

Ex. A Ferris Wheel rotates 3 times each minute. The passengers sit in seats that are 5 m from the center of the wheel. What is the angular velocity of the wheel in radians per second? What distance do the passengers travel in 6.5 seconds?

$$a) \quad \omega = \frac{\theta}{t} = \frac{6\pi \text{ rads}}{1 \text{ min}} = \frac{6\pi \text{ rads}}{60 \text{ sec}} = 0.314 \text{ rads/sec} .$$

$$b) \quad (i) \quad \theta = (\omega)(t) \quad (ii) \quad a = \theta r$$

$$\theta = (0.314)(6.5) \quad a = (2.04)(5 \text{ m})$$

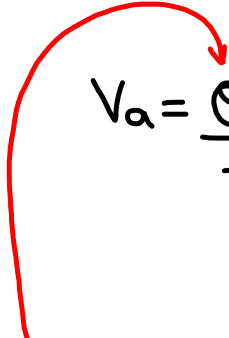
$$\theta = 2.04 \text{ rads} \quad a = 10.2 \text{ m}$$

Ex. A bicycle wheel has a radius of 36 cm and is turning at 4.8m/s. Determine the angular velocity of this wheel?

$$r = 36\text{cm} = 0.36\text{m}$$

$$a = 4.8\text{m (after 1sec)}$$

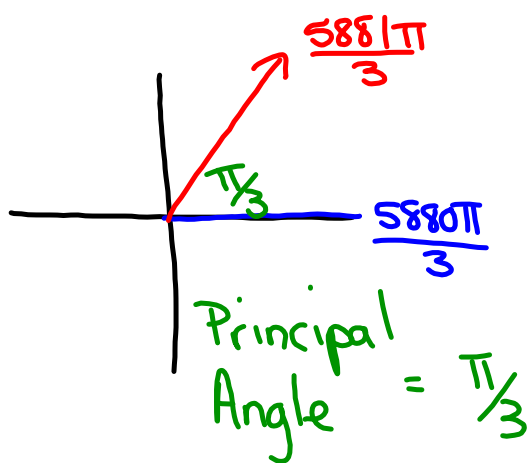
$$\Theta = \frac{a}{r} = \frac{4.8\text{m}}{0.36\text{m}} = \underline{13.\bar{3}\text{rads}}$$

$$v_a = \frac{\Theta}{t} = \frac{13.\bar{3}\text{rads}}{1\text{sec}}$$


Sketch the following and determine a negative angle co-terminal with:

$$(i) \frac{5881\pi}{3} \rightarrow \frac{5880\pi}{3}, \frac{5881\pi}{3}, \frac{5882\pi}{3}$$

$1960\pi$



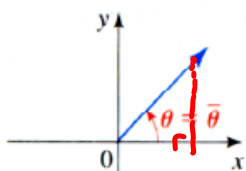
$$\begin{aligned} A_c &= \frac{\pi}{3} - \frac{2\pi}{1} \\ &= \frac{\pi}{3} - \frac{6\pi}{3} \\ &= -\frac{5\pi}{3} \end{aligned}$$

## Reference Triangles:

**Definition 17** The reference angle  $\bar{\theta}$  of an angle  $\theta$  in standard position is the acute angle (between 0 and  $90^\circ$ ) the terminal side makes with the x-axis.

$0$  and  $\frac{\pi}{2}$

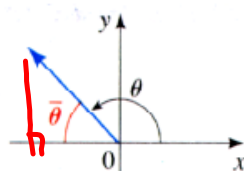
The picture below illustrates this concept.



