

Warm Up

Prove the following identities:

$$\frac{1}{\cot x} = \sin x \sec x$$

$$1 \div \frac{\cos x}{\sin x}$$

$$1 \cdot \frac{\sin x}{\cos x}$$

$$\frac{\sin x}{\cos x}$$

$$\sin x \left(\frac{1}{\cos x} \right)$$

$$\frac{\sin x}{\cos x}$$

$$1 - \cos^2 \theta = \frac{\cos \theta \sin \theta}{\cot \theta}$$

$$\sin^2 \theta$$

$$\cos \theta \sin \theta \div \frac{\cos \theta}{\sin \theta}$$

$$\cancel{\cos \theta} \sin \theta \cdot \frac{\sin \theta}{\cancel{\cos \theta}}$$

$$\sin^2 \theta$$

Questions from last night's homework?

$$\textcircled{a} \text{ j) } \boxed{\tan \theta} + \boxed{\cot \theta} = \frac{1}{\sin \theta \cos \theta}$$

$$\frac{\sin \theta}{\cos \theta} + \frac{\cos \theta}{\sin \theta}$$

$$\frac{\sin^2 \theta}{\sin \theta \cos \theta} + \frac{\cos^2 \theta}{\sin \theta \cos \theta}$$

$$\frac{\sin^2 \theta + \cos^2 \theta}{\sin \theta \cos \theta}$$

$$\frac{1}{\sin \theta \cos \theta}$$

$$\textcircled{a} \text{ g) } \boxed{\cot \theta} \cdot \boxed{\csc \theta} = \frac{\cos \theta}{1 - \cos^2 \theta}$$

$$\frac{\cos \theta}{\sin \theta} \cdot \frac{1}{\sin \theta}$$

$$\frac{\cos \theta}{\sin^2 \theta}$$

$$\frac{\cos \theta}{\sin^2 \theta}$$

Trig Identities

$\tan \theta = \frac{\sin \theta}{\cos \theta}$ $\cot \theta = \frac{\cos \theta}{\sin \theta}$	$\sin^2 \theta + \cos^2 \theta = 1$ $\tan^2 \theta + 1 = \sec^2 \theta$ $1 + \cot^2 \theta = \csc^2 \theta$
$\csc \theta = \frac{1}{\sin \theta}$ $\sec \theta = \frac{1}{\cos \theta}$ $\cot \theta = \frac{1}{\tan \theta}$	$\sin \theta = \frac{1}{\csc \theta}$ $\cos \theta = \frac{1}{\sec \theta}$ $\tan \theta = \frac{1}{\cot \theta}$

$$\sin^2 \theta = 1 - \cos^2 \theta$$

Strategies for Proving Identities:

- Work on the most complex side and simplify so it has the same form as the simpler side
- Methods used in simplifying: direct substitution, factoring, finding a common denominator, multiplying by the conjugate

Prove the following identities:

$$\frac{1}{\sin^2 x} + \frac{1}{\cos^2 x} = \frac{1}{\sin^2 x \cos^2 x}$$

$$\frac{1(\cos^2 x)}{\sin^2 x \cos^2 x} + \frac{1(\sin^2 x)}{\sin^2 x \cos^2 x}$$

$$\frac{\cos^2 x}{\sin^2 x \cos^2 x} + \frac{\sin^2 x}{\sin^2 x \cos^2 x}$$

$$\frac{\cos^2 x + \sin^2 x}{\sin^2 x \cos^2 x}$$

$$\frac{1}{\sin^2 x \cos^2 x}$$

$$\frac{\csc \theta}{\cot^2 \theta} = \tan \theta \sec \theta$$

$$\frac{1}{\sin \theta} \div \frac{\cos^2 \theta}{\sin^2 \theta}$$

$$\frac{1}{\cancel{\sin \theta}} \cdot \frac{\cancel{\sin^2 \theta}}{\cos^2 \theta}$$

$$\frac{\sin \theta}{\cos^2 \theta}$$

$$\left(\frac{\sin \theta}{\cos \theta}\right) \left(\frac{1}{\cos \theta}\right)$$

$$\frac{\sin \theta}{\cos^2 \theta}$$

Homework