

## Warm Up

Prove the following identity:

$$\frac{1 + \cos 2\theta}{\sin 2\theta} = \cot \theta$$

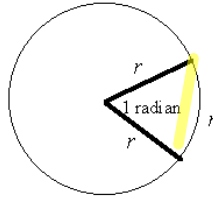
$$\begin{array}{l} \frac{1 + \cos^2 \theta - \sin^2 \theta}{2 \sin \theta \cos \theta} \\ \frac{\cos^2 \theta + \cos^2 \theta}{2 \sin \theta \cos \theta} \\ \frac{\cancel{2} \cos^2 \theta}{\cancel{2} \sin \theta \cancel{\cos \theta}} \\ \boxed{\frac{\cos \theta}{\sin \theta}} \end{array} \quad \left| \quad \boxed{\frac{\cos \theta}{\sin \theta}} \right.$$

Find an angle,  $\theta$ , coterminal with  $-225^\circ$ , where  $-360^\circ \leq \theta \leq 360^\circ$ .

$$\begin{aligned} A_c &= -225^\circ + 360^\circ \\ &= 135^\circ \end{aligned}$$

# Radian Measure

A radian is the angle subtended by an arc of length  $r$  (radius)



$$\theta = \frac{a}{r}$$

← arc length  
← radius

$$360^\circ = \frac{2\pi r}{r}$$

Degrees      Radians

$$360^\circ = 2\pi$$

$$180^\circ = \pi$$

$$1^\circ = \frac{\pi}{180} \text{ radians} \qquad 1 \text{ rad} = \frac{180}{\pi}$$

Ex. Convert the following angles from degrees to radians:

a)  $60^\circ \cdot \frac{\pi}{180^\circ}$

$$\frac{60\pi}{180^\circ}$$

$$\frac{\pi}{3}$$

b)  $728^\circ \cdot \frac{\pi}{180}$

$$\frac{728\pi}{180}$$

$$\frac{182\pi}{45}$$

c)  $-270^\circ \cdot \frac{\pi}{180}$

$$\frac{-270\pi}{180}$$

$$\frac{-3\pi}{2}$$

$$\frac{\pi}{2}$$

Ex. Convert the following angles from radians to degrees:

a)  $\pi/6$

$$\frac{\pi}{6} \cdot \frac{180}{\pi}$$

$$\frac{180\pi}{6\pi}$$

$$\boxed{30^\circ}$$

a)  $-2\pi/5$

$$-\frac{2\pi}{5} \cdot \frac{180}{\pi}$$

$$\frac{-360\pi}{5\pi}$$

$$\boxed{-72^\circ}$$

$$\boxed{288^\circ}$$

c)  $6.485 \text{ rads}$

$$6.485 \times \frac{180}{\pi}$$

$$\frac{1167.3}{\pi}$$

$$\boxed{372^\circ}$$

$$\boxed{12^\circ}$$

Ex. Find the coterminal angle,  $\theta$ , of  $\frac{\pi}{4}$  where  
 $-2\pi \leq \theta \leq 2\pi$

**Remember: Coterminal angles share the same terminal arm!**

$$A_c = \frac{\pi}{4} - 2\pi$$

$$= \frac{\pi}{4} - \frac{8\pi}{4}$$

$$= \boxed{\frac{-7\pi}{4}}$$

# Homework

Omit #7

