

Warm up

Sum of Cubes

$$a^3 + b^3 = (a+b)(a^2 - ab + b^2)$$

$$x^6 + 27$$

$$(x^3 + 3)(x^4 - 3x^3 + 9)$$

Difference of Cubes

$$a^3 - b^3 = (a-b)(a^2 + ab + b^2)$$

$$8x^3 - 64y^3$$

$$8(x^3 - 8y^3)$$

$$8(x-2y)(x^2 + 2xy + 4y^2)$$

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Questions From Homework

$$\begin{aligned}
 & \textcircled{2} \rightarrow (x^5 - 5x^4)(-10x^3 + 50x^2) + 9x - 45 \\
 & x^4(x-5) - 10x^3(x-5) + 9(x-5) \\
 & (x-5)(x^4 - 10x^3 + 9) \quad \xleftarrow{\text{Simple trinomial}} \quad \frac{-9}{-9} \frac{x-1}{+1} = 9 \\
 & (x-5)(x^3 - 9)(x-1) \quad \xleftarrow{\text{Diff of Squares}} \\
 & (x-5)(x-3)(x+3)(x-1)(x+1)
 \end{aligned}$$

Factor Theorem

Factor Theorem

$(x-b)$ is a factor of $f(x)$ if and only if $f(b) = 0$.

Hint: Find a value of "x" that will make it = 0

$$\begin{aligned} &x^3 + 5x^2 - 2x - 24 \\ &(x-2) \quad + 5(x^2) - 2(x) - 24 \\ &\quad 8 + 20 - 4 - 24 \\ &\quad 0 \end{aligned}$$

- ① Common Factor (none)
- ② Count terms (4)
- ↳ grouping (does not work)

$(x - 2)$ is a factor

Use long division to find another factor:

$$\begin{array}{r} x^3 + 7x^2 + 12x \\ \hline x-2 \left. \begin{array}{r} x^3 + 5x^2 - 2x - 24 \\ -(x^3 - 2x^2) \\ \hline 7x^2 - 2x - 24 \\ -(7x^2 - 14x) \\ \hline 12x - 24 \\ -(12x - 24) \\ \hline 0 \end{array} \right. \end{array}$$

Factor further (if possible):

$$\begin{aligned} &(x-2)(x^2 + 7x + 12) \leftarrow \text{Simple trinomial} \quad \begin{matrix} 3 \times 4 = 12 \\ 3 + 4 = 7 \end{matrix} \\ &(x-2)(x+3)(x+4) \end{aligned}$$

Factor Theorem

Factor Theorem

$(x-b)$ is a factor of $f(x)$ if and only if $f(b) = 0$.

$$\begin{aligned}
 P(x) &= 2x^3 - 5x^2 - 4x + 3 & (x-(-1)) \text{ is a factor} \\
 &= 2(-1)^3 - 5(-1)^2 - 4(-1) + 3 & (x+1) \\
 &= -2 - 5 + 4 + 3 \\
 &= 0
 \end{aligned}$$

$$\begin{array}{r}
 \begin{array}{c}
 \color{red}{2x^3} - 7x + 3 \\
 \times + 1 \quad \overline{2x^3 - 5x^2 - 4x + 3} \\
 \underline{- (2x^3 + 2x^2)} \\
 \begin{array}{r}
 \color{green}{-7x^2} - 4x + 3 \\
 - (\color{green}{-7x^2} - 7x) \\
 \underline{\color{blue}{3x} + 3} \\
 - (\color{blue}{3x} + 3) \\
 \hline 0
 \end{array}
 \end{array}
 \end{array}$$

Factor further:

$$\begin{aligned}
 &(x+1)(2x^2 - x - 6) \quad \xrightarrow{\substack{\text{Decomp.} \\ -1 \times -6 = 6 \\ -1 + -6 = -7}} \\
 &(x+1)[(2x-3)(x+3)] \\
 &(x+1)[x(2x-1) - 3(2x-1)] \\
 &\boxed{(x+1)(2x-1)(x-3)}
 \end{aligned}$$

Homework

$$\textcircled{3} \text{ b) } x^3 - 7x + 6 \rightarrow x^3 + 0x^3 - 7x + 6$$

