

## **Applications of Sinusoidal Relations**

- Strategy: (1) Translate ALL key pieces of information from the problem.  
(2) Draw a sketch with ALL key points identified.  
(3) Develop an equation that models the problem.  
(4) Answer the question(s) being asked.

CHECK??? Do the numbers make sense?

## Applications of Sinusoidal Functions

A carnival Ferris wheel with a radius of 14 m makes one complete revolution every 16 seconds. The bottom of the wheel is 1.5 m above the ground. If a person is at the top of the wheel when a stop watch is started, determine how high above the ground that person will be after 1 minute and 7 seconds? Sketch one period of this function.

$$a = 14 \quad P = 16s$$

$$\text{min} = 1.5 \text{ m}$$

$$\text{sin axis: } 15.5 \text{ m}$$

$$b = \frac{360}{16} = 22.5$$

$$\begin{aligned} \text{max} &= \text{min} + \text{diameter} \\ &= 1.5 + 28 \\ &= 29.5 \text{ m} \end{aligned}$$

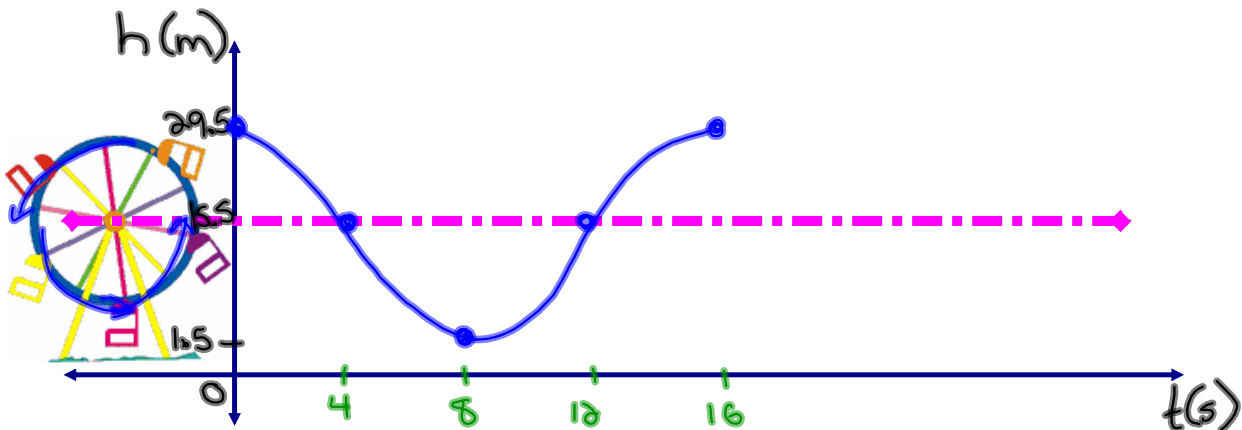
$$d = 15.5$$

$$\text{equation: } y = 14 \cos[22.5(x + 0)] + 15.5$$

$$y = 14 \cos[22.5(x)] + 15.5$$

$$y = 14 \cos[22.5(67)] + 15.5$$

$$y = 20.86 \text{ m}$$

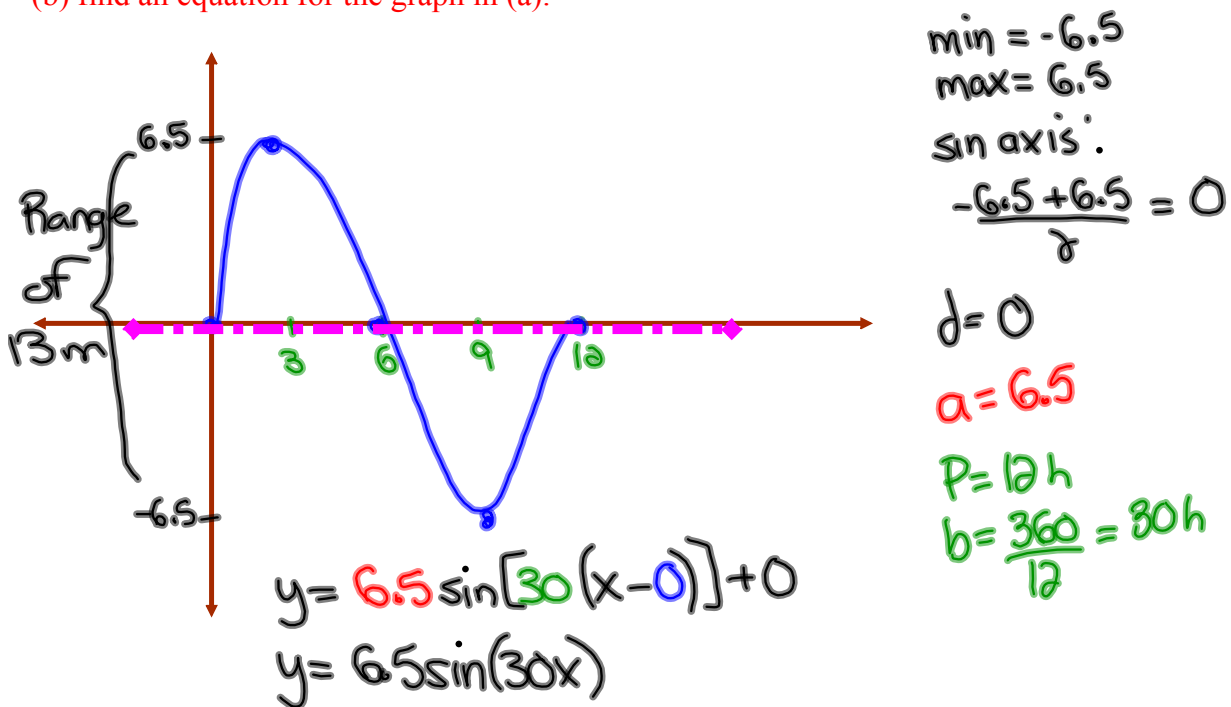


$$\frac{P}{4} = \frac{16}{4} = 4s$$

# Ocean Tides

The alternating half-daily cycles of the rise and fall of the ocean are called tides. Tides in one section of the Bay of Fundy caused the water level to rise 6.5m above mean sea-level and to drop 6.5m below. The tide completes one cycle every 12 h. Assuming the height of water with respect to mean sea-level to be modelled by a sine function,

