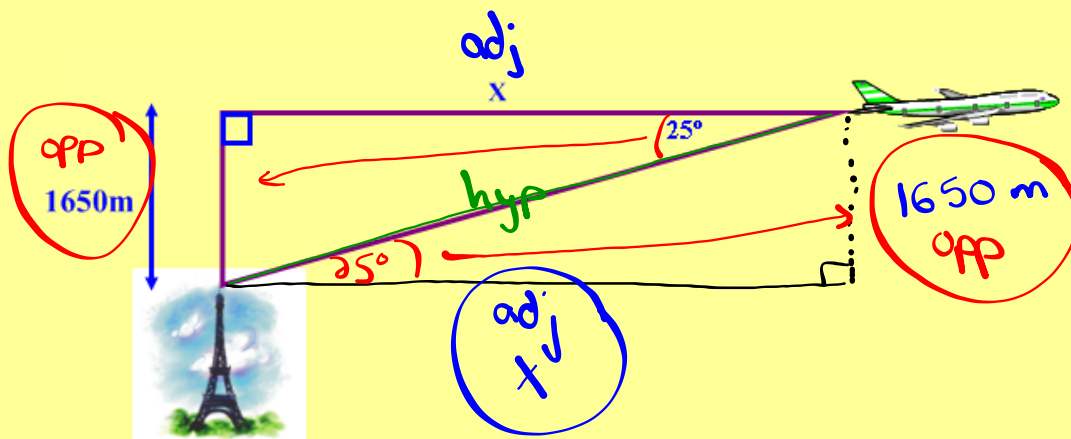


Warm Up Questions !!

#1 The angle of depression from a plane in the air to the top of a tower is 25° . The altitude of the plane is 1650m higher than the top of the tower. What is the horizontal distance from the plane to the tower?



$$\tan \theta = \frac{o}{a}$$

$$\tan 25^\circ = \frac{1650}{x}$$

$$\frac{0.4663}{1} = \frac{1650}{x} \quad | \quad x \cdot 0.4663 = \frac{1650}{x} \cdot x$$

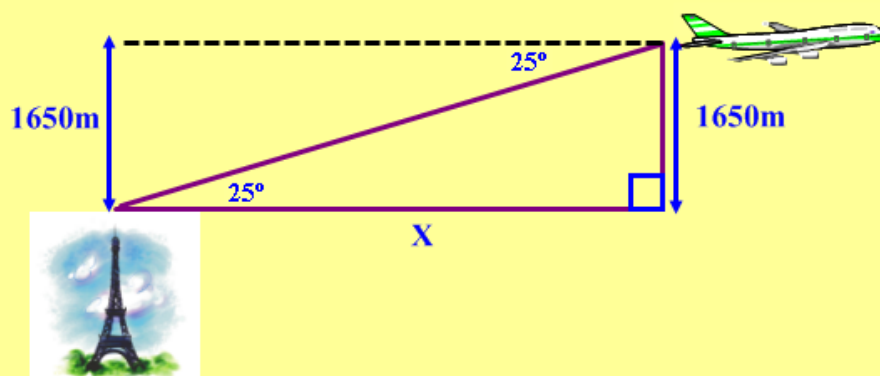
$$\cancel{0.4663}x = \frac{1650}{\cancel{0.4663}}$$

$$0.4663 \quad 0.4663$$

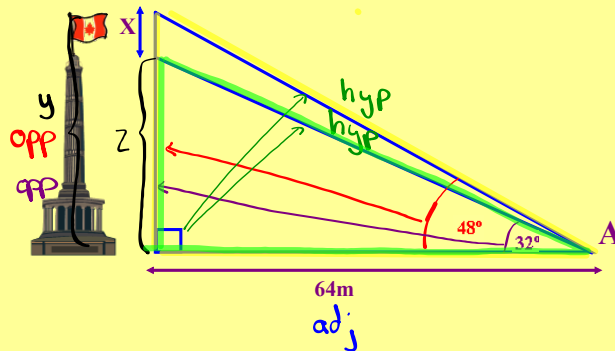
$$x = 3538.5 \text{ m}$$

Warm Up Questions !!

