

**Powers Review**

*Answer Key*

1. Write  $186^{4/5}$  as a radical.

$$\sqrt[5]{186^4}$$

2. Write  $\sqrt[8]{\left(\frac{684}{15}\right)^{11}}$  as a power.

$$\left(\frac{684}{15}\right)^{11/8}$$

3. Evaluate  $0.09^{1/2}$  without using a calculator. (Express as a radical and then evaluate)

$$\begin{aligned} \textcircled{3} \left(\frac{9}{100}\right)^{1/2} &= \sqrt{\frac{9}{100}} \\ &= \frac{3}{10} \end{aligned}$$

4. Evaluate  $(-8)^{-1/3}$  without using a calculator. (Express as a radical and then evaluate)

$$\begin{aligned} \textcircled{4} (-8)^{-1/3} &= \frac{1}{(-8)^{1/3}} \\ &= \frac{1}{\sqrt[3]{-8}} \\ &= \frac{1}{-2} \end{aligned}$$

5. Evaluate  $\left(\frac{16}{625}\right)^{1/4}$  without using a calculator. (Express as a radical and then evaluate)

$$\begin{aligned} \textcircled{5} \sqrt[4]{\frac{16}{625}} &= \frac{2}{5} \\ \textcircled{6} \sqrt[4]{\frac{125}{8}} &= \left(\frac{5}{2}\right)^{1/4} \\ &= \frac{625}{16} \end{aligned}$$

6. Evaluate  $\left(\frac{125}{8}\right)^{4/3}$ .

a.  $\frac{625}{4}$

b. 7.858 958...

c.  $\frac{625}{16}$

d.  $\frac{625}{8}$

7. Evaluate  $2^{-3}$  without using a calculator.

$$\textcircled{7} 2^{-3} \quad \textcircled{8} \left(\frac{2}{3}\right)^{-3}$$

8. Evaluate  $(2)^{-3}$

6. Evaluate  $\left(\frac{125}{8}\right)^{\frac{1}{3}}$ .

a.  $\frac{625}{4}$

b. 7.858 958...

c.  $\frac{625}{16}$

d.  $\frac{625}{8}$

$$= \frac{2}{5} \left( \frac{5}{2} \right)^3$$

$$= \frac{625}{16}$$

7. Evaluate  $2^{-3}$  without using a calculator.

8. Evaluate  $\left(\frac{2}{3}\right)^{-3}$ .

⑦  $2^{-3} = \frac{1}{2^3} = \frac{1}{8}$

⑧  $\left(\frac{2}{3}\right)^{-3} = \left(\frac{3}{2}\right)^3 = \frac{27}{8}$

9. Simplify  $x^{-2}y^6 \cdot x^3y^{-8}$ . Write using powers with positive exponents.

$$x^{-2}y^{-2} = \frac{x}{y^2}$$

10. Simplify  $\frac{12p^3q^{-7}}{15pq^6}$ . Write using powers with positive exponents.

$$\frac{4p^2q^{-13}}{5q^{13}} = \frac{4p^2}{5q^{13}}$$

11. Evaluate  $\left(-\frac{8}{5}\right)^{\frac{3}{4}} \cdot \left(-\frac{8}{5}\right)^{\frac{1}{4}}$ .

⑪  $\left(-\frac{8}{5}\right)^{\frac{8}{4}}$   
 $\left(-\frac{8}{5}\right)^2 = \frac{64}{25}$

12. Simplify  $\frac{(5b^7)^3}{(2a^3)^4} = \frac{5^3 b^{21}}{2^4 a^{12}}$

13. Simplify  $\frac{(m^3n^{-3})^{-1}}{(m^{-2}n)^4} = \frac{m^{-3}n^3}{m^{-8}n^4} = \frac{m^5n^{-1}}{1} = \frac{m^5}{n}$

11. Evaluate  $\left(-\frac{8}{5}\right)^{\frac{7}{4}} \cdot \left(-\frac{8}{5}\right)^{\frac{1}{4}}$   $\rightarrow \left(-\frac{8}{5}\right)^2 = \frac{64}{25}$

12. Simplify  $\frac{(5b^7)^3}{(2a^3)^4} = \frac{5^3 b^{21}}{2^4 a^{12}}$

13. Simplify  $\frac{(m^3 n^{-3})^{-1}}{(m^{-2} n)^4} = \frac{m^{-3} n^3}{m^{-8} n^4} = \frac{m^5 n^{-1}}{1} = \frac{m^5}{n}$

**Evaluate:**

a)  $2401^{3/4}$   
 $\sqrt[4]{2401}^3$   
 $7^3$   
 $343$

b)  $32^{-0.4}$   
 $= 32^{-4/10}$   
 $= 32^{-2/5}$   
 $= \frac{1}{32^{2/5}}$   
 $= \frac{1}{2^5 \cdot 32^2}$   
 $= \frac{1}{32} = \frac{1}{4}$

**Simplify:**

a)  $\left(\frac{(6x^8 y^{-3} \cdot x^{11} y^3)}{(2xy^7)}\right)^{-2}$   
 $\left(\frac{6x^{19} y^0}{2xy^7}\right)^{-2}$   
 $(3x^{18} y^{-7})^{-2}$   
 $\frac{3^{-2} x^{-36} y^{14}}{1} = \frac{y^{14}}{3^2 x^{36}}$

b)  $\left(\frac{5^6 x^3 y^5}{5x^{-2} y^3}\right)^3$   
 $(5^5 x^5 y^2)^3$   
 $5^{15} x^{15} y^6$