

Questions from Homework

$$\textcircled{1} b) i^7 + i^{23} + i^{94} + i^{112}$$

$$(i^4 \cdot i^3) + (i^{20} \cdot i^3) + (i^{92} \cdot i^2) + (1)$$

$$-i + (-i) + (-1) + 1$$

$$\boxed{-2i}$$

$$c) (\sqrt{-16})(\sqrt{-49})(\sqrt{-27})(\sqrt{-12})$$

$$(4i)(7i)(3i\sqrt{3})(2i\sqrt{3}) \rightarrow 504i^4$$

$$(28i^2)(6i^2(3)) \rightarrow \boxed{504}$$

$$(28i^2)(18i^2)$$

$$504(i^4)$$

$$\boxed{504}$$

$$\textcircled{1} d) i^{-5} + i^{-11} + i^{-18} + i^{-196}$$

$$(i^{-4} \cdot i^{-1}) + (i^{-8} \cdot i^{-3}) + (i^{-16} \cdot i^{-2}) + (1)$$

$$-i + i - 1 + 1$$

$$\boxed{0}$$

Number	"a"	"b"	O.P.	Modulus
④ $-2+5i$	-2	5	$(-2, 5)$	$\sqrt{29}$
$\sqrt{7}-\sqrt{-36}$ $=\sqrt{7}-6i$	$\sqrt{7}$	-6	$(\sqrt{7}, -6)$	$\sqrt{43}$

$$\textcircled{3} z = 5-11i$$

$$\text{a) } \bar{z} = 5+11i$$

$$\text{b) } 5-11i + (5+11i)$$

$$= 10$$

$$\text{c) } 5-11i - (5+11i)$$

$$5-11i-5-11i$$

$$= -22i$$

Positive Powers of "i"

$$i^1 = i$$

$$i^2 = -1$$

$$i^3 = -i$$

$$i^4 = 1$$

Negative Powers of "i"

$$i^{-1} = -i$$

$$i^{-2} = -1$$

$$i^{-3} = i$$

$$i^{-4} = 1$$

Notice a pattern?

For positive powers take out the largest multiple of 4
For negative powers take out the largest multiple of -4

Examples

$$i^1 = i$$

$$i^2 = -1$$

$$i^3 = -i$$

$$i^4 = 1$$

$$i^{-1} = -i$$

$$i^{-2} = -1$$

$$i^{-3} = i$$

$$i^{-4} = 1$$

$$i^8 + i^{33} + i^{83} - i^{132}$$

$$(1) + (i) + (-i) - (1)$$

$$\boxed{0}$$

$$i^{-9} + i^{-28} + i^{-83} - i^{-129}$$

$$(i^{-8} \cdot i^{-1}) + (1) + (i^{-80} \cdot i^{-3}) - (i^{-128} \cdot i^{-1})$$

$$(-i) + (1) + (i) - (-i)$$

$$\boxed{1+i}$$

Simplify the following!

$$\frac{(2+3i)(3-i)}{(1-5i)(2+4i)}$$

$$\frac{6+7i-3(i^2)}{2-6i-20(i^2)}$$

$$\frac{(9+7i)(22+6i)}{(22-6i)(22+6i)}$$

$$\frac{198+54i+154i+42(i^2)}{484-36(i^2)}$$

$$\frac{198+208i-42}{484+36}$$

$$\frac{156+208i}{520}$$

$$\frac{156}{520} + \frac{208i}{520}$$

$$\boxed{\frac{3}{10} + \frac{2i}{5}}$$

$$\textcircled{1} \text{ es } \frac{(5+i)(4-3i)}{(2-5i)(1-i)}$$

$$\frac{20 - 11i - 3i^2}{2 - 7i + 5i^2}$$

$$\frac{(23 - 11i)(-3+7i)}{(-3-7i)(-3+7i)}$$

$$\frac{-69 + 161i + 33i - 7i^2}{9 - 49i^2}$$

$$\frac{8 + 194i}{58}$$

$$\frac{8}{58} + \frac{194i}{58}$$

$$\frac{4}{29} + \frac{97i}{29}$$

Number	"a"	"b"	ordered pair	Modulus
$\sqrt{121} + \sqrt{-16}$				
$\underline{11} + \underline{4}i$	11	4	(11, 4)	$\sqrt{137}$
4	4	0	(4, 0)	4

If $z = -3 + 2i$

find $\bar{z} = -3 - 2i$

$$\textcircled{1} f) \frac{(-1+2i)(5-4i)}{(1-2i)(5+4i)}$$

$$\frac{-5 + 14i - 8i^2}{5 - 6i - 8i^2}$$

$$\frac{(3 + 14i)(13 + 6i)}{(13 - 6i)(13 + 6i)}$$

$$\frac{39 + 18i + 182i + 84i^2}{169 - 36i^2}$$

$$\frac{-45 + 200i}{205}$$

$$\frac{-45}{205} + \frac{200i}{205}$$

$$\frac{-9}{41} + \frac{40i}{41}$$

$$\textcircled{a} \text{ b) } i^{-3} - i^{-20}$$

$$i - 1$$

$$\text{d) } i^{-10} - i^{-28} + i^{130} - i^2$$

$$(i^{-8} \cdot i^{-2}) - (1) + (i^{128} \cdot i^2) - (-1)$$

$$((1)(-1)) - 1 + ((1)(-1)) + 1$$

$$-1 - 1 - 1 + 1$$

$$-2$$