$$\theta = 45^\circ$$

$$\bar{\theta} = 45^\circ - 0^\circ$$

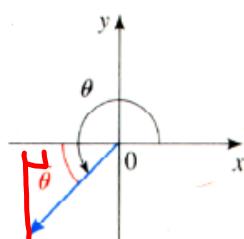
$$\bar{\theta} = 45^\circ$$



$$\theta = 135^\circ$$

$$\bar{\theta} = 180^\circ - 135^\circ$$

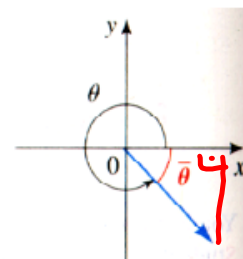
$$\bar{\theta} = 45^\circ$$



$$\theta = 232^\circ$$

$$\bar{\theta} = 232^\circ - 180^\circ$$

$$\bar{\theta} = 52^\circ$$



$$\theta = 320^\circ$$

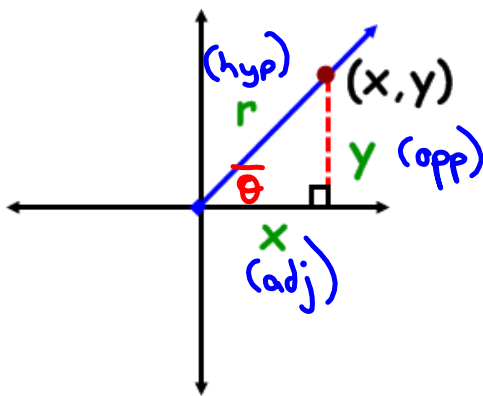
$$\bar{\theta} = 360^\circ - 320^\circ$$

$$\bar{\theta} = 40^\circ$$

What is the significance of reference angles?

## Angles on the Cartesian Plane

- **Reference Angle** - an acute angle formed between the terminal arm and the x-axis.
- **Reference Triangle** - a triangle formed by drawing a perpendicular line from a point on the terminal to the x-axis.



Notice what will happen if the rotation moves into other quadrants?

### TRIG RATIOS on the CARTESIAN PLANE

$$\sin \theta = \frac{y}{r} \qquad \csc \theta = \frac{r}{y}$$

$$\cos \theta = \frac{x}{r} \qquad \sec \theta = \frac{r}{x}$$

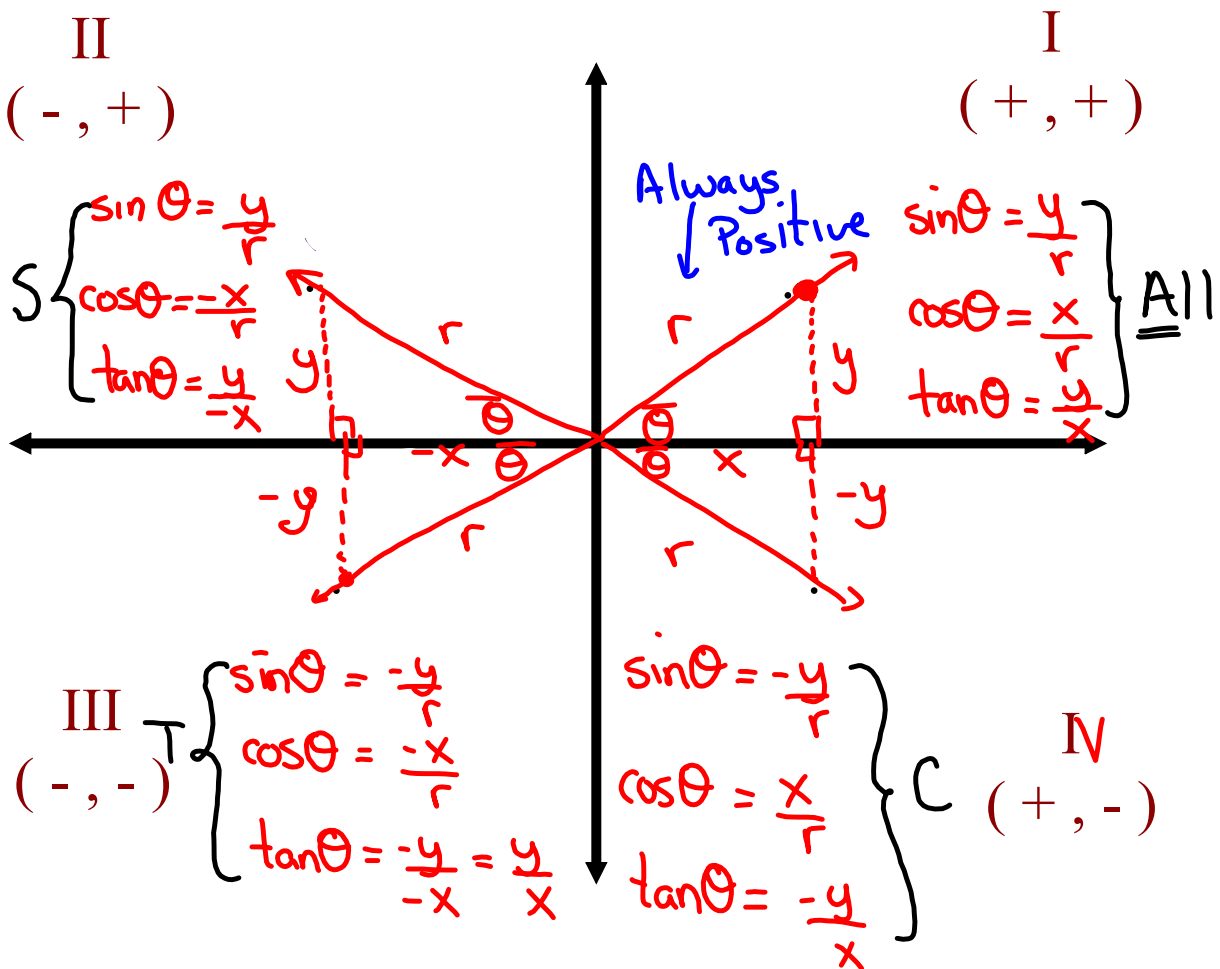
$$\tan \theta = \frac{y}{x} \qquad \cot \theta = \frac{x}{y}$$

