

You try

April 11, 2012

Find the radius and center of the following circle  
(Hint: general to standard)

$$x^2 + y^2 - 24x + 20y + 163 = 0 \quad \rightarrow$$

$$\underline{x^2} + y^2 - \underline{24x} + 20y = -163$$

$$(x^2 - 24x) + (y^2 + 20y) = -163 \quad \text{---} \quad \text{(half)} \quad \text{---}$$

$$(x^2 - 24x + 144) + (y^2 + 20y + 100) = -163 + 144 + 100 \quad \text{---} \quad \text{---} \quad \text{add}$$

factor

$$(x-12)^2 + (y+10)^2 = 81$$

$$(x-h)^2 + (y-k)^2 = r^2$$

Center  $(12, -10)$

$$r^2 = 81$$

$$r = \sqrt{81}$$

$r = 9$

ANSWERS=> EQUATIONS OF A CIRCLE WORKSHEET#3

1.  $x^2 + y^2 - 8x + 8y = 22$

Step 1:  $x^2 - 8x + y^2 + 8y = 22$

Step 2:  $x^2 - 8x + 16 + y^2 + 8y + 16 = 22 + 16 + 16$

Step 3:  $(x-4)^2 + (y+4)^2 = 54$

Center  $(4, -4)$  ;  $r = \sqrt{54}$   
 $r = \sqrt{9 \times 6}$   
 $r = 3\sqrt{6}$  units

a) Center  $\Rightarrow (4, -4)$

b) Radius  $\Rightarrow 3\sqrt{6}$

$$2a) x^2 + y^2 - 6y - 3 = 0$$

Step 1:  $x^2 + y^2 - 6y = 3$

Step 2:  $x^2 + y^2 - 6y + 9 = 3 + 9$

Step 3:  $(x-0)^2 + (y-3)^2 = 12$

Center(0,3);  $r = \sqrt{12}$   
 $r = \sqrt{4 \times 3}$   
 $r = 2\sqrt{3}$  units

$$b) x^2 + y^2 - 10x - 1 = 0$$

Step 1:  $x^2 - 10x + y^2 = 1$

Step 2:  $x^2 - 10x + 25 + y^2 = 1 + 25$

Step 3:  $(x-5)^2 + (y-0)^2 = 26$

Center (5,0) ;  $r = \sqrt{26}$  units.

$$c) x^2 + y^2 - 4x - 2y + 1 = 0$$

$$\text{Step 1: } x^2 - 4x + y^2 - 2y = -1$$

$$\text{Step 2: } x^2 - 4x + 4 + y^2 - 2y + 1 = -1 + 4 + 1$$

$$\text{Step 3: } (x-2)^2 + (y-1)^2 = 4$$

Center  $(2, 1)$ ;  $r = \sqrt{4}$   
 $r = 2$  units.

$$d) x^2 + y^2 + 6x - 8y + 19 = 0$$

$$\underline{\text{Step 1:}} \quad x^2 + 6x + y^2 - 8y = -19$$

$$\underline{\text{Step 2:}} \quad x^2 + 6x + 9 + y^2 - 8y + 16 = -19 + 9 + 16$$

$$\underline{\text{Step 3:}} \quad (x+3)^2 + (y-4)^2 = 6$$

Center (-3, 4);  $r = \sqrt{6}$  units

$$e) 3x^2 + 3y^2 - 18x + 30y + 100 = 0$$

EXTRA STEP: Divide each term by 3.

$$x^2 + y^2 - 6x + 10y + \frac{100}{3} = 0$$

$$\text{Step 1: } x^2 - 6x + y^2 + 10y = -\frac{100}{3}$$

$$\text{Step 2: } x^2 - 6x + 9 + y^2 + 10y + 25 = -\frac{100}{3} + 9 + 25$$

$$\text{Step 3: } (x-3)^2 + (y+5)^2 = -\frac{100}{3} + \frac{34}{1}$$

$$(x-3)^2 + (y+5)^2 = -\frac{100}{3} + \frac{102}{3}$$

$$(x-3)^2 + (y+5)^2 = \frac{2}{3}$$

Center (3, -5);  $r = \sqrt{\frac{2}{3}}$  units.

$$f) x^2 + y^2 + 12x - 14y + 85 = 0$$

$$\text{Step 1: } x^2 + 12x + y^2 - 14y = -85$$

$$\text{Step 2: } x^2 + 12x + 36 + y^2 - 14y + 49 = -85 + 36 + 49$$

$$\text{Step 3: } (x+6)^2 + (y-7)^2 = 0$$

Center  $(-6, 7)$ ;  $r = \sqrt{0}$   
 $r = 0$ .

\* Since  $r=0$ , we have only the point  $(-6, 7)$  and not a circle.

$$g) x^2 + y^2 - 4x + 2y + 6 = 0$$

$$\text{Step 1: } x^2 - 4x + y^2 + 2y = -6$$

$$\text{Step 2: } x^2 - 4x + 4 + y^2 + 2y + 1 = -6 + 4 + 1$$

$$\text{Step 3: } (x-2)^2 + (y+1)^2 = -1$$

\* We can stop here since  $r^2 \neq -1$ !

This is not the equation of a circle or a point.

h)  $2x^2 + 2y^2 + 20x - 12y + 18 = 0$ .

