

Determining the Number of Possible Combinations (Order does not matter)

When counting with *Permutations*, the order the objects are chosen is important. When the order of choosing does not have to be considered, we refer to *Combinations*. A combination is a subset of the number of **permutations** and as such, the number of **combinations** for a particular situation is always less than the number of **permutations**.

The expression for evaluating **combinations** is as follows:

If "**n**" is the size of the sample space, and "**r**" is the number of items chosen on each trial, then the total number of **combinations** is written as:

$${}_n\mathbf{C}_r \text{ and is calculated as } {}_n\mathbf{C}_r = \frac{n!}{r!(n-r)!}$$

Example 1

A baseball team with 12 players is allowed to send four players to a weekend batting clinic. In how many ways can the group be chosen?

Solution

Since order is not important, the group is a **combination**. You are choosing a **combination** of 4 from a group of 12.

$${}_n C_r = \frac{n!}{r!(n-r)!}$$

$${}_{12} C_4 = \frac{12!}{4!(12-4)!}$$

$${}_{12} C_4 = \frac{12!}{4! 8!}$$

$${}_{12} C_4 = 495$$

$$n = 12$$

$$r = 4$$

$${}_{12} C_4 = 495$$

Example 2

↙ and means to multiply

A committee of size 4 and a committee of size 3 are to be assigned from a group of 10 people. How many ways can this be done if no person is assigned to both committees?

Solution

1st Committee

$${}_n C_r = \frac{n!}{r!(n-r)!}$$

$${}_{10} C_4 = \frac{10!}{4!(10-4)!}$$

$${}_{10} C_4 = \frac{10!}{4! 6!}$$

$${}_{10} C_4 = 210$$

2nd Committee

$${}_n C_r = \frac{n!}{r!(n-r)!}$$

$${}_6 C_3 = \frac{6!}{3!(6-3)!}$$

$${}_6 C_3 = \frac{6!}{3! 3!}$$

$${}_6 C_3 = 20$$

Committee of size 4 AND Committee of size 3

$$210 \quad \times \quad 20$$

$$= 4200 \text{ ways}$$

There are 4200 ways to form a committee of size 4 and a committee of size 3 from a group of 10 people if no person is assigned to both committees.

$$\textcircled{1} \begin{array}{l} n=7 \\ r=4 \end{array} \quad {}_7C_4 =$$