

# Properties of a Function

# Domain & Range

**Domain** - the set of first elements in a relation  
(x-values)

**Range** - the set of second elements in a relation  
(y-values)

<sup>x</sup> Sport	<sup>y</sup> Equipment
badminton	shuttlecock
badminton	racquet
hockey	puck
hockey	stick
tennis	ball
tennis	racquet
soccer	ball

**First**

**Second**

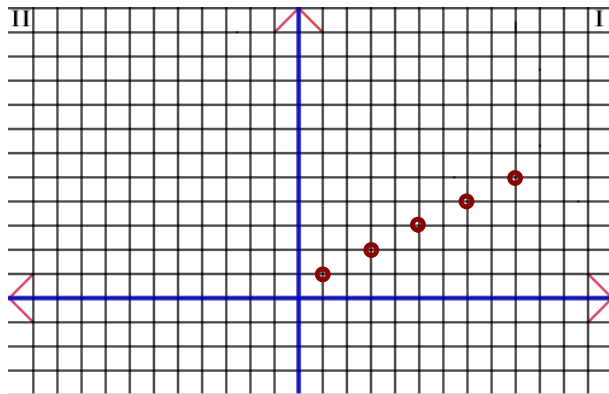
( **Sport, Equipment** )

**Domain**

The set of first elements:  
 { badminton, hockey, tennis, soccer }

**Range**

The set of second elements:  
 { shuttlecock, racquet, puck, stick, ball }



**Remember!!**

$(x, y)$

**Ordered Pairs:**

$\left\{ \begin{array}{c} \text{1st} \quad \text{2nd} \quad \text{1st} \quad \text{2nd} \quad \text{1st} \quad \text{2nd} \quad \text{1st} \quad \text{2nd} \quad \text{1st} \quad \text{2nd} \\ \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \\ \underline{(1,1)}, \underline{(3,2)}, \underline{(5,3)}, \underline{(7,4)}, \underline{(9,5)} \end{array} \right\}$

**Domain** The set of first elements:  $\{1, 3, 5, 7, 9\}$

**Range** The set of second elements:  $\{1, 2, 3, 4, 5\}$

# Function or Nonfunction

Function,

A relation where each element in the first set is associated with one and only one element in the second set.

(x's can't repeat)

<i>x</i>	<i>y</i>
Sport	Equipment
badminton	shuttlecock
badminton	racquet
hockey	puck
hockey	stick
tennis	ball
tennis	racquet
soccer	ball

*x's repeat*

# Function or Nonfunction

{ (2, 5), (3, 7), (4, 2), (2, 6), (8, 0) }

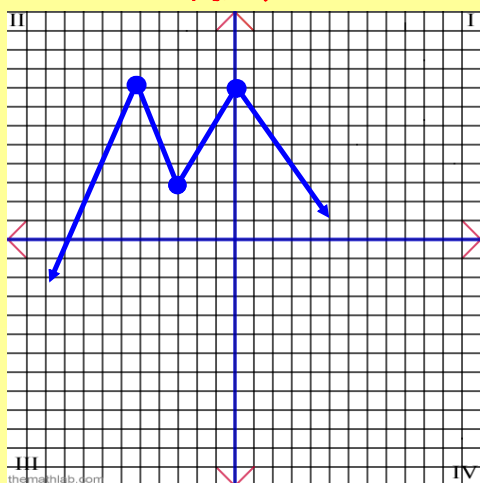
Function or Nonfunction

# Function or Nonfunction

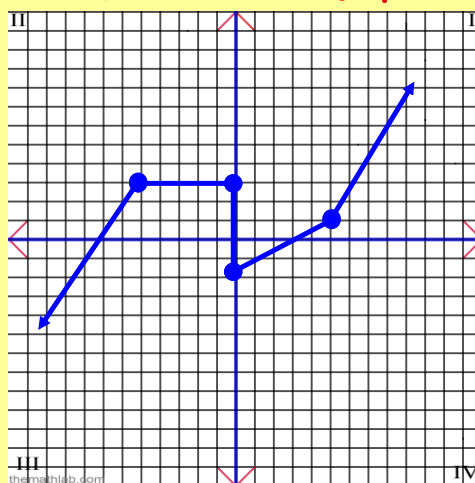


Use the vertical line test!!

