Questions From Homework Questions From Homework

(a) 
$$y = \frac{1}{x^4} = 1x^{-4}$$
 d)  $y(t) = 8t^{-\frac{3}{4}}$ 

$$y' = -4x^{-5} = -\frac{4}{x^5}$$
  $y'(t) = -6t^{-\frac{3}{4}} = -\frac{6}{t^{\frac{3}{4}}}$ 

i) 
$$f(x) = \sqrt[3]{x} = x^{\frac{1}{3}}$$

$$f'(x) = \frac{1}{3}x^{-\frac{3}{3}} = \frac{1}{3}x^{\frac{3}{3}} = \frac{-\frac{3}{3}}{3}$$

k) 
$$y = \frac{1}{\sqrt{x}} = \frac{1}{x^{1/3}} = \frac{1}{x^{1/3}} = \frac{1}{\sqrt{x^3}}$$

$$y' = -\frac{1}{x^3} = -\frac{1}{3x^3} = \frac{1}{3\sqrt{x^3}}$$

$$y = \frac{3}{\sqrt{x}} = \frac{3}{x^{4}} = 3x^{-\frac{1}{4}}$$

$$3x^{-\frac{1}{4}} = \frac{3}{4}$$

$$-\frac{1}{4} - \frac{4}{4} = \frac{3}{4}$$

$$y' = -\frac{3}{4}x^{-\frac{5}{4}} = \frac{3}{4}x^{\frac{5}{4}}$$

$$y = \sqrt{3} \times \sqrt{5}$$
 $y = \sqrt{6} \times \sqrt{5} - 1$ 

(a) Find 
$$y'$$
 (b) Sub in  $x=8$ 

$$y'= \frac{3}{3}x^{3} = \frac{3\sqrt{x}}{3}$$

$$y'= \frac{3\sqrt{8}}{3} = \frac{3\sqrt{2}}{3}$$

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$$y = \frac{3}{3} =$$

$$5) y = \frac{6}{x} , x = -3$$

(1) find y'

$$y = \frac{6}{x} = 6x^{-1}$$

$$y' = \frac{6}{(3)} = \frac{6}{9} = \frac{-2}{3}$$

$$y' = -6x^{-2} = \frac{-6}{x^{2}}$$

$$f'(x) = \lim_{h \to 0} \frac{\frac{1}{x + h} - \frac{1}{x}}{h}$$

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$$f'(x) = \lim_{h \to 0} \frac{x - I(x+h)}{xh(x+h)}$$

$$f'(x) = \lim_{h \to 0} \frac{x - x - h}{xh(x+h)}$$

$$f'(x) = \lim_{h \to 0} \frac{xh(xth)}{xh(xth)} = \frac{-1}{x^3}$$

## **Example:**

Find the slope of the tangent line to the graph of the given function at the given x value.

$$g(x) = \sqrt[5]{x} \qquad x = 32$$

$$0 \text{ find } g'(x)$$

$$g(x) = \sqrt[5]{x} - x'$$

$$g'(x) = \sqrt[5]{3}$$

**Example:** 

Find the equation of the tangent line to the curve  $f(x) = x^6$  at the point (-2, 64)

Remember that the equation of a line is found by using the point-slope formula...  $y - y_1 = m(x - x_1)$ 

The curve is the graph of the function  $f(x) = x^6$  and we know that the slope of the tangent line at (-2, 64) is the derivative f'(-2)

- Find derivative
- Fill in x value and solve for slope
- Use equation of a line formula and solve

$$f(x) = x^6$$

$$f'(x) = 6x^{5}$$

$$\int_{0}^{1} (3) = 6(-33)$$

$$= -193$$

$$y_1 = -3$$
  $m = -193$ 

(11) 
$$y - y_1 = m(x - x_1)$$

$$y-64 = -193(x-6)$$

$$y - 6y = -192 \times -384$$

or 192x+y+320=0

## **Sums and Differences**

These next rules say that the derivative of a sum (difference) of functions is the sum (difference) of the derivatives:

The Sum Rule If f and g are both differentiable, then

$$\frac{d}{dx}[f(x) + g(x)] = \frac{d}{dx}f(x) + \frac{d}{dx}g(x)$$

The Difference Rule If f and g are both differentiable, then

$$\frac{d}{dx}[f(x) - g(x)] = \frac{d}{dx}f(x) - \frac{d}{dx}g(x)$$

## Demonstrate what this all means...

Differentiate each of the following:

1. 
$$f(x) = 2x^4 + \sqrt{x} = 3x^4 + x^{1/3}$$

$$f'(x) = 8x^3 + 1 x^{1/3} = 8x^3 + 1 x^{1/3}$$

2. 
$$f(x) = 6x^4 - 5x^3 - 2x + 17$$
  

$$f'(x) = 34x^3 - 15x^3 - 3$$

3. 
$$f(x) = (2x^3 - 5)^2 = (2x^3 - 5)(2x^3 - 5)$$
  
 $f(x) = 4x^6 - 10x^3 - 10x^3 + 35$   
 $f(x) = 4x^6 - 30x^3 + 35$   
 $f(x) = 34x^5 - 60x^3$ 

## Homework

(b) 
$$y = \frac{x+1}{\sqrt{x}} = \frac{x+1}{x^{1/3}} = \frac{x}{x^{1/3}} = x^{1/3}(x+1) = x^{1/3} + x^{-1/3}$$

$$y' = \frac{1}{3}x^{-1/3} - \frac{1}{3}x^{-1/3}$$