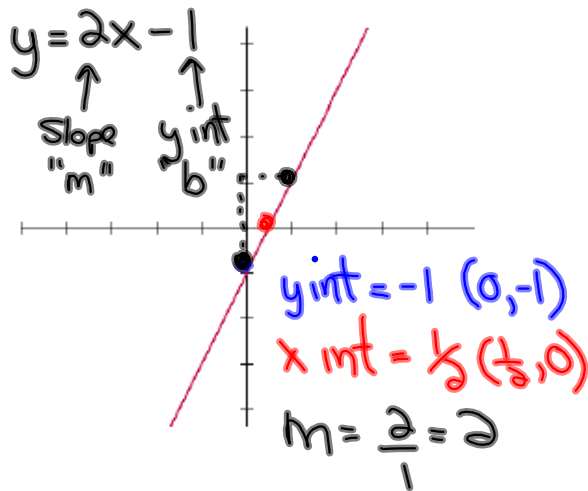


Catalog of Essential Functions

1. Linear



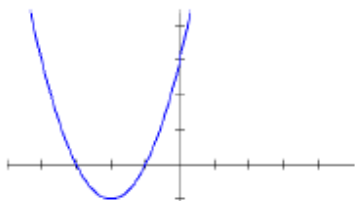
Straight Line

Equation will be degree one

Should be able to identify the **slope, intercepts, and equation** from the graph

$$y = x$$

2. Quadratic



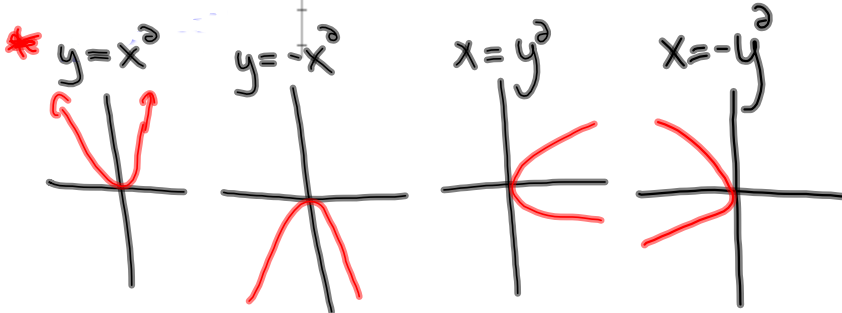
Parabola (U-Shaped)

Either y or x will be squared (not both!)

*

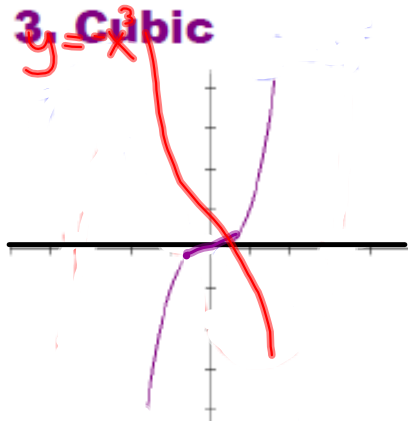
Should know the 4 basic quadratic functions

Should be able to apply transformations to the basic quadratic functions



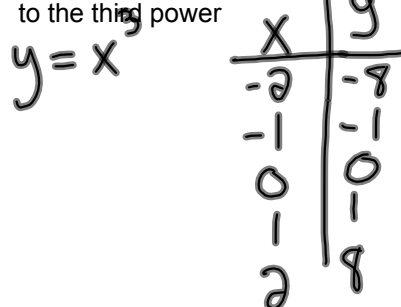
$y = x^2$	
x	y
-2	4
-1	1
0	0
1	1
2	4

3. Cubic



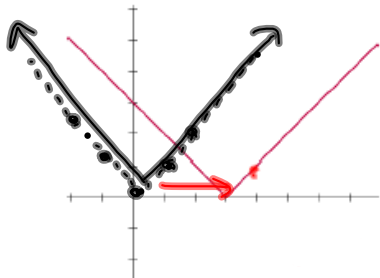
S-Shaped

We will work with functions that are raised to the third power



Catalog of Essential Functions

4. Absolute Value



V-Shaped

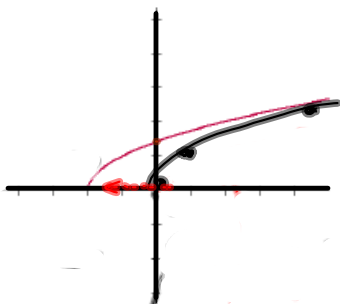
Equation will have a variable within the absolute value bars

