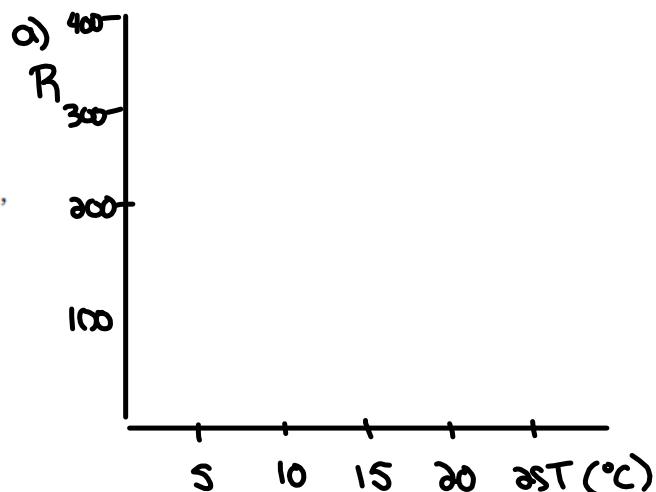


Questions from Homework

8. If seafood is not kept frozen (below 0 °C), it will spoil due to bacterial growth. The relative rate of spoilage increases with temperature according to the model

$R = 100(2.7)^{\frac{T}{8}}$, where T is the temperature, in degrees Celsius, and R is the relative spoilage rate.

- a) Sketch a graph of the relative spoilage rate R versus the temperature T from 0 °C to 25 °C.
- b) Use your graph to predict the temperature at which the relative spoilage rate doubles to 200.
- c) What is the relative spoilage rate at 15 °C?
- d) If the maximum acceptable relative spoilage rate is 500, what is the maximum storage temperature?



9. A bacterial culture starts with 2000 bacteria and doubles every 0.75 h. After how many hours will the bacteria count be 32 000?

Given:

$$\text{Initial Amount} = 2000$$

$$\text{Base} = 2$$

$$\exp = \frac{x}{0.75}$$

$$A = 32000$$

$$\frac{\log 16}{\log 2} = 4$$

↑
Base

$$y = 2000(2)^{\frac{x}{0.75}}$$

$$A = 2000(2)^{\frac{t}{0.75}}$$

$$\frac{32000}{2000} = \frac{2000(2)^{\frac{t}{0.75}}}{2000}$$

$$16 = 2^{\frac{t}{0.75}}$$

$$2^4 = 2^{\frac{t}{0.75}}$$

$$(0.75)4 = \frac{t}{0.75} (0.75)$$

$3h = t$

$$16 = 2^{\frac{t}{0.75}}$$
$$\cancel{16} = (\cancel{16})^{\frac{0.25}{0.75}}$$

$$(0.75)^{-1} = \frac{0.25t}{0.75} (0.75)$$

$$\frac{0.75}{0.25} = \frac{0.25t}{0.25}$$

$$3 = t$$

Given: $y = -3(2)^{2x+2} + 4$

$$y = -3(\underline{2})^{\underline{2(x+1)}} + \underline{4}$$

- i) state the parameters and describe the corresponding transformations
- ii) create a table to show what happens to the given points under each transformation
- iii) sketch the graph of the base function and the transformed function
- iv) describe the effects on the domain, range, equation of the horizontal asymptote, and intercepts

(i) $y = \underline{-3}(\underline{2})^{\underline{2(x+1)}} + \underline{4}$ $c = \text{base} = 2$

$a = -3 \rightarrow$ a vertical stretch by a factor of 3
and a reflection in the x-axis

$b = 2 \rightarrow$ a horizontal stretch by a factor of $\frac{1}{2}$

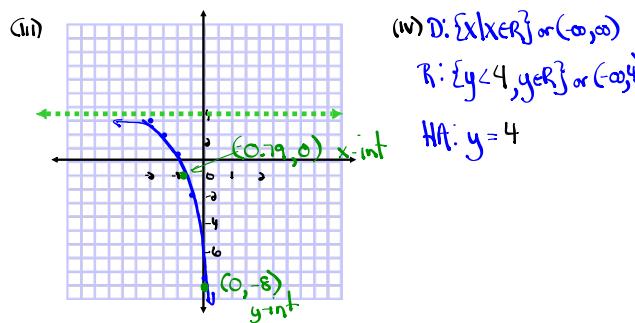
$h = -1 \rightarrow 1 \text{ unit left}$