**"Primary"**

**"Reciprocal"**

# TRIG RATIOS IN ALL 4 QUADRANTS

What primary trig ratios are **POSITIVE** in...



4CAST

## Homework



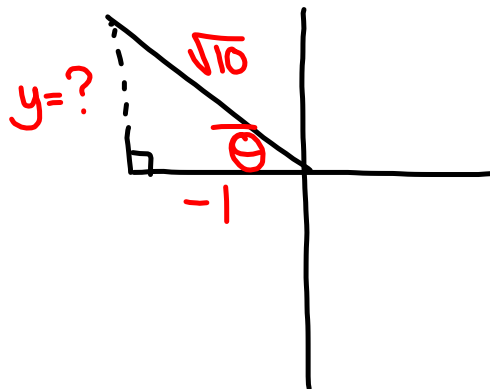
(sine is positive)

If  $\sec \theta = -\sqrt{10}$  and  $\sin \theta > 0$ , determine the value of  $\csc \theta$

$$\sec \theta = \frac{r}{x}$$

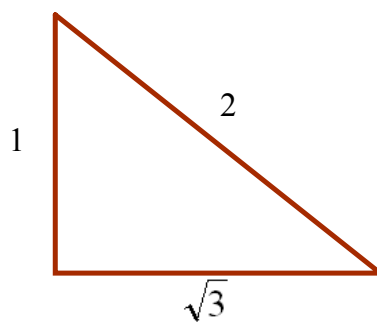
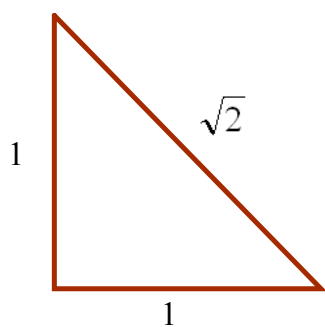
$$r = \sqrt{10}$$