Should be able to apply transformations to the basic absolute value function

$y = |x|$

x	y
-2	2
-1	1
0	0
1	1
2	2

5. Square Root



Half Parabola

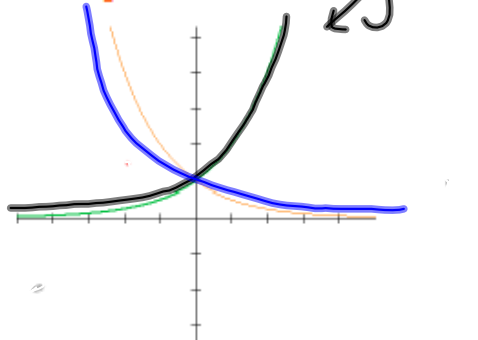
Equation will have a variable under the square root sign

Should be able to apply transformations to the basic square root function

$y = \sqrt{x}$

x	y
0	0
4	2
9	3

6. Exponential



Steadily increasing or decreasing

Base will be a number and variable will appear in the exponent ex: $y = 2^x$

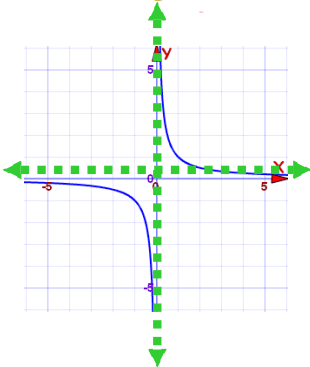
Should be able to identify the **horizontal asymptote**

$y = 2^x$

x	y
-2	1/4
-1	1/2
0	1
1	2
2	4

Catalog of Essential Functions

7. Reciprocal



Will have two branches

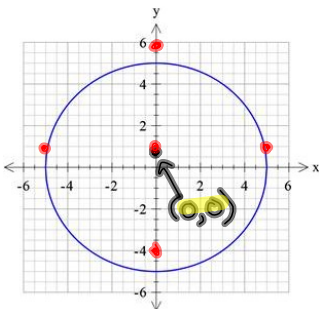
Equation will have a variable within the denominator of a rational expression

Should be able to identify the vertical and horizontal asymptotes

$$y = \frac{1}{x}$$

x	y
-2	-1/2
-1	-1
0	undefined
1	1
2	1/2

8. Circle



• General form: $(x - h)^2 + (y - k)^2 = r^2$

* center: (h, k) $(0, 0)$
 * radius = r 5

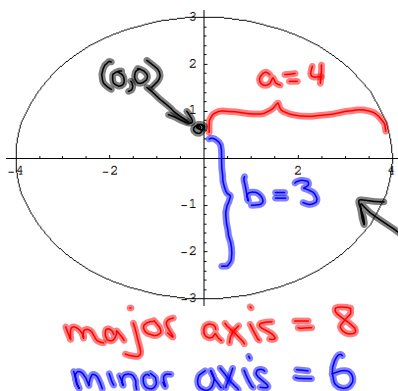
• Be able to identify the function that would describe either just the top or bottom of the circle.

$$x^2 + y^2 = r^2$$

$$x^2 + y^2 = 5^2$$

$$x^2 + y^2 = 25$$

9. Ellipse



• General form: $\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1$

Where ...

- Center: (h, k)
- $a > b$
- If a is the denominator of the "y" term the ellipse will have a vertical major axis.

$$\frac{(x-0)^2}{4^2} + \frac{(y-0)^2}{3^2} = 1$$

$$\frac{x^2}{16} + \frac{y^2}{9} = 1$$

Transformations:

New Functions From Old Functions

- ① ✓ Translations (Slide transformations)
- ② Stretches
- ③ Reflections

Translations

* h = horizontal translation (shift left or right)
 Focus on... k = vertical translation (shift up or down)

- determining the effects of h and k in $y - k = f(x - h)$ on the graph of $y = f(x)$ or $y = f(x - h) + k$
- sketching the graph of $y - k = f(x - h)$ for given values of h and k , given the graph of $y = f(x)$
- writing the equation of a function whose graph is a vertical and/or horizontal translation of the graph of $y = f(x)$

base: $y = x^2$

Ex: ① $y = (x - 3)^2 + 2$
 $h = 3$ right 3
 $k = 2$ up 2

base: $y = |x|$

② $y - 4 = |x + 3|$
 $y = |x + 3| + 4$
 $h = -3$ left 3
 $k = 4$ up 4

function notation:

③ $g(x) = f(x + 2) - 1$
 $h = -2$ left 2
 $k = -1$ down 1

Translation

- To *translate* or *shift* a graph is to move it up, down, left, or right without changing its shape.
- Translation is summarized by the following table and illustration:

