

ANSWERS \rightarrow Exercise 3.13.

1. A bowl contains 3 white and 5 black balls.

$$\begin{aligned} \text{a) } P(\text{white and black}) &= P(w) \times P(b|w) \\ &= \frac{3}{8} \times \frac{5}{7} \\ &= \frac{15}{56} \end{aligned}$$

$$\begin{aligned} \text{b) } P(\text{black and black}) &= P(b) \times P(b|b) \\ &= \frac{5}{8} \times \frac{4}{7} \\ &= \frac{20}{56} \\ &= \frac{5}{14} \end{aligned}$$

$$\begin{aligned} \text{c) } P(\text{white and white}) &= P(w) \times P(w|w) \\ &= \frac{3}{8} \times \frac{2}{7} \\ &= \frac{6}{56} \\ &= \frac{3}{28} \end{aligned}$$

2. A bag contains 4 nickels and 6 quarters

a) $P(\text{nickel and quarter})$ b) $P(\text{quarter and nickel})$

$$= P(n) \times P(q|n)$$

$$= \frac{4}{10} \times \frac{6}{9}$$

$$= \frac{2}{5} \times \frac{2}{3}$$

$$= \frac{4}{15}$$

$$= P(q) \times P(n|q)$$

$$= \frac{6}{10} \times \frac{4}{9}$$

$$= \frac{3}{5} \times \frac{4}{9}$$

$$= \frac{12}{45}$$

c) $P(\text{quarter and quarter})$ = $\frac{4}{15}$

$$= P(q) \times P(q|q)$$

$$= \frac{6}{10} \times \frac{5}{9}$$

$$= \frac{3}{5} \times \frac{5}{9}$$

$$= \frac{15}{45}$$

$$= \frac{1}{3}$$

3. A box contains 6 black chips, 9 blue chips.

a) $P(\text{black and blue})$

$$= P(\text{black}) \times P(\text{blue}|\text{black})$$

$$= \frac{6}{15} \times \frac{9}{14}$$

$$= \frac{2}{5} \times \frac{9}{14}$$

$$= \frac{18}{70}$$

$$= \frac{9}{35}$$

b) $P(\text{blue and blue and blue})$

$$= P(b) \times P(b|b) \times P(b|2b)$$

$$= \frac{9}{15} \times \frac{8}{14} \times \frac{7}{13}$$

$$= \frac{3}{5} \times \frac{4}{7} \times \frac{7}{13}$$

$$= \frac{84}{455}$$

$$= \frac{12}{65}$$

c) $P(b \text{ and } b \text{ and } b \text{ and } b \text{ and } b \text{ and } b \text{ and } b)$

$$= P(b) \times P(b|b) \times P(b|2b) \times P(b|3b) \times P(b|4b) \times P(b|5b) \times P(b|6b)$$

$$= \frac{6}{15} \times \frac{5}{14} \times \frac{4}{13} \times \frac{3}{12} \times \frac{2}{11} \times \frac{1}{10} \times \frac{0}{9}$$

$$= 0 \quad \text{IMPOSSIBLE!}$$

4a) INDEPENDENT/DEPENDENT EVENTS.

Similarities

- To get both you find the product of individual probabilities.

Differences

- Numerators / Denominators change if one event is dependent on another.

5. A box has 3 hockey and 6 football cards.

a) $P(\text{hockey and hockey})$

$$= P(h) \times P(h|h)$$

$$= \frac{3}{9} \times \frac{2}{8}$$

$$= \frac{1}{3} \times \frac{1}{4}$$

$$= \frac{1}{12}$$

b) $P(\text{hockey and football})$

$$= P(h) \times P(f|h)$$

$$= \frac{3}{9} \times \frac{6}{8}$$

$$= \frac{1}{3} \times \frac{3}{4}$$

$$= \frac{3}{12}$$

$$= \frac{1}{4}$$

100 plugs , 5 are defective

$$b) P(\text{not defective}) = 1 - P(\text{defective})$$

$$= \frac{1}{1} - \frac{5}{100}$$

$$= \frac{100}{100} - \frac{5}{100}$$

$$= \frac{95}{100}$$

$$= \boxed{\frac{19}{20}}$$

6. A box contains 100 plugs, 5 are defective.

$$\begin{aligned} \text{a) } P(\text{defective plug}) &= \frac{5}{100} \\ &= \frac{1}{20} \end{aligned}$$