EXTRA STEP: Divide each term by 2.

$$x^2 + y^2 + 10x - 6y + 9 = 0$$

Step 1:  $x^2 + 10x + y^2 - 6y = -9$

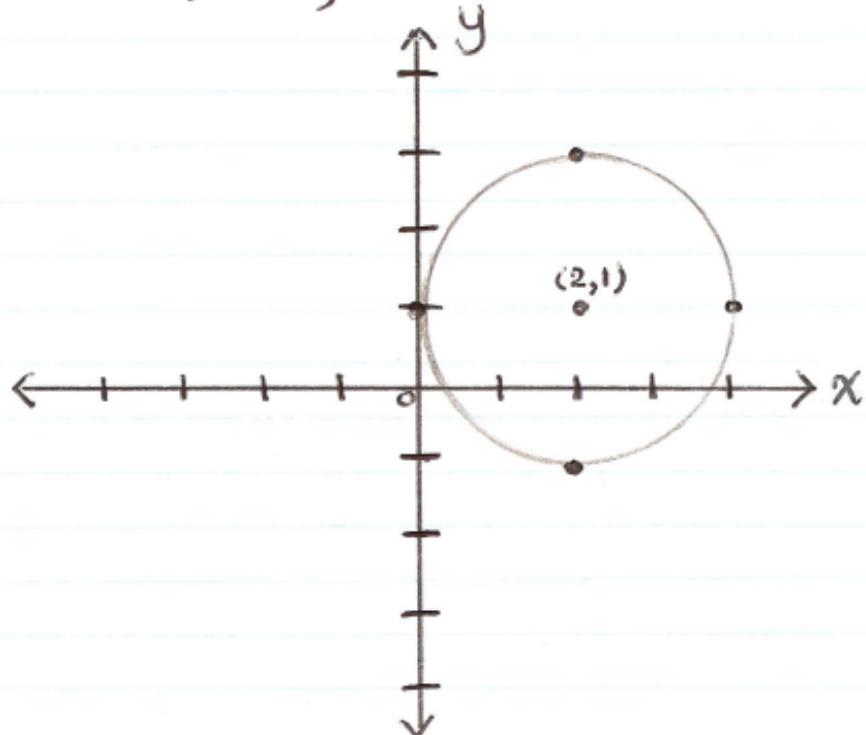
Step 2:  $x^2 + 10x + 25 + y^2 - 6y + 9 = -9 + 25 + 9$

Step 3:  $(x+5)^2 + (y-3)^2 = 25$

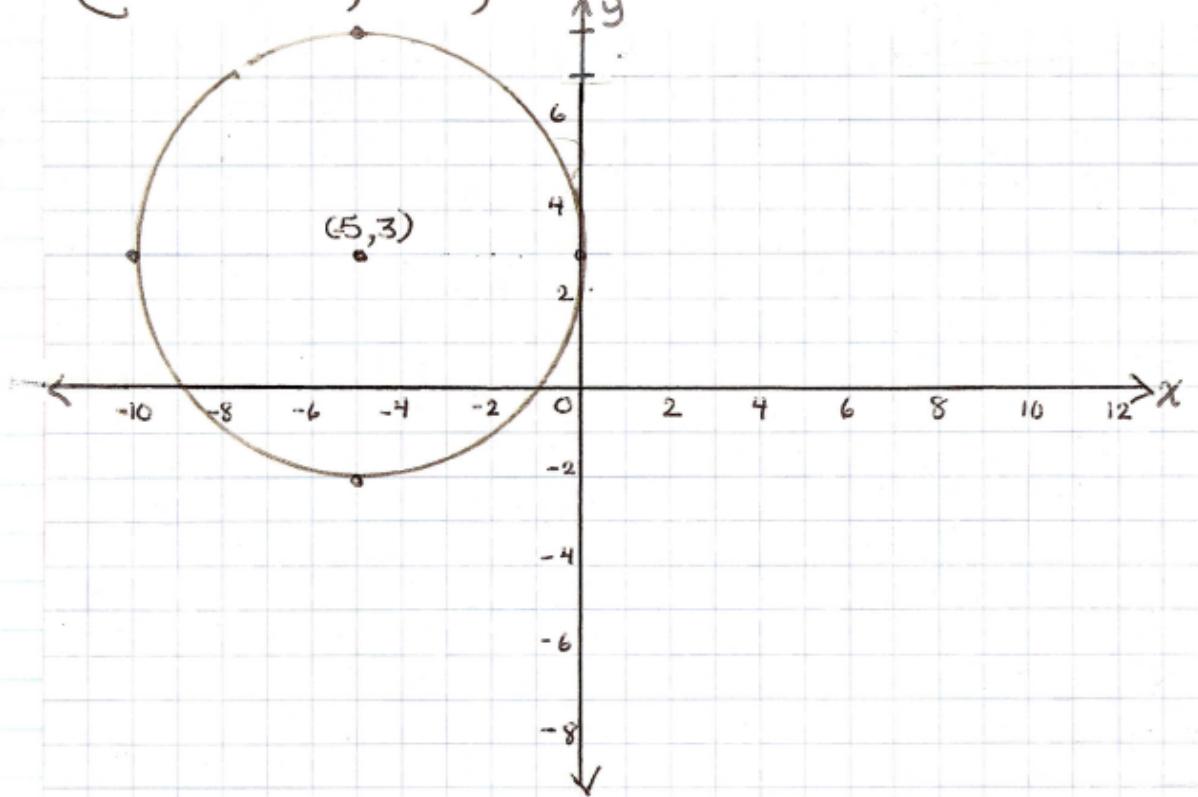
Center  $(-5, 3)$ ;  $r = \sqrt{25}$   
 $r = 5$  units.

3.

2(c) Center  $(2, 1)$ ;  $r = 2$  units.



2(h) Center  $(-5, 3)$  ;  $r = 5$  units



# Worksheet

# 1 - 12

