

Solutions to Exponential Growth Exercise 1.notebook

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Exercise 1

3. $\{(1,3), (2,6), (3,12), (4,24), \dots\}$

y-values: $3, 6, 12, 24$ x-values: increase by 1.
 $\times 2 \times 2 \times 2$

This is an exponential function with a common ratio of 2.

4. $\{(1,3), (3,15), (5,0.75), (7,0.375), \dots\}$

y-values: $3, 15, 0.75, 0.375$ x-values: increase by 2
 $\times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2}$

$* \frac{1}{2} = \frac{1}{2}$
 This is an exponential function with a common ratio of $\frac{1}{2}$. Since the x-values increase by 2.

7. $\{(2,8), (5,12), (8,18), (11,27), \dots\}$

y-values: $8, 12, 18, 27$
 $\times 1.5 \times 1.5 \times 1.5$

This is an exponential function with a common ratio of $\sqrt[3]{1.5}$ or $\frac{3}{2}$.

{ since the x-values increase by 3 }

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9. $\{(-1,40), (0,8), (1,1.6), (2,0.32), \dots\}$

y-values: $40, 8, 1.6, 0.32$ x-values: increase by 1.
 $\times 0.2 \times 0.2 \times 0.2$

This is an exponential function with a common ratio of 0.2.

10. $\{5, 15, 45, \frac{135}{x_3}, \frac{405}{x_3}, \frac{1215}{x_3}\}$ common ratio is 3

11. $\{-4, 16, -64, \frac{256}{x_4}, \frac{-1024}{x_4}, \frac{4096}{x_4}\}$ common ratio is -4

12. $\{\frac{5}{7}, \frac{5}{14}, \frac{5}{28}, \frac{5}{56}, \frac{5}{112}, \frac{5}{224}\}$ common ratio is $\frac{1}{2}$

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14. $y = 4^x$

common ratio = 4

15. $y = 1.8^x$

common ratio = 1.8

16. $y = 0.3^x$

common ratio = 0.3.

17. $y = 2700(0.6)^x$

common ratio = 0.6.

18. Joe borrows \$250 from Tom. Tom charges 2% interest per day.

* At the end of 1 day, he will owe 102%.

EQUATION:

$y = \text{initial amount} \cdot (\text{common ratio})^x$

$y = \$250(1.02)^x$

After 5 days: $y = \$250(1.02)^5$
 $= \$250(1.104080803)$
 $= \$276.02$

After 20 days: $y = \$250(1.02)^{20}$
 $= \$250(1.485947396)$
 $= \$371.49$

After 100 days: $y = \$250(1.02)^{100}$
 $= \$250(7.244646118)$
 $= \$1811.16$

This function is an example of exponential growth!

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19. Samantha buys a car for \$34000. The vehicle depreciates by 18% each year.

a) Time (x)

0	1	2	3	4
\$34000	\$19680	\$16137.60	\$132328.3	\$108509.2

b) Common Ratio = 0.82
 $(100\% - 18\% = 82\%)$

c) This function is an example of exponential decay.

d) EQUATION : $y = 34000(0.82)^x$

$\downarrow \quad \downarrow$
Initial Amount Common Ratio

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