- (a) draw the graph for a the motion of the tides for one complete day;  
 (b) find an equation for the graph in (a).



The alternating half-daily cycles of the rise and fall of the ocean are called tides. Tides in one section of the Bay of Fundy caused the water level to rise 6.5m above mean sea-level and to drop 6.5m below. The tide completes one cycle every 6 h. Assume the height of water with respect to mean sea-level to be modelled by a sinusoidal relationship. If it is high tide at 8:00 AM, determine where the water level would be at 1:47 PM.

# Solutions to Homework

**Applications of Sinusoidal Functions**

1. A Ferris wheel has a radius of 12m and makes one complete revolution every 12 seconds. The bottom of the wheel is 2m above the ground. *If a person gets on at the bottom and goes up*, determine the following:

a) Amplitude: = 12m    b) Period: 12s    c) b: -30    d) d: = 14m

e) Minimum Height: = 2m    f) Maximum Height: = 26m  $\Rightarrow (2+24)$   
min + diameter

g) Equation:  $y = -12\cos(30x) + 14$

h) Sketch the graph for two revolutions (periods):

i) How high is the person at these times?

i) 12 seconds  $\rightarrow y = -12\cos(30(12)) + 14 = 2\text{m}$

ii) 5 minutes  $\rightarrow y = -12\cos(30(300)) + 14 = 2\text{m}$

2. The tide on the Miramichi River has a range of 8m. At time 0 the tide is midway and at 4 hours the tide is low. The tide completes one full cycle in 16 hours.

a) Draw the graph for a 32 hour period.

b) Write the equation for this graph.