$k = 4 \rightarrow 4 \text{ units up}$

(ii) $(x, y) \rightarrow \left(\frac{1}{2}x - 1, -3y + 4\right)$

$$\begin{array}{|c|c|} \hline x & y \\ \hline -2 & \frac{1}{4} \\ -1 & \frac{1}{2} \\ 0 & 1 \\ 1 & 2 \\ 2 & 4 \\ \hline \end{array}$$

$$\begin{array}{|c|c|} \hline x & y \\ \hline -2 & \frac{13}{4} = 3.25 \\ -1.5 & \frac{5}{2} = 2.5 \\ -1 & 1 \\ -0.5 & -2 \\ 0 & -8 \\ \hline \end{array}$$



x int ($y = 0$)

 $y = -3(2)^{2(x+1)} + 4$
 $0 = -3(2)^{2(x+1)} + 4$
 $-4 = -3(2)^{2(x+1)}$
 $\frac{-4}{-3} = 2^{2(x+1)}$
 $\log \frac{4}{3} = 2(x+1)$
 $\frac{\log 4}{\log 3} = 2(x+1)$
 $\frac{0.43}{2} = 2(x+1)$
 $0.21 = 2(x+1)$
 $\boxed{0.79 = x}$
 $\underline{\underline{(-0.79, 0)}}$

y int ($x = 0$)

 $y = -3(2)^{2(0+1)} + 4$
 $y = -3(2)^{2(1)} + 4$
 $y = -3(2^2) + 4$
 $y = -3(4) + 4$
 $y = -12 + 4$
 $\boxed{y = -8}$

Check graph for these points $(0, -8)$

Ex: Exponential Equation

$$64^x = \left(\frac{1}{8}\right)^{x+1} (\sqrt{32})$$

$$64^x = \left(\frac{1}{8}\right)^{x+1} \cdot (32)^{\frac{1}{2}}$$

$$\frac{\log 64}{\log 2} = 6$$

$$(2^6)^x = \left(\frac{1}{2^3}\right)^{x+1} (2^5)^{\frac{1}{2}}$$

$$\frac{\log(1/8)}{\log 2} = -3$$

$$\frac{\log 32}{\log 2} = 5$$

$$2^{6x} = 2^{-3x-3} \cdot 2^{\frac{5}{2}}$$

$$2^{6x} = 2^{-3x-3 + \frac{5}{2}}$$

$$2^{6x} = 2^{-3x - \frac{6}{2} + \frac{5}{2}}$$

$$2^{6x} = 2^{-3x - \frac{1}{2}}$$

$$6x = -3x - \frac{1}{2}$$

$$\frac{9x}{9} = -\frac{1}{2} \div 9$$

$$x = -\frac{1}{2} \cdot \frac{1}{9}$$

$$x = -\frac{1}{18}$$

Base α : a) $\left(\frac{1}{4}\right)$ and $\sqrt{64}$

$\left(\frac{1}{4}\right)$ and 8

$$\frac{\log(1)}{\log \alpha} = -\alpha \quad \text{and} \quad (\alpha)^3 = \frac{\log 8}{\log \alpha} = 3$$

$$\begin{aligned} & \sqrt{64} \\ & (\underline{\underline{64}})^{\frac{1}{2}} \\ & (\cancel{2}^6)^{\frac{1}{2}} \\ & \cancel{2}^3 \end{aligned}$$

$$\begin{aligned} & \underline{\underline{4}}^6 \quad \text{or} \quad 4096 \\ & (\cancel{2}^6)^6 \\ & \cancel{2}^{12} \end{aligned}$$

$$\frac{\log 4096}{\log \cancel{2}} = \underline{\underline{12}}_{\text{base}}^{\text{exp}}$$