$$x = -1$$

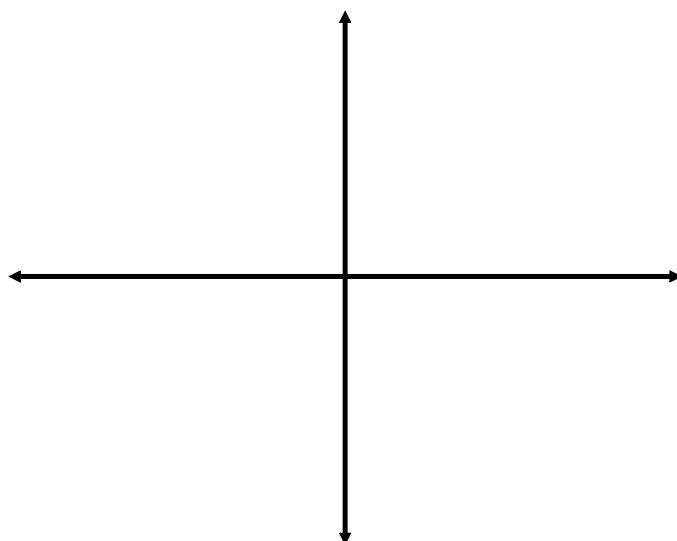


Determine the measure (in radians) of an angle whose terminal arm passes through the ordered pair  $(-2\sqrt{3}, -4)$

## Special Angles (in radians)

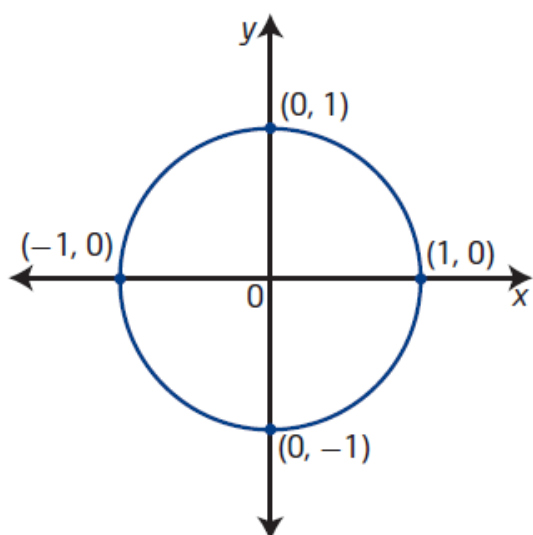


### Quadrantal Angles



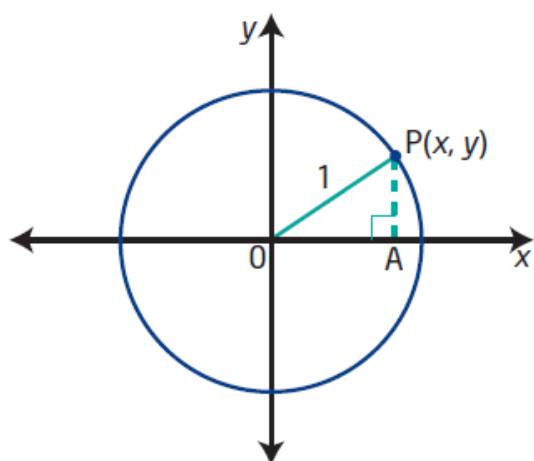


# Unit Circle



## unit circle

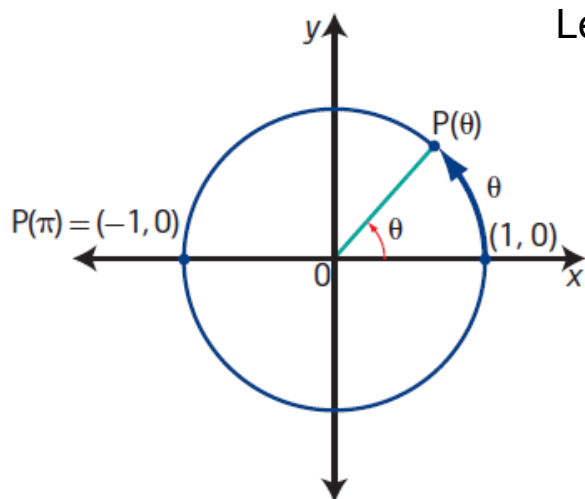
- a circle with radius 1 unit
- a circle of radius 1 unit with centre at the origin on the Cartesian plane is known as *the* unit circle



The equation of the unit circle is  $x^2 + y^2 = 1$ .

