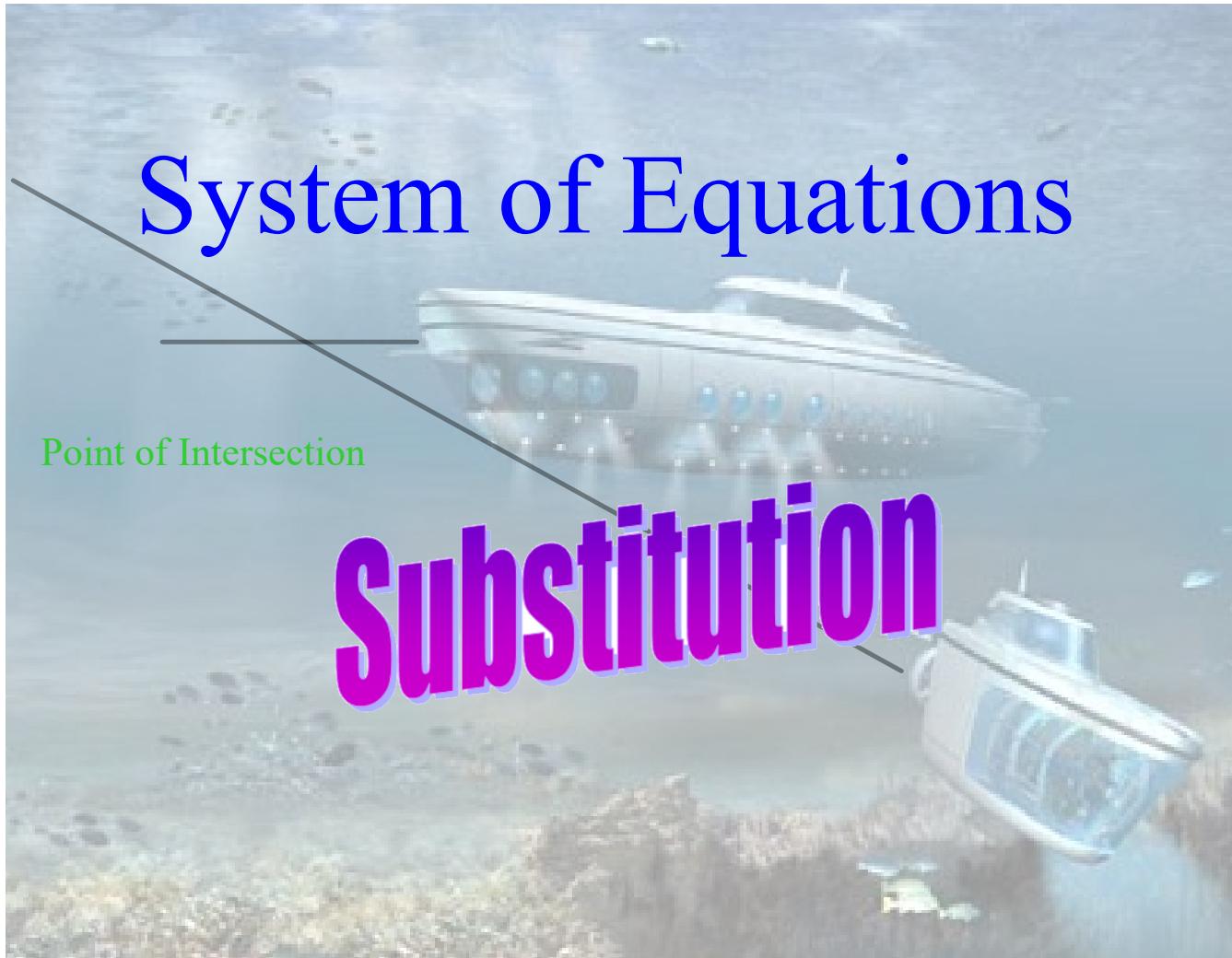


# System of Equations

Point of Intersection

# Substitution



## Substitution Method

Steps: *look for a 1x or a 1y*

- i) Choose one equation and isolate one variable;  
this equation will be considered the first equation.  
(easiest one to get  $x =$  or  $y =$  from either eqn 1 or eqn 2)
- ii) Substitute the solution from step 1 into the second  
equation and solve for the variable in the equation.
- iii) Using the value found in step 2, substitute it into the  
first equation and solve for the second variable.  
*(either)*
- iv) Substitute the values for both variables into both  
equations to show they are correct.

