Find the volumes (dimensions are cm):



$$\begin{aligned} & l \times w \times h \\ & 4 \times 6 \times 10 \\ & = 240 \text{ cm}^3 \end{aligned}$$

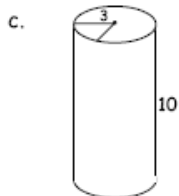


$$\left(\frac{b \times h}{2} \right) \times H$$

$$\left(\frac{6 \times 4}{2} \right) \times 10$$

$$\left(\frac{24}{2} \right) \times 10$$

$$12 \times 10 = 120 \text{ cm}^3$$



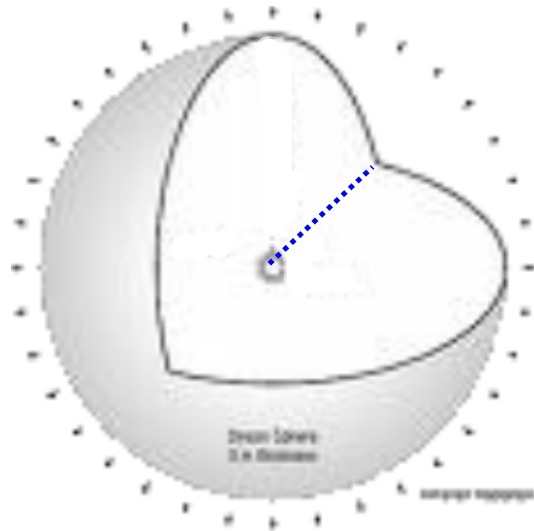
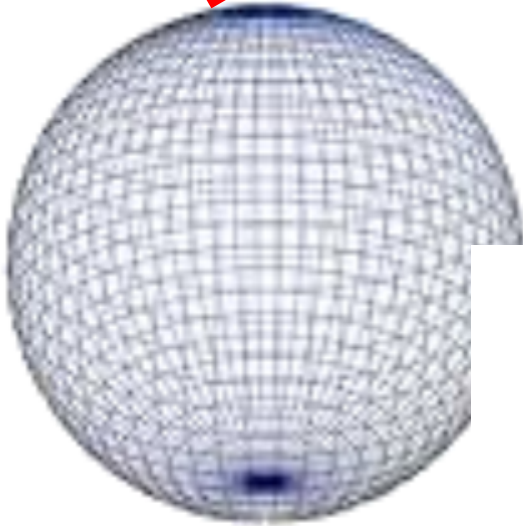
$$\pi r^2 \times H$$

$$\pi (3)^2 \times 10$$

$$\pi \times 9 \times 10$$

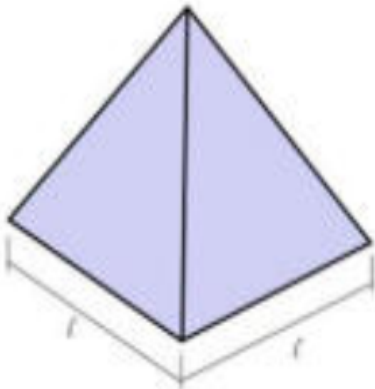
$$= 282.7 \text{ cm}^3$$

Sphere



$$V = \frac{4}{3}\pi r^3$$

Anything that comes to a point !!



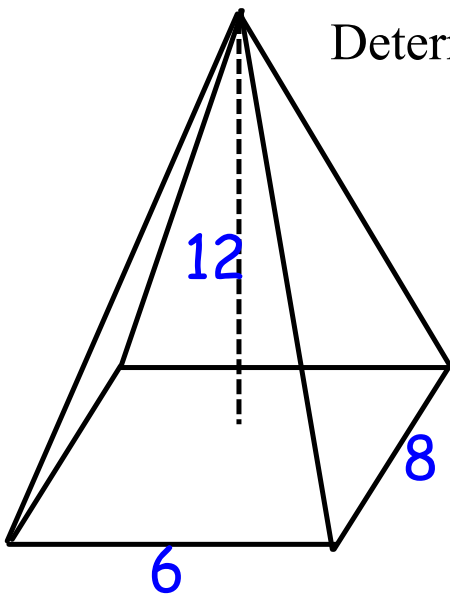
Pyramid

Pyramid
or
Cone



Cone

$$V = \frac{1}{3} (\text{Area of base}) \times \text{Height}$$



Determine the Volume

Step 1) Find the area of the base

$$\begin{array}{l} L \times W \\ 6 \times 8 \\ = 48 \end{array}$$

Step 2) This is a pyramid.

Use the equation to find volume.

$$\begin{array}{l} \frac{48 \times 12}{3} \\ = 192 \text{ cm}^3 \end{array}$$

A "DrumStick" icecream bar has the following dimensions shown.
What is the volume?



$$\frac{\pi r^2 \times H}{3}$$
$$\frac{\pi (4)^2 \times 13}{3}$$
$$\frac{\pi \times 16 \times 13}{3}$$
$$\frac{653.5}{3}$$
$$= 217.8$$

