Problem of the Week Grade 11 and 12

A Simple System of Equations? Solution

Problem

If $2^{3x} = 16^{y+1}$ and 2x = 5y - 17, determine the value of x + y.

Solution 1

For this solution we will attempt to answer the question only. We will not determine the values of x and y that generate the sum.

$$2^{3x} = 16^{y+1}$$

$$2^{3x} = (2^4)^{y+1}$$

$$2^{3x} = 2^{4y+4}$$

$$\therefore \quad 3x = 4y+4 \quad (1)$$
But
$$2x = 5y-17 \quad (2)$$

$$(1) - (2) \qquad x = -y+21$$
Rearranging
$$x + y = 21$$

 $\therefore x + y = 21$. Notice that the problem only asks for x + y, it is not necessary to find values for x and y.

Solution 2

This solution carries on from equations (1) and (2) in solution 1 to find the values of x and y, and then determines the sum.

As before (but with much more work) x + y = 21.



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