\* your answer will be an ordered pair  
 $(x, y)$ . This is the point where the two  
lines intersect.

Solve this system of equation by substitution.

$$\begin{array}{l} \underline{y = 15 + 6x} \\ -3x - 2y = 0 \end{array}$$

$$\begin{aligned} -3x - 2y &= 0 \\ -3x - 2(15 + 6x) &= 0 \\ -3x \cancel{-30} \cancel{-12x} &= 0 \\ -3x \cancel{-12x} &= 0 + \cancel{30} \\ -15x &= \frac{\cancel{30}}{\cancel{-15}} \\ x &= \underline{\underline{-2}} \end{aligned}$$

$$\begin{aligned} y &= 15 + 6x \\ y &= 15 + 6(-2) \\ y &= 15 - 12 \\ y &= 3 \end{aligned}$$

$$(-2, 3)$$

Solve the system by Substitution Method

$$x + 2y = 3$$

$$\underline{3x + 5y = 8}$$

solve for x  $\rightarrow x = \underline{\underline{3 - 2y}}$

$$3x + 5y = 8$$

$$3(\underline{\underline{3 - 2y}}) + 5y = 8$$

$$\underline{\underline{9 - 6y}} + 5y = 8$$

$$-6y + 5y = 8 - 9$$

$$-y = -1$$

$$y = 1$$



$$x + 2y = 3$$

$$x + 2(1) = 3$$

$$x + 2 = 3$$

$$x = 3 - 2$$

$$x = 1$$

$$(1,1)$$

Use Substitution to Find the Point of Intersection

$$\begin{aligned} 1) \quad & x - 4y = 6 \\ & 7x + 6y = 8 \end{aligned} \longrightarrow \begin{aligned} & x - 4y = 6 \quad \text{+4y} \\ & \underline{x = 6 + 4y} \end{aligned}$$

$$\begin{aligned} (\text{ii}) \quad & x = 6 + 4y \\ & x = 6 + 4(-1) \\ & x = 6 - 4 \\ & x = 2 \end{aligned}$$

$$\begin{aligned} (\text{ii}) \quad & 7x + 6y = 8 \\ & 7(6 + 4y) + 6y = 8 \\ & 42 + \cancel{28y} + \cancel{6y} = 8 \quad \cancel{-42} \quad \cancel{-42} \\ & \frac{34y}{34} = \frac{-34}{34} \end{aligned}$$

$$\begin{aligned} (\text{iv}) \quad & (2, -1) \end{aligned}$$

$$\underline{y = -1}$$

Use Substitution to Find the Point of Intersection

$$\begin{aligned} 2) \quad & 2x + y = 9 \\ & 3x - 5y = -19 \end{aligned}$$

$$\begin{aligned} \text{(i)} \quad & 2x + y = 9 \\ & y = 9 - 2x \end{aligned}$$

$$\begin{aligned} \text{(ii)} \quad & y = 9 - 2x \\ & y = 9 - 2(2) \\ & y = 9 - 4 \\ & y = 5 \end{aligned}$$

$$\text{(iv)} \quad \boxed{(2, 5)}$$

$$\begin{aligned} \text{(iii)} \quad & 3x - 5y = -19 \\ & 3x - 5(9 - 2x) = -19 \\ & 3x - 45 + 10x = -19 + 45 \\ & \frac{13x}{13} = \frac{26}{13} \\ & x = 2 \end{aligned}$$