- #1 The angle of depression from a plane in the air to the top of a tower is 25° . The altitude of the plane is 1650m higher than the top of the tower. What is the horizontal distance from the plane to the tower?



- #2 The angle of elevation to the top of a building from point A is 32° . Point A is located 64.0m from the base of the building. A flagpole is on the top of the building. The angle of elevation from point A to the top of the flagpole is 48° . What is the length of the flagpole?



- ① Find distance from ground to top of flag (Big)

$$\tan \theta = \frac{o}{a}$$

$$\tan 48^\circ = \frac{y}{64}$$

$$64 \cdot 1.1106 = \frac{y}{64} \cdot 64$$

$$\boxed{71.1\text{m} = y}$$

- ② Find distance from ground to top of building (Small)

$$\tan \theta = \frac{o}{a}$$

$$\tan 32^\circ = \frac{z}{64}$$

$$64 \cdot 0.6249 = \frac{z}{64} \cdot 64$$

$$\boxed{40\text{m} = z}$$

- ③ Find the height of the flagpole (x)

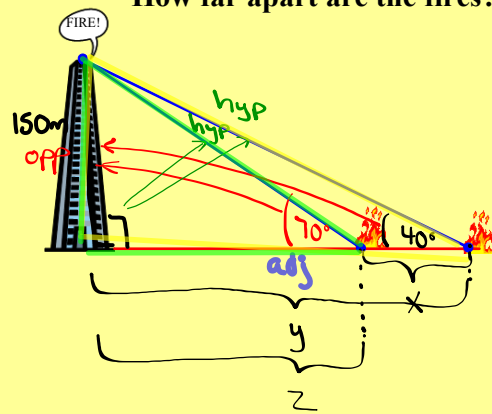
$$x = y - z$$

$$x = 71.1 - 40$$

$$\boxed{x = 31.1\text{m}}$$

Exam Question

A forest ranger in a tower 150m high sights two fires in the same line of sight with the angles of depression of 40 and 70 degrees. How far apart are the fires?



① Find y : (Big \triangle)

$$\tan \theta = \frac{o}{a}$$

$$\tan 40^\circ = \frac{150}{y}$$

$$y \cdot 0.8391 = \frac{150}{y} \cdot y$$

$$\frac{0.8391y}{0.8391} = \frac{150}{0.8391}$$

$$y = \underline{178.8m}$$

② Find z : (Small \triangle)

$$\tan \theta = \frac{o}{a}$$

$$\tan 70^\circ = \frac{150}{z}$$

$$z \cdot 2.7475 = \frac{150}{z} \cdot z$$

$$\frac{2.7475z}{2.7475} = \frac{150}{2.7475}$$

$$z = \underline{54.6m}$$

③ Find x :

$$x = y - z$$

$$x = 178.8 - 54.6$$

$$x = \underline{124.2m}$$

Homework

1, 2, 5

Solutions

The diagram shows a tower of height 1150m. A horizontal dashed line extends from the top of the tower to the right. An airplane is shown to the right of this line. A line of sight connects the top of the tower to the airplane, forming an angle of depression of 17° with the horizontal dashed line. A right-angle symbol is at the top of the tower. Below the diagram are two right-angled triangles used for calculation.

1st Triangle: A right-angled triangle with a vertical side of 1150 (labeled 'opp'), a horizontal side of x (labeled 'Adj'), and a hypotenuse of x (labeled 'Hyp'). The angle at the top vertex is 17°.

$$\tan 17^\circ = \frac{1150}{x}$$

$$0.3057x = 1150$$

$$\frac{0.3057x}{0.3057} = \frac{1150}{0.3057}$$

$$x = 3761.5 \text{ m}$$

2nd Triangle: A right-angled triangle with a vertical side of 1150 (labeled 'opp'), a horizontal side of x (labeled 'Adj'), and a hypotenuse of x (labeled 'Hyp'). The angle at the top vertex is 17°.

