

## Midpoint of a Line Segment

Answer should be:  $(x, y)$

If  $M$  is the coordinate of the midpoint of a line segment joining  $A(x_1, y_1)$  and  $B(x_2, y_2)$ , then the coordinates of  $M$  are given by:

$$M = \left( \frac{x_2 + x_1}{2}, \frac{y_2 + y_1}{2} \right)$$

## Example

Find the midpoint between **S(3, -4)** and **T(-15, 2)**.

$$\begin{aligned}M &= \left[ \frac{x_2 + x_1}{2}, \frac{y_2 + y_1}{2} \right] \\&= \left[ \frac{-15 + 3}{2}, \frac{2 + (-4)}{2} \right] \\&= \left[ \frac{-12}{2}, \frac{-2}{2} \right] \\&= (-6, -1)\end{aligned}$$

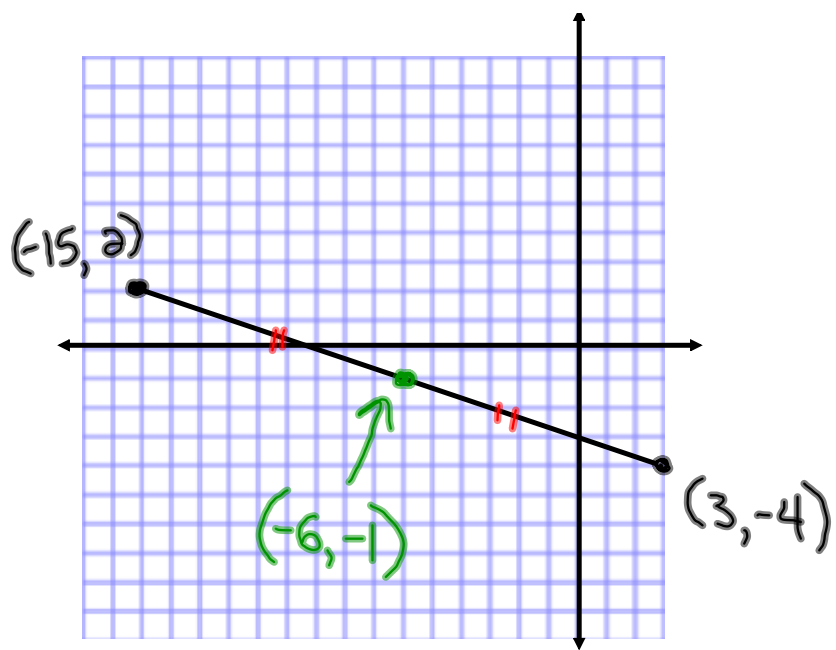
## Solution

$$(x_1, y_1) = (3, -4)$$

$$(x_2, y_2) = (-15, 2)$$

$$\begin{aligned} M_{ST} &= \left( \frac{x_2 + x_1}{2}, \frac{y_2 + y_1}{2} \right) \\ &= \left( \frac{-15 + 3}{2}, \frac{2 + (-4)}{2} \right) \\ &= \left( \frac{-12}{2}, \frac{-2}{2} \right) \\ &= (-6, -1) \end{aligned}$$

**The midpoint is therefore (-6, -1).**



## Example 2

The midpoint of AB is given by  $M(-1, 3)$  for the points  $A(\underline{-4}, \underline{2})$  and  $B(\underline{x}, \underline{y})$ .  
Find  $x$  and  $y$ .

$x$   $y$   
↓ ↓

## Solution

$$\frac{-1}{1} = \frac{(x + -4)}{2}$$

$$(-1)(2) = x - 4$$

$$-2 = x - 4$$

$$-2 + 4 = x$$

$$2 = x$$

$$\frac{3}{1} = \frac{(y + 2)}{2}$$

$$(3)(2) = y + 2$$

$$6 = y + 2$$

$$6 - 2 = y$$

$$4 = y$$

**Therefore, point B is (2, 4).**