Vertical and Horizontal Shifts Suppose $c > 0$. To obtain the graph of

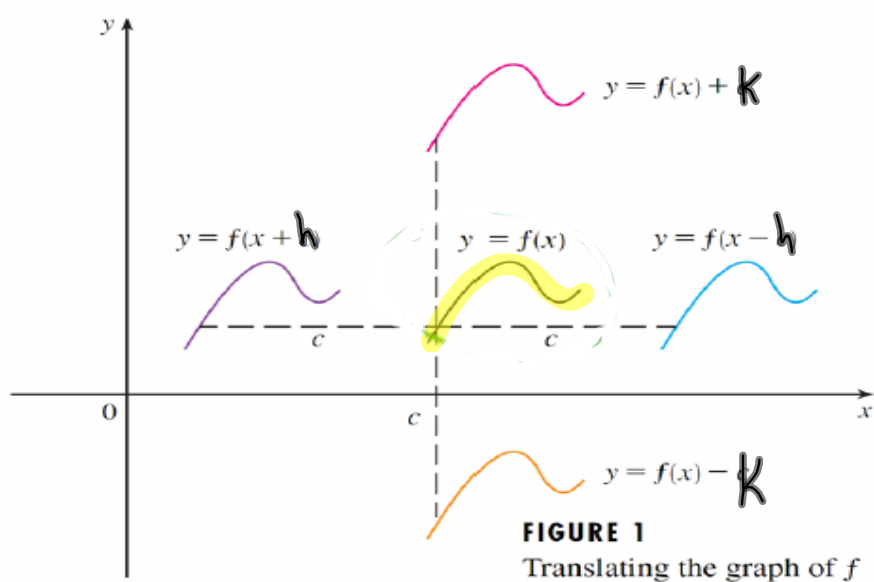
$y = f(x) + k$ shift the graph of $y = f(x)$ a distance k units upward

$y = f(x) - k$ shift the graph of $y = f(x)$ a distance k units downward

$y = f(x - h)$, shift the graph of $y = f(x)$ a distance h units to the right

$y = f(x + h)$, shift the graph of $y = f(x)$ a distance h units to the left

Translations illustrated...



Using Mapping Notation to Describe Transformations:

*Think of this as a set of instructions to follow to transform a graph.

base: $y = x^2$

x	$y = x^2$
-3	9
-2	4
-1	1
0	0
1	1
2	4
3	9

$k=2 \rightarrow$ up 2

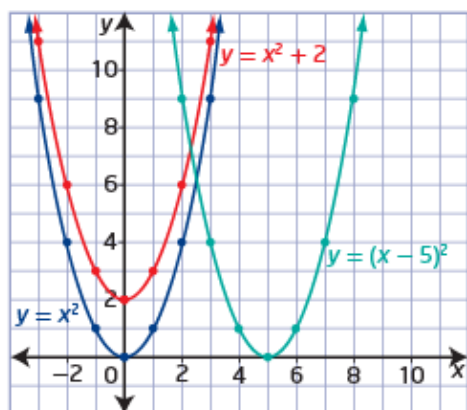
x	$y = x^2 + 2$
-3	11
-2	6
-1	3
0	2
1	3
2	6
3	11

$h=5 \rightarrow$ right 5

x	$y = (x - 5)^2$
2	9
3	4
4	1
5	0
6	1
7	4
8	9

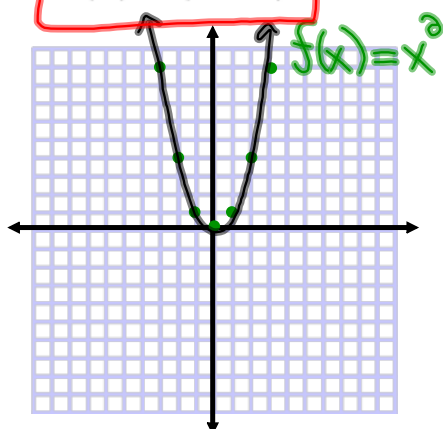
$$(x, y) \rightarrow (x, y + k)$$

$$(x, y) \rightarrow (x + h, y)$$

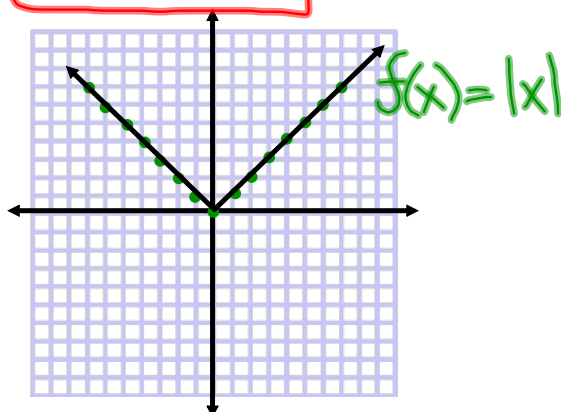
Graph Translations of the Form $y - k = f(x)$ and $y = f(x - h)$ 

