

# System of Equations

Point of Intersection

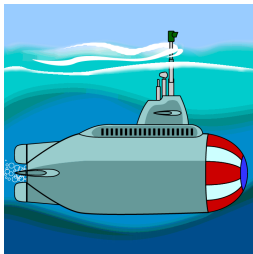
# Substitution

## Substitution Method

Steps:

- i) Choose one equation and isolate one variable;  
this equation will be considered the first equation.  
(easiest one to get  $x=$  or  $y=$  from either eqn 1 or eqn 2)
- ii) Substitute the solution from step 1 into the second equation and solve for the variable in the equation.
- iii) Using the value found in step 2, substitute it into the first equation and solve for the second variable.
- iv) Substitute the values for both variables into both equations to show they are correct.

# Substitution



You need to isolate  $x$  or  $y$

$$y = 3 + 3x \quad (1)$$

$$+3x - 8y = -3 \quad (2)$$

$$(-1, 0)$$

$$3x - 8(3 + 3x) = -3$$

$$3x + 24 - 24x = -3 + 24$$

$$\frac{-21x}{-21} = \frac{21}{-21}$$

$$x = -1$$

$$y = 3 + 3(-1)$$

$$y = 3 - 3$$

$$y = 0$$

Solve this system of equation by substitution.

$$y = 15 + 6x \quad (1)$$

$$-3x - 2y = 0 \quad (2)$$

$$-3x - 2(15 + 6x) = 0$$

$$-3x - 30 - 12x = 0$$

$$\frac{-15x}{-15} = \frac{+30}{-15}$$

$$x = -2$$

$$y = 15 + 6(-2)$$

$$y = 15 - 12$$

$$y = 3$$

$$(-2, 3)$$

$$-3x - 2y = 0$$

$$-3x - 2(15 + 6x) = 0$$

$$-3x - 30 - 12x = 0$$

$$-3x - 12x = 0 + 30$$

$$-15x = 30$$

$$x = -2$$

$$y = 15 + 6x$$

$$y = 15 + 6(-2)$$

$$y = 15 - 12$$

$$y = 3$$

$$(-2, 3)$$

## Substitution

$$y = 2x + 2 \quad (1)$$

$$y = 6x + 14 \quad (2)$$

$$y = 6x + 14$$

$$2x + 2 = 6x + 14$$

$$2x - 6x = 14 - 2$$

$$\frac{-4x}{-4} = \frac{12}{-4}$$

$$x = -3$$

$$(-3, -4)$$

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$$y = 2(-3) + 2$$

$$y = -6 + 2$$

$$y = -4$$

What if??  ~~$8x - 2y = -2$~~  ①

~~$-4x + 3y = 11$~~  ②

Rearrange ①

$8x + 2y = -2$

$-2y = -2 - 8x$   
 $-2y = -2 - 8x$

$y = 1 + 4x$  ①

$-4x + 3(1 + 4x) = 11$

$-4x + 3 + 12x = 11 - 3$

$-4x + 12x = 8$

$\frac{8x}{8} = \frac{8}{8}$

$x = 1$

$y = 1 + 4(1)$   
 $y = 5$

$(1, 5)$

Solve the system by Substitution Method

$$x + 2y = 3$$

$$3x + 5y = 8$$

.....solve for x..... $x = 3 - 2y$

$$3x + 5y = 8$$

$$3(3-2y) + 5y = 8$$

$$9 - 6y + 5y = 8$$

$$-6y + 5y = 8 - 9$$

$$y = 1 \quad -y = -1$$



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$$x + 2y = 3$$

$$x + 2(1) = 3$$

$$x + 2 = 3$$

$$x = 3 - 2$$

$$x = 1$$

(1,1)

Use Substitution to Find the Point of Intersection

$$\begin{aligned} 1) \quad & \cancel{x - 4y = 6} \quad \textcircled{1} \\ & \underline{7x + 6y = 8} \quad \textcircled{2} \end{aligned}$$

Rearrange ①

$$x - 4y = 6$$

$$x = 6 + 4y$$

$$(2, -1)$$

$$7(6 + 4y) + 6y = 8$$

$$42 + 28y + 6y = 8 - 42$$

$$\frac{34y}{34} = \frac{-34}{34}$$

$$y = -1$$

$$x = 6 + 4(-1)$$

$$x = 6 - 4$$

$$x = 2$$