$$\sin 17^\circ = \frac{1150}{x}$$

$$0.2924x = 1150$$

$$\frac{0.2924x}{0.2924} = \frac{1150}{0.2924}$$

$$x = 3933.3 \text{ m}$$

Solutions

$$\tan 17^\circ = \frac{1150}{x}$$

$$0.3057x = 1150$$

$$\frac{0.3057}{0.3057} = \frac{1150}{0.3057}$$

$$x = 3761.5 \text{ m}$$

$$\sin 17^\circ = \frac{1150}{x}$$

$$0.2924x = 1150$$

$$\frac{0.2924}{0.2924} = \frac{1150}{0.2924}$$

$$x = 3933.3 \text{ m}$$

-> The horizontal distance is 3761.5 m.
 => The distance btw. the plane and the tower 3933.3 m.

OPP. 128.0m Hyp. 61°

$$\tan 61^\circ = \frac{128}{x}$$

$$x = 70.1 \text{ m}$$

OPP. 128.0m Hyp. 42°

$$\tan 42^\circ = \frac{128}{x}$$

$$x = 142 \text{ m}$$

* The distance btw. the fires is

$$142.2 \text{ m} - 70.1 \text{ m} = 72.1 \text{ m}$$

Solutions

#3.

1st

$$\tan 29^\circ = \frac{26}{X}$$

$$0.5543 X = 26$$

$$0.5543 \quad 0.5543$$

$$X = \underline{\underline{46.9m}}$$

2nd

$$\tan 39^\circ = \frac{X}{46.9}$$

$$X = \underline{\underline{38.0m}}$$

3rd

38.0m
26m
64m

* The building is 64m tall

Solutions

* The building is 64m tall

#4.

352.0m

A

1st

Hyp

Opp

352m

52°

2nd

Hyp

Opp

352m

38°

3rd

450.5 m

- 275.0 m

175.5 m

$$\tan 52^\circ = \frac{X}{352}$$

$$X = 450.5 \text{ m}$$

$$\tan 38^\circ = \frac{X}{352}$$

$$X = 275.0 \text{ m}$$

* The helicopter rised 175.5m Above the building.

Solutions

#5.

1st

$$\tan 58^\circ = \frac{x}{56.0}$$

$$x = \underline{\underline{89.6 \text{ m}}}$$

2nd

$$\tan 62^\circ = \frac{x}{56.0}$$

$$x = \underline{\underline{105.3}}$$

3rd

$$105.3 \text{ m}$$

$$- 89.6 \text{ m}$$

$$\underline{\underline{15.7 \text{ m}}}$$

* The flagpole is 15.7m long.

Solutions

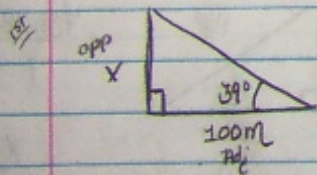
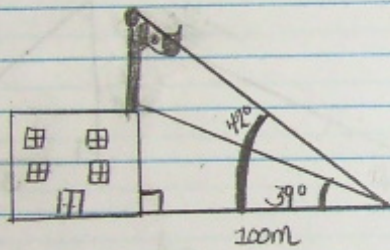
$x = \underline{\underline{89.6\text{ m}}}$

$x = \underline{\underline{105.3}}$

* The flagpole is 15.7m long.

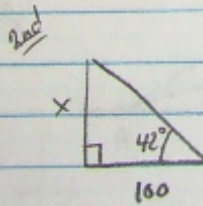
#6.

* The school is 80.9m high.
 * The flagpole is 9.1m tall.



$$\frac{\tan 39^\circ = x}{100}$$

$$x = 80.9\text{ m}$$



$$\frac{\tan 42^\circ = x}{100}$$

$$x = 90.0\text{ m}$$

$$\begin{array}{r} 90.0\text{ m} \\ - 80.9\text{ m} \\ \hline 9.1\text{ m} \end{array}$$

