

# Warm Up

Prove the following identities:

$$\frac{1}{\cot x} = \sin x \sec x$$

$\tan x$

$$\frac{\sin x}{\cos x}$$

$$\sin x \left( \frac{1}{\cos x} \right)$$

$$\frac{\sin x}{\cos x}$$

$$1 - \cos^2 \theta = \frac{\cos \theta \sin \theta}{\cot \theta}$$

$\sin^2 \theta$

$\sin^2 \theta$

$$\frac{\cos \theta \sin \theta}{\frac{\cos \theta}{\sin \theta}}$$

$$\cancel{\cos \theta} \sin \theta \cdot \frac{\sin \theta}{\cancel{\cos \theta}}$$

$\sin^2 \theta$

Questions from last night's homework?

$$\tan \theta \cos \theta = \sin \theta$$

$$\cot \theta \sec \theta = \csc \theta$$

$$\frac{1 + \cot^2 \theta}{\csc^2 \theta} = 1$$

$$\frac{\tan^2 \theta}{1 + \tan^2 \theta} = \sin^2 \theta$$

$$\frac{\tan^2 \theta}{\sin^2 \theta} = 1 + \tan^2 \theta$$

Questions from last night's homework?

$$\textcircled{2} \quad \boxed{\cot\theta} \boxed{\sec\theta} = \boxed{\csc\theta}$$

$$\frac{\cancel{\cos\theta}}{\sin\theta} \left( \frac{1}{\cancel{\cos\theta}} \right) = \frac{1}{\sin\theta}$$

$$\boxed{\frac{1}{\sin\theta}}$$

$$\textcircled{3} \quad \frac{\boxed{1 + \cot^2\theta}}{\csc^2\theta} = \boxed{1}$$

$$\frac{\csc^2\theta}{\csc^2\theta} = \boxed{1}$$

$$\textcircled{4} \quad \frac{\tan^2\theta}{\boxed{1 + \tan^2\theta}} = \boxed{\sin^2\theta}$$

$$\frac{\boxed{\tan^2\theta}}{\csc^2\theta}$$

$$\frac{\sin^2\theta}{\cos^2\theta} \div \frac{1}{\cos^2\theta}$$

$$\frac{\sin^2\theta}{\cancel{\cos^2\theta}} \times \frac{\cancel{\cos^2\theta}}{1}$$

$$\boxed{\sin^2\theta}$$

$$\textcircled{5} \quad \frac{\boxed{\tan^2\theta}}{\sin^2\theta} = \boxed{1 + \tan^2\theta}$$

$$\frac{\sin^2\theta}{\cos^2\theta} \times \frac{1}{\sin^2\theta}$$

$$\frac{1}{\cos^2\theta}$$

$$\sec^2\theta$$

$$\boxed{1 + \tan^2\theta}$$

## Trig Identities

$\tan \theta = \frac{\sin \theta}{\cos \theta}$ $\cot \theta = \frac{\cos \theta}{\sin \theta}$	$\sin^2 \theta + \cos^2 \theta = 1$ $\tan^2 \theta + 1 = \sec^2 \theta$ $1 + \cot^2 \theta = \csc^2 \theta$
$\csc \theta = \frac{1}{\sin \theta}$ $\sec \theta = \frac{1}{\cos \theta}$ $\cot \theta = \frac{1}{\tan \theta}$	$\sin \theta = \frac{1}{\csc \theta}$ $\cos \theta = \frac{1}{\sec \theta}$ $\tan \theta = \frac{1}{\cot \theta}$

**Strategies for Proving Identities:**

- Work on the most complex side and simplify so it has the same form as the simpler side
- Methods used in simplifying: direct substitution, factoring, finding a common denominator, multiplying by the conjugate

**Prove the following identities:**

$$\frac{1}{\sin^2 x} + \frac{1}{\cos^2 x} = \frac{1}{\sin^2 x \cos^2 x}$$

pythagorean  
→

$$\frac{\cos^2 x + \sin^2 x}{\sin^2 x \cos^2 x}$$
$$\frac{1}{\sin^2 x \cos^2 x}$$

$$\frac{\csc \theta}{\cot^2 \theta} = \tan \theta \sec \theta$$

# Homework