$$\left(\frac{1}{125}\right)^{2x} = 5^{3x+2} \cdot \sqrt{3125}$$

$$\left(\frac{1}{125}\right)^{2x} = \underline{(5)^{3x+2}} \cdot \underline{(3125)^{\frac{1}{2}}}$$

$$(5^{-3})^{2x} = (5)^{3x+2} (5^5)^{\frac{1}{2}}$$

$$5^{-6x} = 5^{3x+2} \cdot 5^{\frac{5}{2}}$$

$$5^{-6x} = 5^{3x+2 + \frac{5}{2}}$$

$$\cancel{5^{-6x}} = \cancel{5^{3x+2 + \frac{5}{2}}}$$

$$-6x = 3x + \frac{9}{2}$$

$$\frac{-9x}{-9} = \frac{9}{2} \div -9$$

$$x = \frac{9}{2} \cdot -\frac{1}{9}$$

$$x = -\frac{9}{18} = -\frac{1}{2}$$

Homework

Chapter 7 Review pg. 366-367 (Do all questions)

For $y = c^x$

D: $\{x | x \in \mathbb{R}\}$

R: $\{y | y > \underline{0}, y \in \mathbb{R}\}$

x int: none

y int: $(0, 1)$

HA: $y = \underline{0}$

For $y = ac^{b(x-h)} + \underline{k}$

D: $\{x | x \in \mathbb{R}\}$

R: $\{y | y > \underline{k}, y \in \mathbb{R}\}$ (if $a < 0$ then $y < k$)

x int: sub 0 in for y

y int: sub 0 in for x

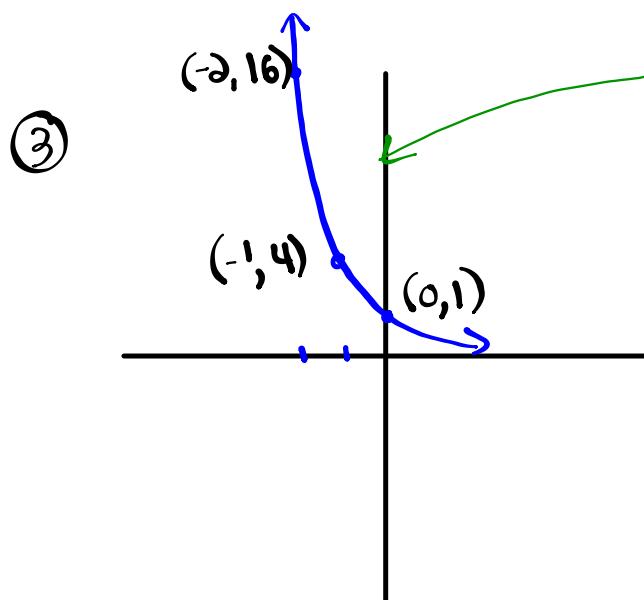
HA: $y = \underline{k}$

$$\textcircled{6} \quad \underline{\underline{a}} = 1.07^x$$

$$\cancel{(1.07)}^{10.2} = \cancel{1.07}^x$$

$$\frac{\log \underline{\underline{a}}}{\log \cancel{1.07}} = \frac{10.2}{\cancel{\text{Base}}} \exp$$

$$10.2 = x$$



x	y
-2	16
-1	4
0	1

$$y = \left(\frac{1}{4}\right)^x$$

⑪ b) $2^{x-2} = \underline{\underline{3^{x+1}}}$

$$2^{x-2} = (2)^{1.58x+1}$$

$$\frac{\log 3}{\log 2} = 1.58 \quad \begin{matrix} \text{Base} \\ \downarrow \\ \text{exp} \end{matrix}$$

$$2^{x-2} = 2^{1.58x+1.58}$$

$$x-2 = 1.58x + 1.58$$

$$-2 - 1.58 = 1.58x - x$$

$$\frac{-3.58}{0.58} = \frac{0.58x}{0.58}$$

$-6.17 = x$

⑫ $N_1 - 6S$ half-life of 2.5 h

$$\text{Base} = \frac{1}{2}$$

$$A_F = A_0 \left(\frac{1}{2}\right)^{\frac{t}{2.5}}$$

$$\text{exp} = \frac{t}{2.5}$$

Initial Amount = A_0

$$y = a(c)^{b(x-h)} + k \quad \left| \begin{array}{l} y = \text{Initial Amount (Base)}^{\text{exp.}} \\ \text{Finding a common base} \\ \frac{\log(\text{have})}{\log(\text{want})} = \text{exp.} \\ \text{Base} \end{array} \right.$$