Identify the translations for each of the following...
and then sketch the transformed curve

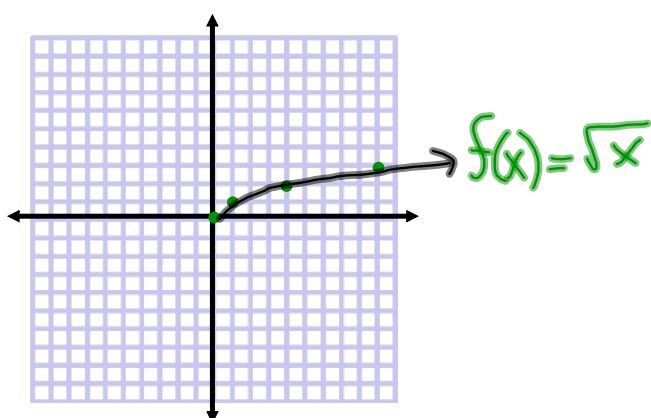
$$f(x) = (x+7)^2$$



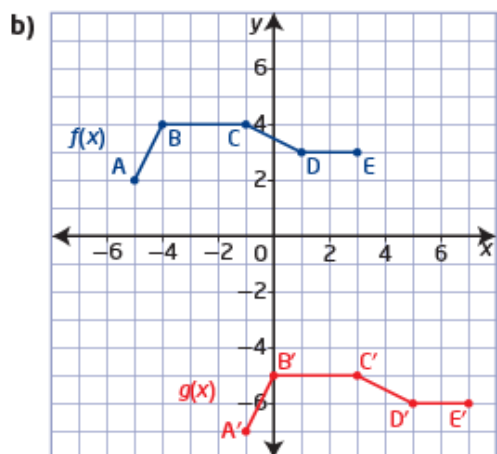
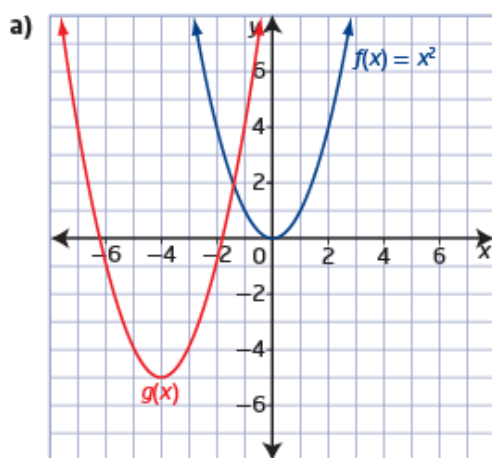
$$f(x) = |x| + 3$$



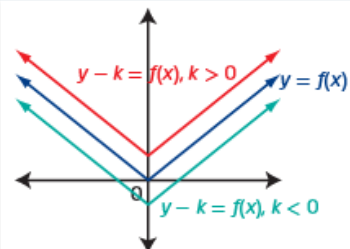
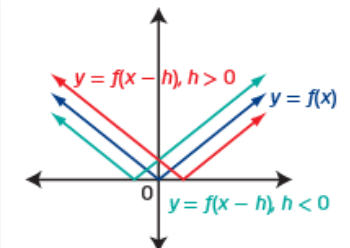
$$f(x) = \sqrt{x-3} - 2$$



Determine the Equation of a Translated Function:



- Translations are transformations that shift all points on the graph of a function up, down, left, and right without changing the shape or orientation of the graph.
- The table summarizes translations of the function $y = f(x)$.

Function	Transformation from $y = f(x)$	Mapping	Example
$y - k = f(x)$ or $y = f(x) + k$	A vertical translation If $k > 0$, the translation is up. If $k < 0$, the translation is down.	$(x, y) \rightarrow (x, y + k)$	
$y = f(x - h)$	A horizontal translation If $h > 0$, the translation is to the right. If $h < 0$, the translation is to the left.	$(x, y) \rightarrow (x + h, y)$	

- A sketch of the graph of $y - k = f(x - h)$, or $y = f(x - h) + k$, can be created by translating key points on the graph of the base function $y = f(x)$.

Homework

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