Function



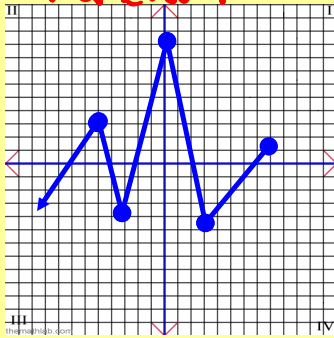
Non-Function



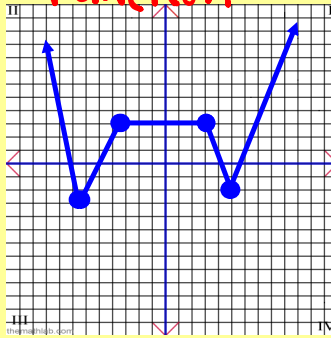


# Function or Nonfunction

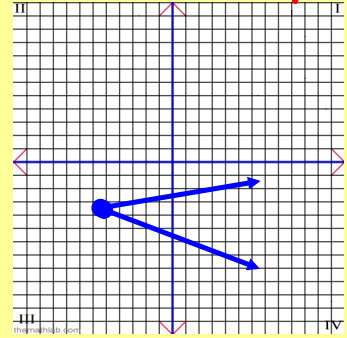
Function



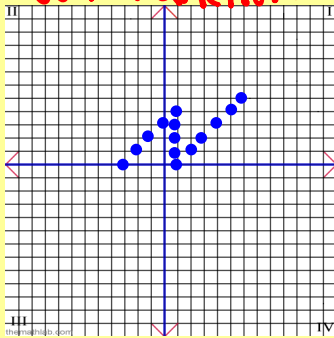
Function



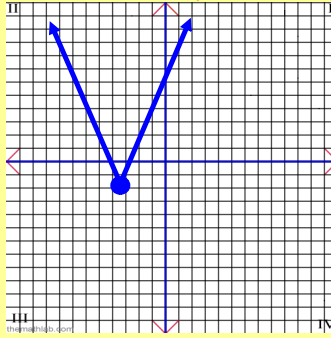
Non-Function



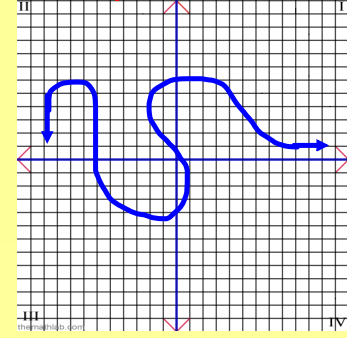
Non-Function

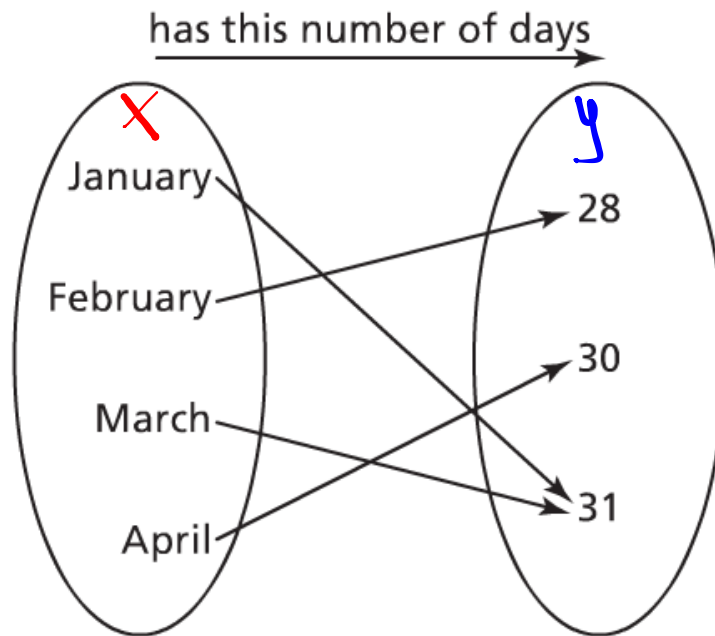


Function



Non-Function





## Function or Nonfunction

Domain: {January, February, March, April}

Range: {28, 30, 31}

# Independent / Dependent

## Dependent

- a variable whose value is determined by the value of another (independent) variable. (y-value)

## Independent

- a variable whose value is not determined by the value of another variable, and whose value determines the value of another (dependent) variable  
(x-value)

## Independent Variable

- Hours do not depend on the person's pay.

Hours Worked, $h$	Gross Pay, $P$ (\$)
1	12
2	24
3	36
4	48
5	60

## Dependent Variable

- A person's pay often depends on the number of hours worked.