$$(x, y) \rightarrow \left[\frac{1}{b}x + h, ay + k \right]$$

Ex:

$$\sqrt{81} \cdot 9^x = 81^{5x-4} \div \left(\frac{1}{3}\right)^x$$

$$81^{\frac{1}{2}} \cdot 9^x = 81^{5x-4} \div \left(\frac{1}{3}\right)^x$$

$$(3^3)^{\frac{1}{2}} \cdot (3^2)^x = (3^4)^{5x-4} \div (3^{-1})^x$$

$$3^{2x+3} \cdot 3^{2x} = 3^{20x-16} \div 3^{-x}$$

$20x-16-(x)$
 $20x-16+x$

$$2x+3 = 2x-16$$

$\cancel{2x+3}$ $\cancel{2x-16}$

$2x+3/2 = 2x-16$

$$\frac{3}{2} + \frac{16}{1} = 21x - 2x$$

$$\frac{3}{2} + \frac{32}{2} = 19x$$

$$\frac{35}{2} = \frac{19x}{19}$$

$$\frac{35}{2} \times \frac{1}{19} = x$$

$$\frac{35}{38} = x$$

**7.1 Characteristics of Exponential Functions,
pages 334-345**

1. Match each item in set A with its graph from set B.

Set A

a) The population of a country, in millions, grows at a rate of 1.5% per year. **(Increasing)** B

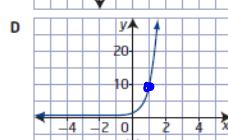
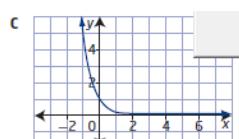
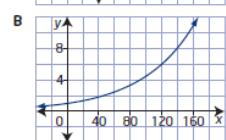
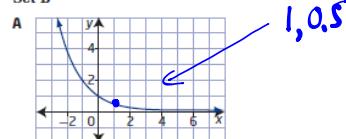
b) $y = 10^x$ **(Increasing)** D

c) Tungsten-187 is a radioactive isotope that has a half-life of 1 day. **(Decreasing)** A

d) $y = 0.2^x$ **(Decreasing)**

$$\begin{array}{|c|c|} \hline x & y \\ \hline 0 & 1 \\ 1 & 0.5 \\ \hline \end{array}$$

Set B



③ $\begin{array}{l} (x, y) \\ -2, 16 \\ -1, 4 \\ 0, 1 \end{array} > \frac{1}{4}$ $y = c^x$ (Find c)
 $y = (\frac{1}{4})^x$

$$\begin{array}{r} 16 \\ | \\ \left(\frac{1}{4}\right)^{-2} \\ 4^2 \\ 16 \end{array} \quad \checkmark$$

⑤ $y = -2(4)^{\frac{3(x-1)}{3}} + 2 \quad a = -2 \quad b = 3 \quad h = 1 \quad k = 2$

$$y = 4^x \quad (x, y) \rightarrow \left(\frac{1}{3}x+1, -2y+2\right)$$

x	y
-2	1/16
-1	1/4
0	1
1	4
2	16

x	y
1/3	15/8
2/3	3/2
1	0
4/3	-6
5/3	-20

$$\textcircled{1} \text{ c) } \left(\sqrt[3]{216}\right)^5$$

$$(216^{\frac{1}{3}})^5$$

$$(216)^{\frac{5}{3}}$$

$$\frac{\log 216}{\log 6} = 3 \quad (6^3)^{\frac{5}{3}}$$

$$6^5$$

$$y = c^x$$

$$16 = c^{-2}$$

$$16 = \left(\frac{1}{c}\right)^2$$

$$16 = \frac{1}{c^2}$$

$$16c^2 = 1$$

$$c^2 = \frac{1}{16}$$

$$c = \frac{1}{4}$$