$a = 4$   
 $P = 16$   
 $b = \frac{360}{16} = 22.5$   
 $c = 0$   
 $d = 0$

$y = -4\sin(22.5x)$

# Solutions to Homework

3. A water wheel has a radius of 10m. 3m of the wheel is submerged under water. If the wheel makes one revolution in 360 degrees and the bucket starts at the center and goes up, find:

a) Amplitude: = 10m    b) Period: = 360°    c) b: = 1    d) d: = 7

e) Min Height: = -3m    f) Max Height: = 17m  $\rightarrow (-3 + 20)$   
min + diameter

g) Equation of Graph:  $y = 10\sin(x) + 7$

h) Sketch the graph for 2 revolutions:

i) How high will the bucket be after?

(i)  $40^\circ \rightarrow y = 10\sin(40^\circ) + 7 = 13.43\text{m}$

(ii)  $110^\circ \rightarrow y = 10\sin(110^\circ) + 7 = 16.4\text{m}$

(iii)  $200^\circ \rightarrow y = 10\sin(200^\circ) + 7 = 3.58\text{m}$

j) After how many degrees would the height be equal to 11? (Hint sub 11 in for y)

$11 = 10\sin(x) + 7$   
 $4 = 10\sin(x)$   
 $0.4 = \sin(x)$   
 $x = 22.58^\circ$      $\sin^{-1}(0.4) = x$

4. A water wheel is defined by the equation  $y = 7\cos[18(x)] + 4$     a = 7  
 Find:    b = 18  
 c = 0  
 d = 4

a) Amplitude = 7    b) Period =  $\frac{360}{18} = 20\text{s}$

c) Sketch the graph if the bucket starts at the top and goes down. Assume this function models the height of the bucket in meters over time in seconds.

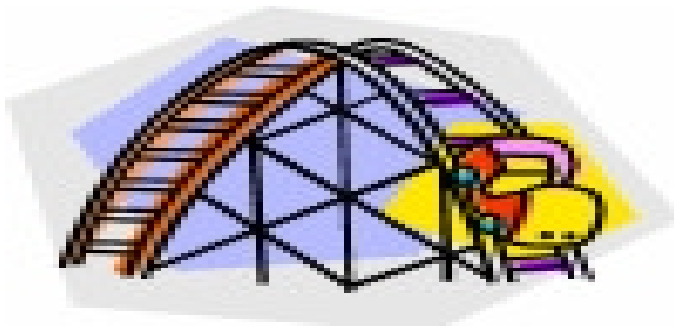
d) How much of the wheel is submerged? 3m (min = -3)

e) What is the Radius? = 7m  
↑  
 Amp.

f) When is the bucket 5m high?