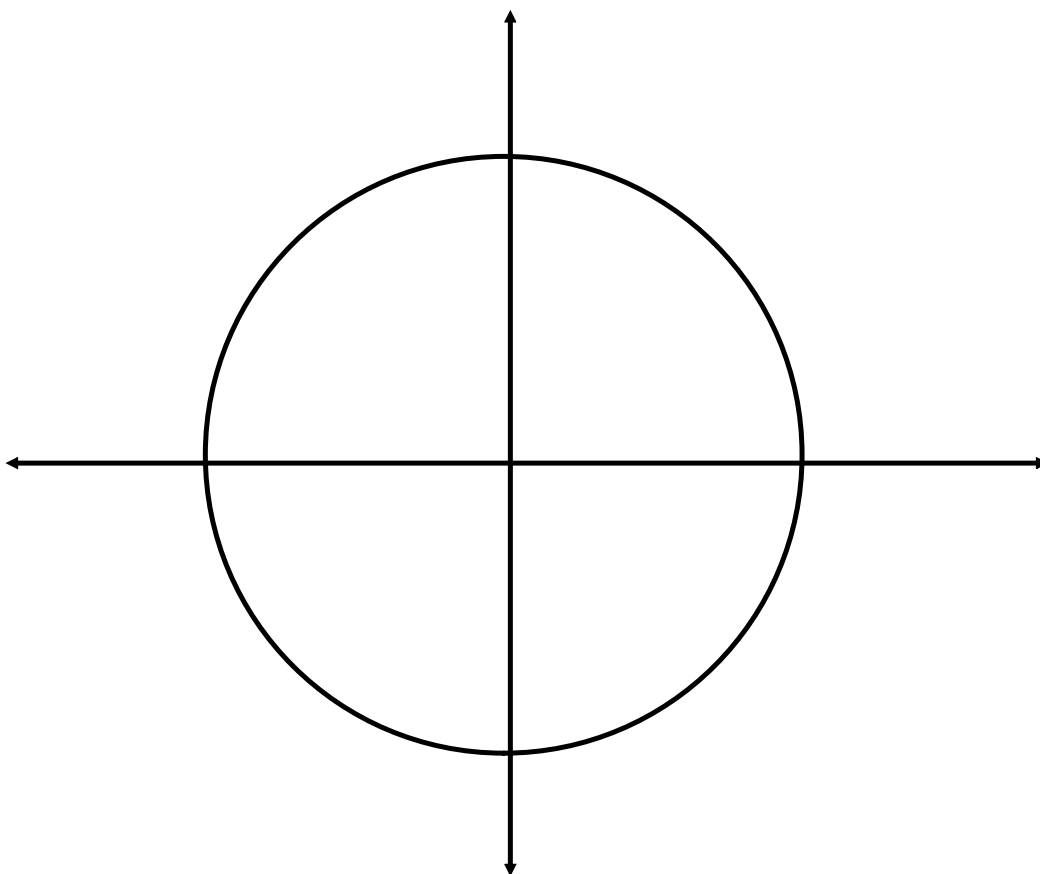
Determine the equation of a circle with centre at the origin and radius 6.