$$\begin{aligned} \text{b) } P(\text{not defective}) &= 1 - P(\text{defective}) \\ &= 1 - \frac{1}{20} \\ &= \frac{20}{20} - \frac{1}{20} \\ &= \frac{19}{20} \end{aligned}$$

$$\begin{aligned} \text{c) } & P(\text{defective and defective}) \\ &= P(\text{defective}) \times P(\text{defective}) \\ &= \frac{5}{100} \times \frac{4}{99} \\ &= \frac{1}{20} \times \frac{4}{99} \\ &= \frac{4}{1980} \\ &= \frac{1}{495} \end{aligned}$$

$$\begin{aligned} \text{d) } & P(\text{not defective and not defective}) \\ &= 1 - P(\text{defective and defective}) \\ &= 1 - \frac{1}{495} \\ &= \frac{495}{495} - \frac{1}{495} \\ &= \frac{494}{495} \end{aligned}$$

7. Class \rightarrow 16 girls, 14 boys.

a) $P(\text{girl and girl})$	b) $P(\text{boy and boy})$	c) $P(\text{boy and girl})$
$= P(g) \times P(g g)$	$= P(b) \times P(b b)$	$= P(b) \times P(g b)$
$= \frac{16}{30} \times \frac{15}{29}$	$= \frac{14}{30} \times \frac{13}{29}$	$= \frac{14}{30} \times \frac{16}{29}$
$= \frac{8}{15} \times \frac{15}{29}$	$= \frac{7}{15} \times \frac{13}{29}$	$= \frac{7}{15} \times \frac{16}{29}$
$= \frac{120}{435}$	$= \frac{91}{435}$	$= \frac{112}{435}$ (Only one way!)
$= \frac{8}{29}$		$\frac{112}{435} \times 2 = \frac{224}{435}$

8. 24 Cards

- #'s 0~9
- 2 equilateral Δ 's
- 3 rectangles
- 3 squares
- 4 parallelograms
- 2 circles

$$\begin{aligned} \text{a) } P(\text{number and geometric figure}) &= P(\text{number}) \times P(\text{geometric}|\#) \\ &= \frac{10}{24} \times \frac{14}{23} \\ &= \frac{70}{276} \\ &= \frac{35}{138} \end{aligned}$$

$$b) P(\text{number and number})$$

$$= P(\#) \times P(\#/\#)$$

$$= \frac{10}{24} \times \frac{9}{23}$$

$$= \frac{5}{12} \times \frac{9}{23}$$

$$= \frac{45}{276}$$

$$= \frac{15}{92}$$

$$c) P(\Delta \text{ and } O)$$

$$= P(\Delta) \times P(O/\Delta)$$

$$= \frac{2}{24} \times \frac{2}{23}$$

$$= \frac{1}{12} \times \frac{2}{23}$$

$$= \frac{2}{276}$$

$$= \frac{1}{138}$$

$$\begin{aligned} \text{d) } P(\text{parallel and even}) &= P(p) \times P(e|p) \\ &= \frac{10}{24} \times \frac{5}{23} \\ &= \frac{5}{12} \times \frac{5}{23} \\ &= \frac{25}{276} \end{aligned}$$

$$\begin{aligned} \text{e) } P(\text{figure without right angle and parallelogram}) &= P(\text{no right}) \times P(\text{parallelogram} | \text{no right}) \\ &= \frac{4}{24} \times \frac{7}{23} \\ &= \frac{1}{6} \times \frac{7}{23} \\ &= \frac{7}{138} \end{aligned}$$