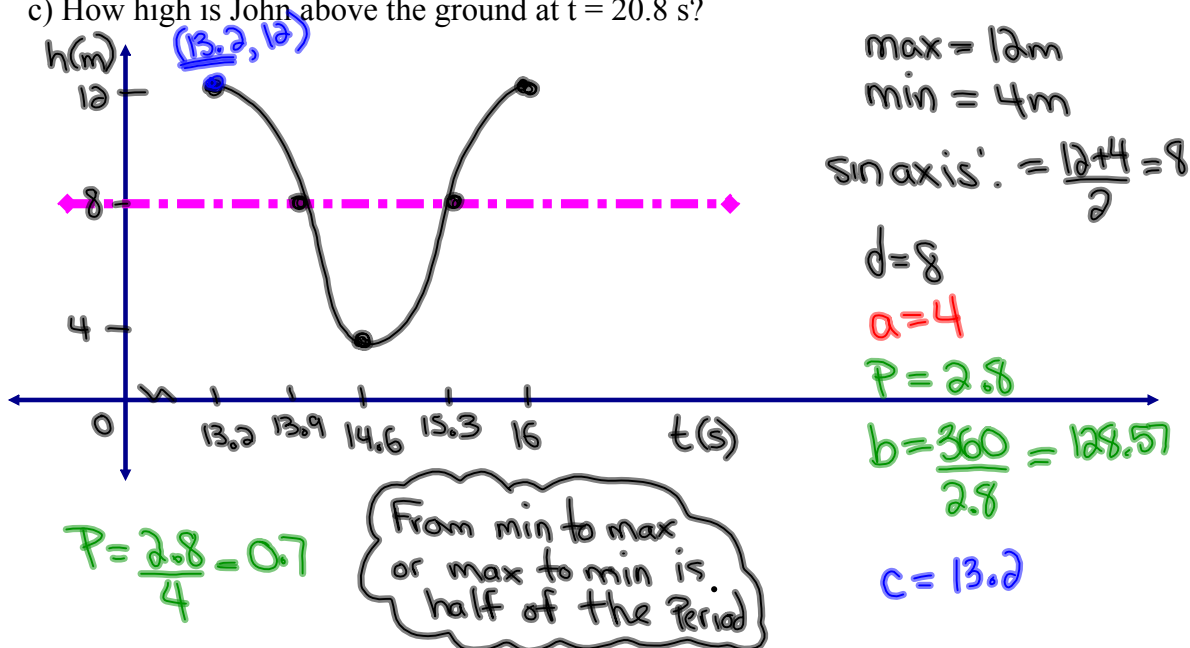
$5 = 7\cos(18x) + 4$   
 $1 = 7\cos(18x)$   
 $0.1428 = \cos(18x)$   
 $0.1428 = 18x$      $\cos^{-1}(0.1428) = 18x$   
 $4.57\text{s} = x$

# Roller Coaster



John climbs on a roller coaster at Six Flags Amusement Park. An observer starts a stopwatch and observes that John is at a maximum height of 12 m at  $t = 13.2$  s. At  $t = 14.6$  s, John reaches a minimum height of 4 m.

- Sketch a graph of the function.
- Find an equation that expresses John's height in terms of time.
- How high is John above the ground at  $t = 20.8$  s?



