

SOLUTIONS \Rightarrow Point Estimate & Confidence Interval Questions

1. $n = 47$
 $\mu = 230$
 $\sigma = 23$
 $\bar{x} = 236$

a) $\bar{x} \pm z \frac{\sigma}{\sqrt{n}}$

$$236 \pm 1.645 \frac{23}{\sqrt{47}}$$

$$236 \pm 5.52$$

The 90% Confidence interval is between 230.48 and 241.52.

$$b) \bar{x} \pm z \frac{\sigma}{\sqrt{n}}$$

$$236 \pm 1.96 \frac{23}{\sqrt{47}}$$

$$236 \pm 6.58$$

The 95% confidence interval is between 229.42 and 242.58.

$$c) \bar{x} \pm z \frac{\sigma}{\sqrt{n}}$$

$$236 \pm 2.56 \frac{23}{\sqrt{47}}$$

$$236 \pm 8.59$$

The 99% confidence interval is between 227.41 and 244.59.

d) As the confidence level increases, the confidence interval gets wider.

e) The 90% confidence interval (230.48 to 241.52) does not enclose the population mean of 230.

In general, not all confidence intervals enclose the population mean.

$$\begin{aligned} 2. \quad \mu &= 168 \\ \sigma &= 15 \\ n &= 40 \end{aligned}$$

$$\begin{aligned} a) \quad \bar{x} &= \frac{6652}{40} \\ \bar{x} &= 166.3 \end{aligned}$$

b) The sample mean of 166.3 is considered a point estimate.

$$\begin{aligned} c) \quad \bar{x} \pm z \frac{\sigma}{\sqrt{n}} \\ 166.3 \pm 1.96 \frac{15}{\sqrt{40}} \\ 166.3 \pm 4.65 \end{aligned}$$

The 95% confidence interval is between 161.65 and 170.95.

d) The 95% confidence interval is an interval estimator.

- e) The 95% confidence interval (161.65 to 170.95) does enclose the population mean of 168.
- f) The method that produced this interval from 161.65 to 170.95 has a 0.95 probability of producing a confidence interval that encloses the population mean.

3. $n=72$
 $\bar{x}=232$
 $S_x=18$

$$\bar{x} \pm z \frac{S_x}{\sqrt{n}}$$

$$232 \pm 1.645 \frac{18}{\sqrt{72}}$$

$$232 \pm 3.49$$

The 90% confidence interval is between 228.51 and 235.49.

The method that produced this interval has a 0.90 probability of producing a confidence interval that encloses the population mean.

$$4. \quad n = 56$$

$$\bar{x} = 14.7$$

$$S_x = 1.3$$

$$\bar{x} \pm z \frac{S_x}{\sqrt{n}}$$

$$14.7 \pm 1.96 \frac{1.3}{\sqrt{56}}$$

$$14.7 \pm 0.34$$

The 95% confidence interval is between 14.36 and 15.04.

5. $n=60$
 $\bar{x}=6.1$
 $S_x=0.4$

$$\bar{x} \pm z \frac{S_x}{\sqrt{n}}$$

$$6.1 \pm 1.645 \frac{0.4}{\sqrt{60}}$$

$$6.1 \pm 0.09$$

The 90% confidence interval is between 6.02 and 6.19.

The method that produced the interval from 6.02 and 6.19 has a 0.90 probability of producing a confidence interval that encloses the population mean.

$$6. \begin{aligned} n &= 67 \\ \bar{x} &= 23.7 \\ S_x &= 3.2 \end{aligned}$$

$$\begin{aligned} \bar{x} \pm z \frac{S_x}{\sqrt{n}} \\ 23.7 \pm 2.56 \frac{3.2}{\sqrt{67}} \\ 23.7 \pm 1.00 \end{aligned}$$

The 99% confidence interval is between 22.7 and 24.7.