## Special Angles on the Unit Circle:

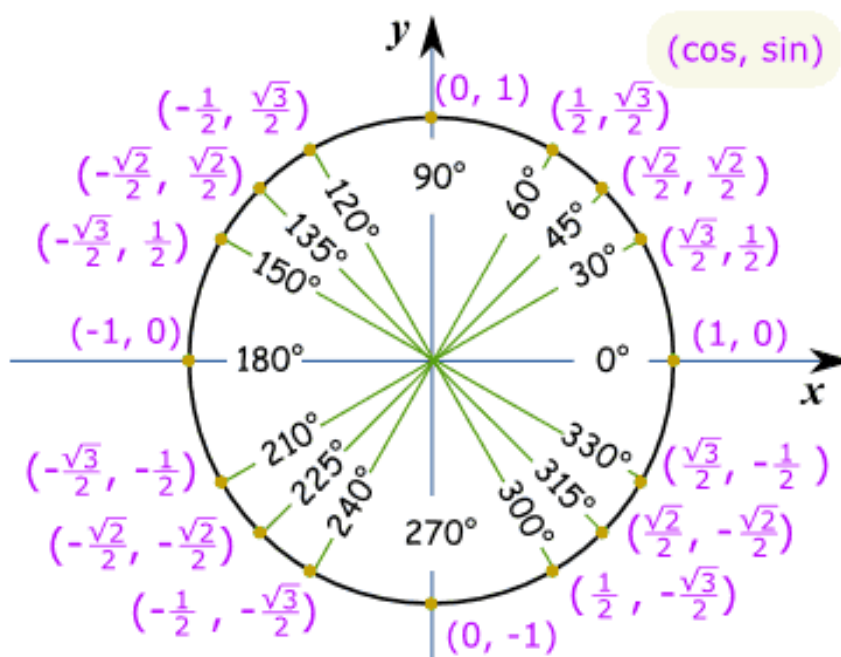


Let's use  $\frac{\pi}{4}$  as our reference angle

Construct reference triangles  
for all multiples of  $\pi/4$   
between 0 and  $2\pi$

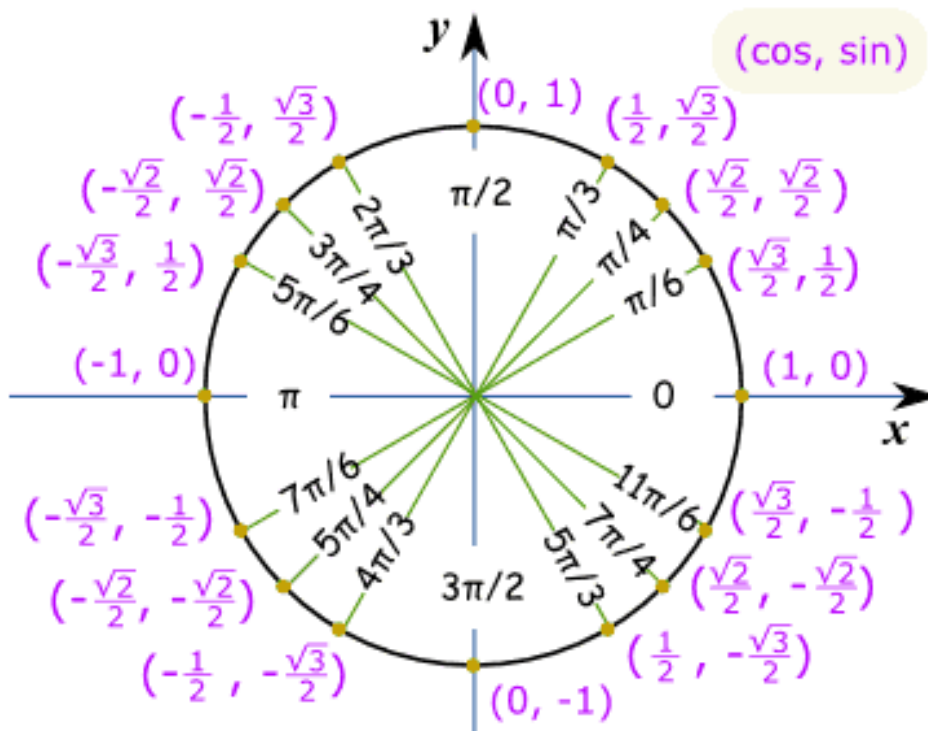


## Unit Circle of Special Angles in Degrees



This is lovely...so what is it used for????

### Unit Circle of Special Angles in Radians



## Attachments

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Worksheet - Sketching Angles in Radians.doc