

Curve Sketching

Intercepts:

To find the x -intercept of $y = f(x)$, set $y = 0$ and solve for x .

To find the y -intercept of $y = f(x)$, set $x = 0$; the y -intercept is $f(0)$.

Example:
$$y = \frac{x^2 - x - 6}{x + 1}$$

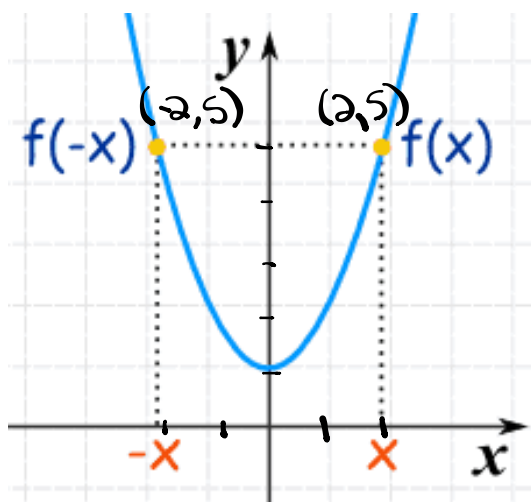
<p style="text-align: center;">x-int ($y=0$)</p> <p>$(x+1) 0 = \frac{x^2 - x - 6}{x+1} \cdot (x+1)$</p> <p>$0 = x^2 - x - 6$ factor $\begin{matrix} \underline{2} & \underline{x^3} = -6 \\ \underline{2} & \underline{+3} = -1 \end{matrix}$</p> <p>$0 = (x+2)(x-3)$</p> <p>$x+2=0 \quad \quad x-3=0$ $x=-2 \quad \quad x=3$</p> <p>$(-2, 0) \quad (3, 0)$</p>	<p style="text-align: center;">y-int ($x=0$)</p> <p>$y = \frac{(0)^2 - (0) - 6}{(0) + 1}$</p> <p>$y = \frac{-6}{1} = -6$</p> <p>$(0, -6)$</p>
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Symmetry:

An **even function** satisfies

$$f(-x) = f(x)$$

for all x in its domain. Thus, a function is even if it is unchanged when x is replaced by $-x$. The graph of an even function is symmetric about the y -axis.

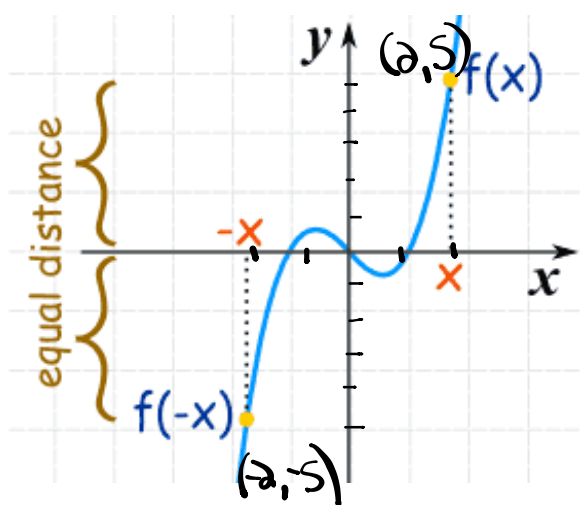


$$\left. \begin{array}{l} f(2) = 5 \\ f(-2) = 5 \end{array} \right\} f(-x) = f(x)$$

An **odd function** satisfies

$$f(-x) = -f(x)$$

for all x in its domain. The graph of an odd function is symmetric about the origin. $(0,0)$



$$\left. \begin{array}{l} f(a) = 5 \\ f(-a) = -5 \end{array} \right\} f(-x) = -f(x)$$

Symmetry is used to reduce the amount of work in graphing. If we have graphed an *even function* for $x \geq 0$, we just reflect in the *y-axis* to get the entire graph. For an *odd function* we just rotate through 180 degrees about the origin.

Example: Test: replace x with $(-x)$

Determine whether each function is even, odd, or neither

a) $f(x) = \underline{x^6}$

$$f(-x) = (-x)^6$$

$$f(-x) = (-x)(-x)(-x)(-x)(-x)(-x)$$

$$f(-x) = \underline{x^6}$$

$$f(-x) = f(x) \text{ (Even)}$$

b) $g(x) = x^3 + \frac{1}{x}$

$$g(-x) = (-x)^3 + \frac{1}{(-x)}$$

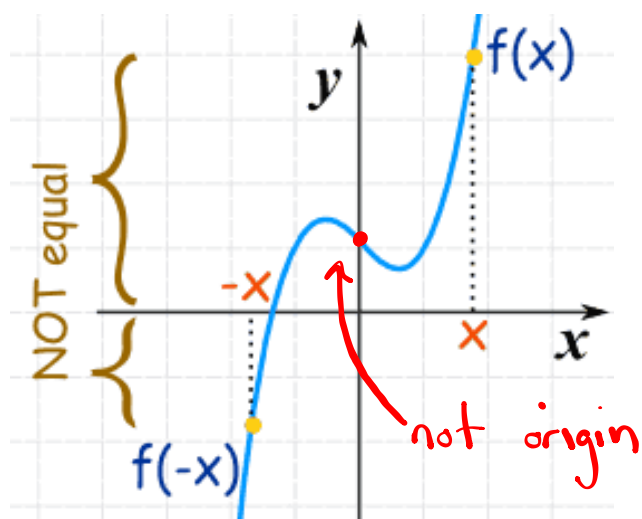
$$g(-x) = -x^3 - \frac{1}{x}$$

$$g(-x) = -\left(x^3 + \frac{1}{x}\right)$$

$$g(-x) = -g(x) \text{ (Odd)}$$

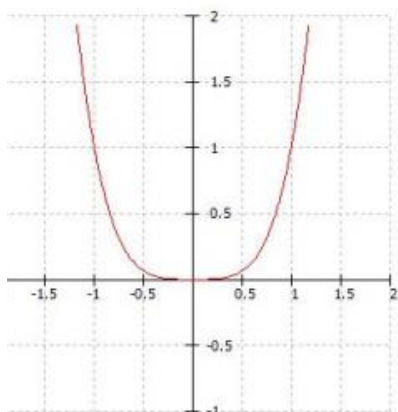
Is this function Even or Odd?

Neither

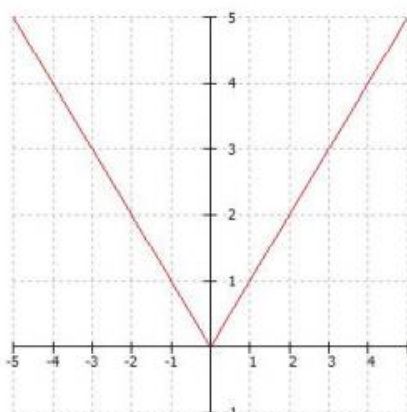


Homework

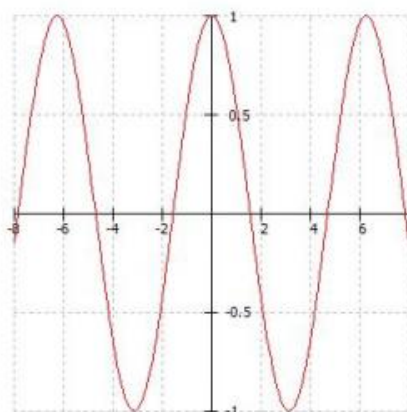
Even Functions



$f(x) = x^4$



$g(x) = |x|$



$h(x) = \cos x$