$$b) \quad y = 4 \cos[128.57(x - 13.2)] + 8$$

$$c) \quad y = 4 \cos[128.57(20.8 - 13.2)] + 8$$

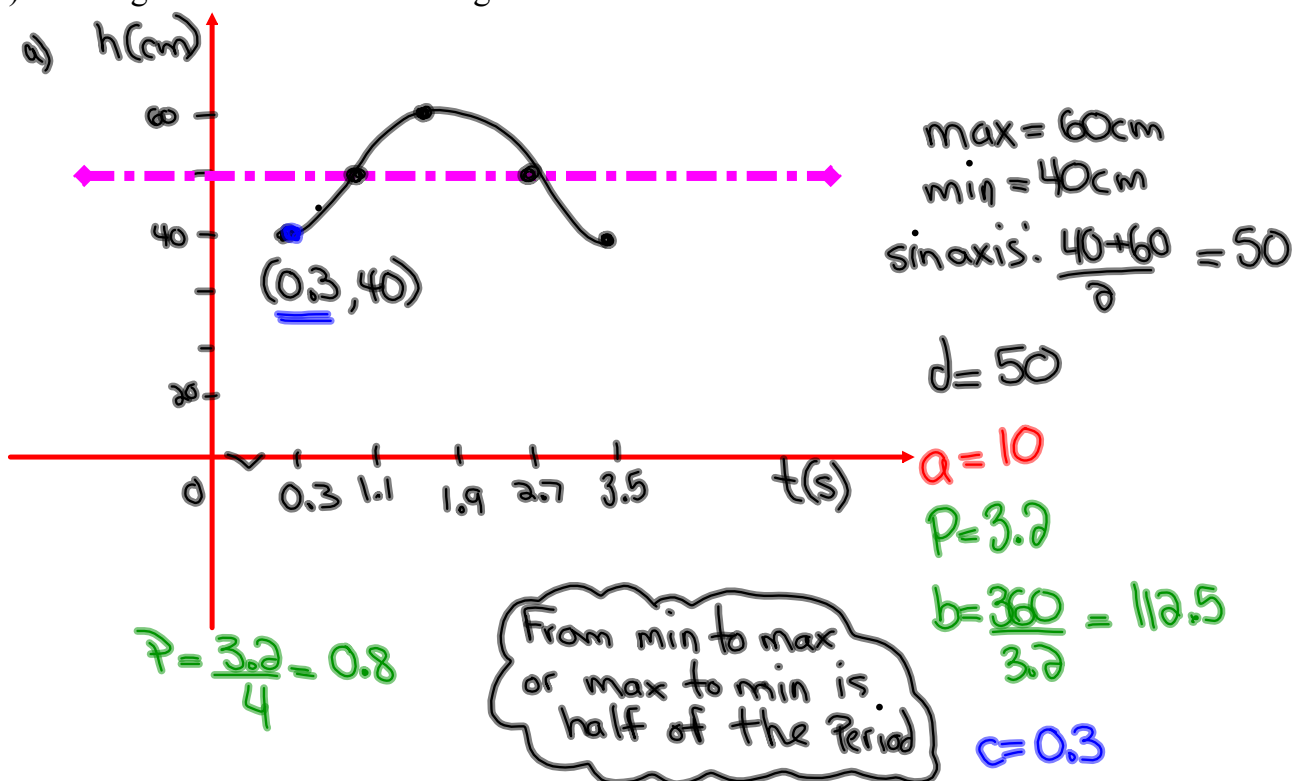
$$y = 4 \cos[128.57(7.6)] + 8$$

$$y = 7.1m$$

# Spring Problem

A weight attached to a long spring is being bounced up and down by an electric motor. As it bounces, its distance from the floor varies periodically with time. When the stopwatch reads 0.3 seconds, the weight reaches its first low point 40 cm above the ground. The next high point, 60 cm above the ground, occurs at 1.9 seconds.

- Sketch a graph of the function.
- Write an equation expressing the distance above the ground in terms of the numbers of seconds the stopwatch reads.
- How high is the mass above the ground after 17.2 seconds?



$$b) \quad y = -10 \cos [112.5(x - 0.3)] + 50$$

$$c) \quad y = -10 \cos [112.5(17.2 - 0.3)] + 50$$

$$y = -10 \cos [112.5(16.9)] + 50$$

$$y = 52 \text{ cm}$$

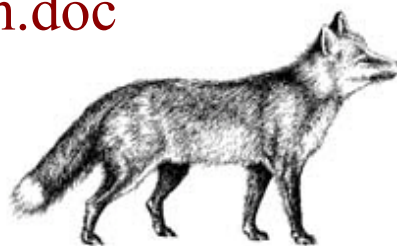
# Biology!

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Naturalists find that the populations of some animals varies periodically with time. Records started being taken at  $t = 0$  years. A minimum number, 200 foxes, occurred when  $t = 2.9$  years. The next maximum, 800 foxes, occurred at  $t = 5.1$  years.

**Give two different times at which the fox population is 625.**

**Bonus Soln - Fox Population.doc**





Let's look at the detailed solutions...

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 [Worksheet Solns - Applications of Sinusoidal Relations.doc](#)

## Attachments

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Worksheet - Finding the Equation.doc

Worksheet - Sketching Trigonometric Functions.doc

Worksheet Solns - Sketching Sinusoidal Relations.doc

Worksheet - Sketching Sinusoidal relations (sept06).pdf

Bonus Soln - Fox Population.doc

Worksheet Solns - Applications of Sinusoidal Relations.doc

Review - Practice Test for Sinusoidal Functions.doc

Review - Trigonometric Functions(3)(4).doc

Sketching Sinusoidal Functions #2.pdf

Sketching Sinusoidal Functions #2.doc

Sketching Sinusoidal Functions #3 (Solutions).doc

worksheet-sketching in radian measure.doc