

## Questions from Homework

$$\textcircled{1} \text{ g) } y = \frac{x+1}{\sqrt{x}} = \frac{x+1}{x^{1/2}} = x^{-1/2}(x+1) = x^{1/2} + x^{-1/2}$$

$$y' = \frac{1}{2}x^{-1/2} - \frac{1}{2}x^{-3/2} = \frac{1}{2x^{1/2}} - \frac{1}{2x^{3/2}}$$

$$\text{k) } u(t) = a + \frac{b}{t} + \frac{c}{t^2} = a + bt^{-1} + ct^{-2}$$

$$u'(t) = -bt^{-2} - 2ct^{-3} = -\frac{b}{t^2} - \frac{2c}{t^3}$$

$$\text{l) } v(r) = \sqrt{r}(2+3r) = r^{1/2}(2+3r) = 2r^{1/2} + 3r^{3/2}$$

$$v'(r) = r^{-1/2} + \frac{9}{2}r^{1/2} = \frac{1}{\sqrt{r}} + \frac{9\sqrt{r}}{2}$$

## Questions from Homework

① At what point on the parabola  $y = 3x^2$  is the slope of the tangent line equal to 24  $\uparrow$   $m$

①  $y = 3x^2$   
 $y' = 6x$

②  $y' = 6x$   
 $24 = 6x$   
 $4 = x$

③  $y = 3x^2$   
 $y = 3(4)^2$   
 $y = 3(16)$   
 $y = 48$

④  $(4, 48)$

## Questions from Homework

(x, y)

- ⑧ Find the point on the curve  $y = x\sqrt{x}$  where the tangent line is parallel to  $6x - y = 4$   
same slope.

(i) Find slope of

$$6x - y = 4$$

$$-y = \frac{-6x + 4}{-1}$$

$$y = 6x - 4$$

$$(y = mx + b)$$

$$m = 6$$

(iv) Solve for y

$$y = x\sqrt{x}$$

$$y = (16)\sqrt{(16)}$$

$$y = 16(4)$$

$$y = 64$$

(ii) Find  $y'$  (slope of tangent)

$$y = x\sqrt{x} = x \cdot x^{1/2} = x^{3/2}$$

$$y' = \frac{3}{2}x^{1/2} = \frac{3\sqrt{x}}{2} \leftarrow m$$

(iii) set slopes equal

$$\frac{3\sqrt{x}}{2} = 6$$

$$\frac{3\sqrt{x}}{3} = \frac{12}{3}$$

$$\sqrt{x} = 4$$

$$(x^{1/2})^2 = (4)^2$$

$$x = 16$$

(16, 64) is the point

## Warm Up

Differentiate the following:

$$f(x) = -4x^2 - 5x(x^3 + 7)^2 + 2\sqrt[5]{x^9} - \frac{5}{x^{10}} + \frac{7x^2}{\sqrt{x}} - e^6$$

$$f(x) = -4x^2 - 5x(x^6 + 14x^3 + 49) + 2x^{9/5} - 5x^{-10} + 7x^2(x^{-1/2})$$

$$f(x) = -4x^2 - 5x^7 - 70x^4 - 245x + 2x^{9/5} - 5x^{-10} + 7x^{3/2}$$

$$f'(x) = -8x - 35x^6 - 280x^3 - 245 + \frac{18}{5}x^{4/5} + 50x^{-11} - \frac{21}{2}x^{-1/2}$$

## Differentiation Rules

### Product Rule:

**The Product Rule** If  $f$  and  $g$  are both differentiable, then

$$\frac{d}{dx} [f(x)g(x)] = f(x) \frac{d}{dx} [g(x)] + g(x) \frac{d}{dx} [f(x)]$$

Express the product rule verbally if you are considering a function of the form...

$$f(x) = (\text{First}) \times (\text{Second})$$

In words, *the Product Rule* says that the *derivative of a product of two functions is: the derivative of the first function times the second function, plus the first function times the derivative of the second function*

*Get in the habit of verbalizing the rule as you differentiate...it will help when the functions get more complicated.*

$$(fg)'(x) = f'(x)g(x) + f(x)g'(x)$$

Examples:

$$y = f(x)g(x)$$

$$y' = f'(x)g(x) + f(x)g'(x)$$

$$y = (2x^3 + 5)(3x^2 - x)$$

$$y' = \overset{\text{first}}{6x^2} \overset{\text{second}}{(3x^2 - x)} + (2x^3 + 5)(6x - 1)$$

$$y' = \underline{18x^4} - \underline{6x^3} + \underline{12x^4} - \underline{2x^3} + 30x - 5$$

$$y' = 30x^4 - 8x^3 + 30x - 5$$

$$f(x) = \sqrt{x}(2 - 3x) = x^{1/2}(2 - 3x)$$

$$f'(x) = \frac{1}{2}x^{-1/2}(2 - 3x) + x^{1/2}(-3)$$

$$f'(x) = \frac{1}{2x^{1/2}}(2 - 3x) - 3x^{1/2}$$

$$f'(x) = \frac{2 - 3x}{2x^{1/2}} - \frac{3x^{1/2}}{1} \quad \text{co: } 2x^{1/2}$$

$$f'(x) = \frac{2 - 3x}{2x^{1/2}} - \frac{6x}{2x^{1/2}} = \boxed{\frac{2 - 9x}{2\sqrt{x}}}$$

Examples:

$$f(x) = (7x^3 - x^2 + 5)(x^9 + 3x - 5)$$

$$f'(x) = (21x^2 - 2x)(x^9 + 3x - 5) + (7x^3 - x^2 + 5)(9x^8 + 3)$$

$$h(t) = (t^3 - 5t)(6\sqrt{t} - t^{-5})$$

$$h'(t) = (3t^2 - 5)(6\sqrt{t} - t^{-5}) + (t^3 - 5t)(3t^{-1/2} + 5t^{-6})$$

# Homework



