

Arithmetic
(common difference "d")

$$t_n = a + (n - 1)d$$

$$S_n = \frac{n}{2}(2a + (n - 1)d)$$

$$S_n = \frac{n}{2}(a + t_n)$$

Geometric
(Common Ratio "r")

$$t_n = ar^{n-1}$$

$$S_n = \frac{a(r^n - 1)}{r - 1}$$

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$$S_n = \frac{a}{1 - r}$$

$$-1 < r < 1$$

Ex 1.7

$$\textcircled{1} \text{ b) } 1 - \frac{2}{3} + \frac{4}{9} - \frac{8}{27} + \dots$$

$$a = 1$$

$$r = \frac{-2}{3}$$

$$S_{\infty} = \frac{a}{1-r}$$

$$= \frac{1}{1 - \left(\frac{-2}{3}\right)} \rightarrow 1 + \frac{2}{3}$$

$$= \frac{1}{\frac{5}{3}} \leftarrow \frac{3}{3} + \frac{2}{3}$$

$$= 1 \times \frac{3}{5}$$

$$= \boxed{\frac{3}{5}}$$

$$\text{c) } \left(\frac{1}{4}\right) - \frac{5}{16} + \frac{25}{64} - \frac{125}{256} + \dots$$

$$a = \frac{1}{4}$$

Divergent (r is too small)

$$r = \frac{-5}{4}$$

$$\textcircled{2} \text{ b) } \sum_{n=1}^{\infty} \left(\frac{-2}{5}\right)^n = \left(\frac{-2}{5}\right) + \frac{4}{25} - \frac{8}{125} + \frac{16}{625} - \dots$$

$$a = \frac{-2}{5}$$

$$r = \frac{4}{25} \div \frac{-2}{5}$$

$$= \frac{4}{25} \times \frac{5}{-2}$$

$$= \frac{-2}{5}$$

$$S_n = \frac{\frac{-2}{5}}{1 - \left(\frac{-2}{5}\right)}$$

$$= \frac{\frac{-2}{5}}{\frac{7}{5}}$$

$$= \frac{-2}{5} \times \frac{5}{7}$$

$$= \boxed{\frac{-2}{7}}$$

Series and Sequence Review

① $t_{12} = 15$

$$t_n = a + (n-1)d$$

$$t_{12} = a + (12-1)d$$

$$t_{12} = a + 11d$$

$$a + 11d = 15$$

$$S_{15} = 105$$

$$S_n = \frac{n}{2}(2a + (n-1)d)$$

$$S_{15} = \frac{15}{2}(2a + (15-1)d)$$

$$S_{15} = 7.5(2a + 14d)$$

$$S_{15} = 15a + 105d$$

$$15a + 105d = 105$$

Elimination Method:

$$\begin{array}{r} a + 11d = 15 \\ \ominus) a + 7d = 7 \\ \hline 4d = 8 \end{array}$$

$$d = 2$$

$$a + 7d = 7$$

$$-7 \quad -5 \quad -3$$

$$a + 7(2) = 7$$

$$a + 14 = 7$$

$$a = -7$$