<sup>x</sup> Hours Worked, $h$	<sup>y</sup> Gross Pay, $P$ (\$)
1	12
2	24
3	36
4	48
5	60

Let's write the function notation

$$P(h) = 12h$$

What is the person's pay after 20 hours?

$$\begin{aligned}P(20) &= 12(20) \\ &= \$240\end{aligned}$$

Examples:

$$f(x) = 3x + 2$$
$$y = 3x + 2$$

**Try This!!**

<sup>x</sup> Number of Marbles, $n$	<sup>y</sup> Mass of Marbles, $m$ (g)
1	1.27
2	2.54
3	3.81
4	5.08
5	6.35
6	7.62

- State the domain & Range.
- Is this relation a function?
- State the dependent and independent variables.
- Write the function notation.

## Solution:

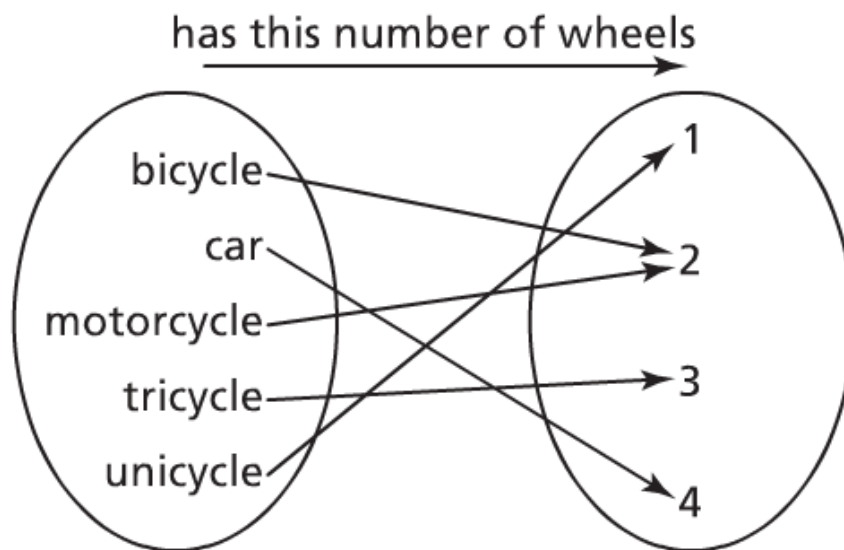
a) Domain: {1, 2, 3, 4, 5, 6}

Range: {1.27, 2.54, 3.81, 5.08, 6.35, 7.62 }

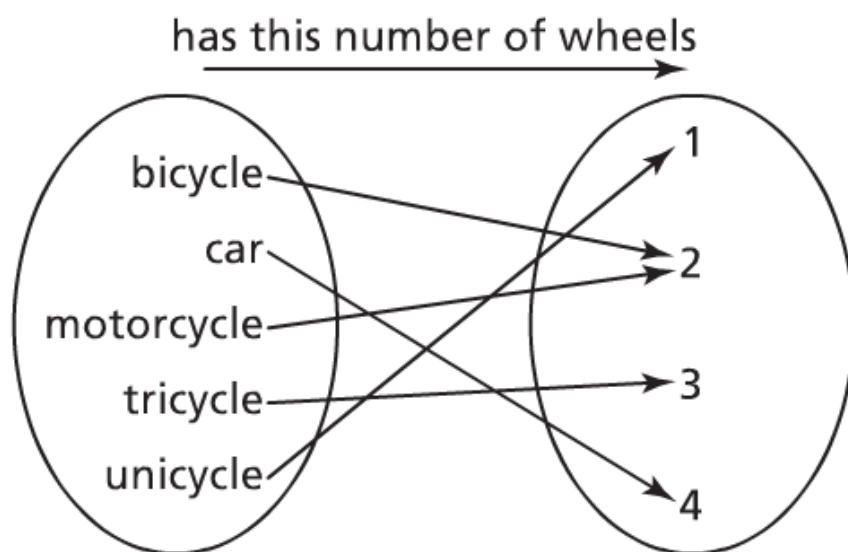
b) Function (x's do not repeat)

c) Independent - Number of marbles (x)  
Dependent - Mass of marbles (y)

d)  $M(n) = 1.27n$

**Domain****The first set of elements:****{bicycle, car, motorcycle, tricycle, unicycle}****Range****The second set of elements:****{1, 2, 3, 4}**





# Function or Nonfunction

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