

Questions From Homework

① e) $5x^2 + 13x + 6$ $\frac{10}{5} \times \frac{3}{1} = \frac{30}{5}$
 $\frac{10}{5} + \frac{3}{1} = \frac{13}{1}$
 $(x + \frac{10}{5})(x + \frac{3}{1})$
 $(x + 2)(5x + 3)$

① g) $t^3 + 2t^2 - 3t$ $-1 \times 3 = -3$
 $t(t^2 + 2t - 3)$ $-1 + 3 = 2$
 $t(t-1)(t+3)$

③ f) $x^6 + 8$ $a^3 + b^3 = (a+b)(a^2 - ab + b^2)$
 $(x^2 + 2)(x^4 - 2x^2 + 4)$

② g) $x^4 - 16$
 $(x^2 + 4)(x^2 - 4)$
 $(x^2 + 4)(x + 2)(x - 2)$

③ b) $x^3 + 0x^2 - 7x + 6$ $x=1$
 $(1)^3 + 0(1)^2 - 7(1) + 6$ $(x-1)$ is a factor
 $1 + 0 - 7 + 6$
 0

| | |
|---|--|
| $\begin{array}{r} \underline{x-1} \overline{) x^3 + 0x^2 - 7x + 6} \\ \underline{-(x^3 - x^2)} \\ x^2 - 7x + 6 \\ \underline{-(x^2 - x)} \\ -6x + 6 \\ \underline{-(-6x + 6)} \\ 0 \end{array}$ | $\begin{array}{l} (x-1)(x^2 + x - 6) \\ (x-1)(x+3)(x-2) \end{array}$ |
|---|--|

Synthetic Substitution

Factor using synthetic substitution $x^3 - 7x^2 - 4x + 28$

Find a value of x that makes it equal 0

$$\begin{aligned} (\color{red}{2})^3 - 7(\color{red}{2})^2 - 4(\color{red}{2}) + 28 \\ \color{red}{8} - \color{red}{28} - \color{red}{8} + \color{red}{28} \end{aligned}$$

(x -value)

$$\begin{array}{r|l} \color{red}{2} & \end{array}$$



$$(x - \color{red}{2})(x^2 - 5x - 14)$$

$$(x - \color{red}{2})(x - 7)(x + 2)$$

(Coefficients of the polynomial)

$$\begin{array}{r|rrrr} & 1 & -7 & -4 & 28 \\ & & \color{red}{2} & -10 & -\color{red}{28} \\ \hline & 1 & -5 & -14 & \end{array}$$

Bring down the first coefficient

Multiply the first coefficient by the x -value and place under the second coefficient. ADD.

Repeat the steps. The coefficients of the other factor are in the bottom row.

$$x^3 + 5x^2 - 2x - 24 \quad \text{Find a value of } x \text{ that makes it equal } 0$$

$$(\cancel{2})^3 + 5(\cancel{2})^2 - \cancel{2}(\cancel{2}) - 24$$

$$8 + 20 - 4 - 24$$

$\overset{0}{\cancel{2}}$
(x-value)

(Coefficients of the polynomial)

$$\begin{array}{r} \cancel{2} \end{array} \Big|$$

$$\begin{array}{cccc} 1 & 5 & -2 & -24 \end{array}$$

$$\begin{array}{cccc} & \cancel{2} & 14 & \cancel{24} \end{array}$$

$$\hline \begin{array}{cccc} 1 & 7 & 12 & \end{array}$$

$$(x - \cancel{2})(x^2 + 7x + 12)$$

$$(x - 2)(x + 4)(x + 3)$$

Homework

Omit 31 cf
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$$\textcircled{29} \text{ a) } x^3 - 4x^2 + x + 6 = 0$$

$$(-1)^3 - 4(-1)^2 + (-1) + 6 = 0$$

$$-1 - 4 - 1 + 6 = 0$$

$$0 = 0$$

$$x = -1$$

$\textcircled{32}$ Use synthetic sub.

$$\text{a) } (a^3 - 4a^2 + a + 6) \div (a - 2)$$

$$\begin{array}{r|rrrr} 2 & 1 & -4 & 1 & 6 \\ & & 2 & -4 & -6 \\ \hline & 1 & -2 & -3 & \end{array}$$