

## Curve Sketching

Intercepts:

To find the  $x$ -intercept of  $y = f(x)$ , set  $y = 0$  and solve for  $x$ .

To find the  $y$ -intercept of  $y = f(x)$ , set  $x = 0$ ; the  $y$ -intercept is  $f(0)$ .

Example:

$$y = \frac{x^2 - x - 6}{x + 1}$$

$x$ -intercept ( $y=0$ )

$$\frac{0}{1} = \frac{x^2 - x - 6}{x + 1}$$

$$\underline{1}x^2 + x - \underline{6} = 0 \quad \text{Factor: } \begin{array}{l} \underline{2}x - \underline{3} = -6 \\ \underline{2} + \underline{-3} = -1 \end{array}$$

$$(x^2 + 2x)(-3x - 6) = 0$$

$$x(x+2) - 3(x+2) = 0$$

$$(x-3)(x+2) = 0$$

$$x-3=0 \quad | \quad x+2=0$$

$$x=3 \quad | \quad x=-2$$

$$(3,0) \quad | \quad (-2,0)$$

$y$  intercept ( $x=0$ )

$$y = \frac{(0)^2 - (0) - 6}{(0) + 1} = \frac{-6}{1} = -6$$

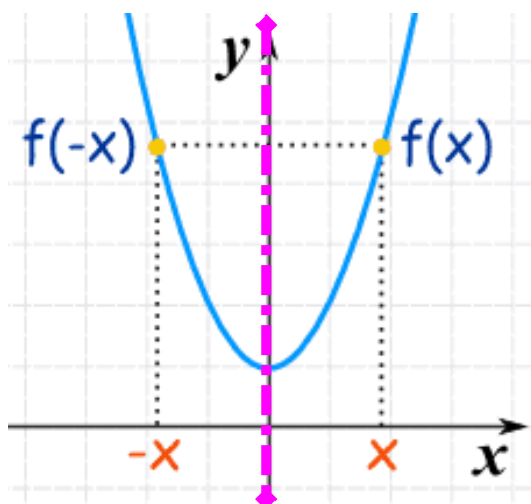
$$(0, -6)$$

## Symmetry:

An **even function** satisfies

$$f(-x) = f(x)$$

for all  $x$  in its domain. Thus, a function is even if it is unchanged when  $x$  is replaced by  $-x$ . The graph of an even function is symmetric about the  $y$ -axis.



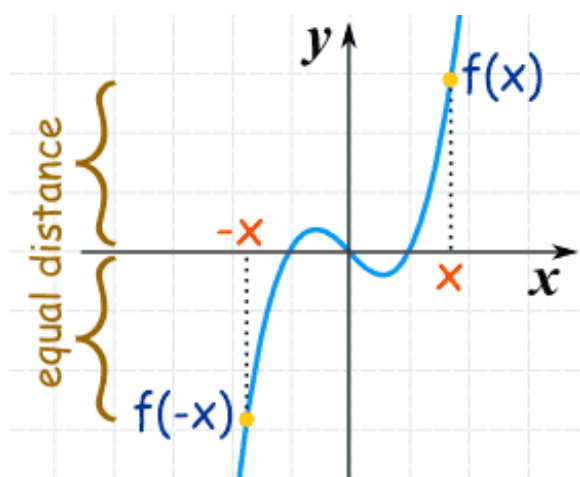
$$f(1.75) = 4.5$$

$$f(-1.75) = 4.5$$

An **odd function** satisfies

$$f(-x) = -f(x)$$

for all  $x$  in its domain. The graph of an odd function is symmetric about the **origin**.



$$f(1.75) = 3$$

$$f(-1.75) = -3$$

Symmetry is used to reduce the amount of work in graphing. If we have graphed an *even function* for  $x \geq 0$ , we just reflect in the  $y$ -axis to get the entire graph. For an *odd function* we just rotate through 180 degrees about the origin.

### Example:

Determine whether each function is even, odd, or neither

a)  $f(x) = \underline{\underline{x^6}}$

$$f(-x) = (-x)^6$$

$$f(-x) = \underline{\underline{x^6}}$$

Since:  $f(-x) = f(x)$

Even

b)  $g(x) = \underline{\underline{x^3 + \frac{1}{x}}}$

$$g(-x) = (-x)^3 + \frac{1}{(-x)}$$

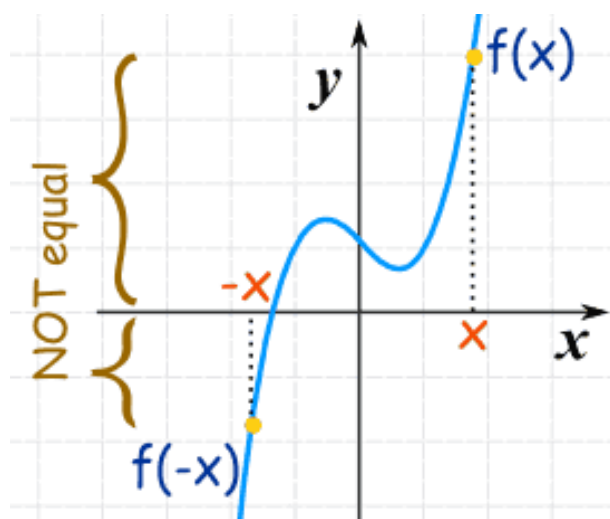
$$g(-x) = -x^3 - \frac{1}{x}$$

$$g(-x) = -\left(x^3 + \frac{1}{x}\right)$$

Since:  $g(-x) = -g(x)$

Odd

Is this function Even or Odd? (Neither)

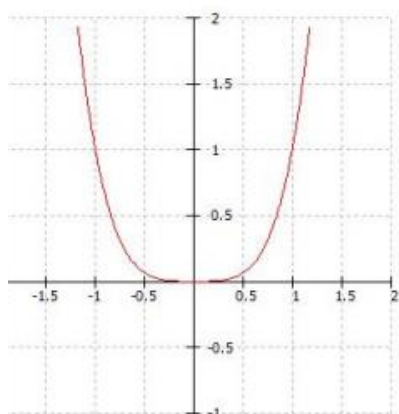


$$f(1.75) = 4$$

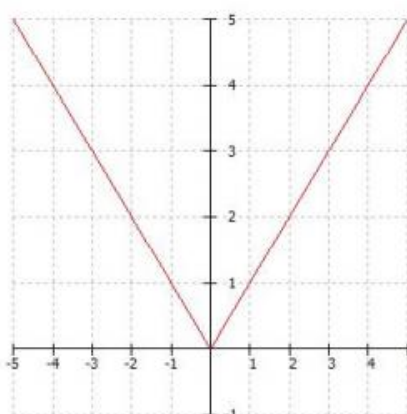
$$f(-1.75) = -1.75$$

# Homework

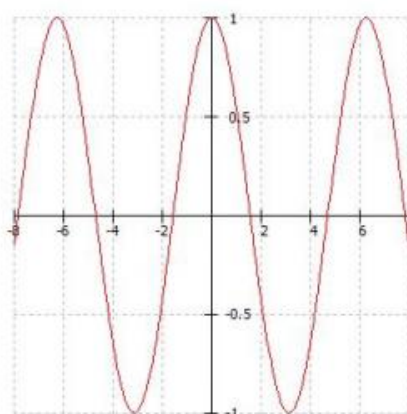
**Even Functions**



$f(x) = x^4$



$g(x) = |x|$



$h(x) = \cos x$