

## Simple Interest

$$I = Prt$$

- Interest calculated as a percentage of the principal.

$I$  = Interest

$P$  = Principal

$r$  = rate (as a decimal)

$t$  = time in years

## Compound Interest

$$A = P\left(1 + \frac{r}{n}\right)^{nt}$$

- The interest paid on the principal plus interest

$A$  = final value of the investment (principal + interest)

$P$  = principal (invest/borrow)

$r$  = annual interest rate (as a decimal)

$n$  = number of compounding periods in a year

$t$  = term of the investment or loan in number of years

## Terminology Tango

		# of compounds per year
annually	—————→	1
semi-annually	—————→	2
quarterly	—————→	4
monthly	—————→	12
semi-monthly	—————→	24
bi-weekly	—————→	26
weekly	—————→	52
daily	—————→	365

Allison wants to invest \$2000.00. Her bank offers an investment option that earns compound interest at a rate of 1.75% per year compounded annually for 3 years.

$$P = 2000.00$$

$$r = 0.0175$$

$$t = 3$$

Interest period	Investment value at beginning of period	Interest earned $I = Prt$	Investment value at end of period
1	\$2000	$\$2000 \times 0.0175 \times 1 = \$35$	\$2035
2	\$2035	$\$2035 \times 0.0175 \times 1 = \$35.61$	\$2070.61
3	\$2070.61	$\$2070.61 \times 0.0175 \times 1 = \$36.24$	\$2106.85

Allison wants to invest \$2000.00. Her bank offers an investment option that earns compound interest at a rate of 1.75% per year compounded annually for 10 years.

Interest period	Investment value at beginning of period	Interest earned $I = Prt$	Investment value at end of period
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??

**Formula:**  $A = P \left( 1 + \frac{r}{n} \right)^{nt}$

A = final value of the investment ...(principal + interest)  $A = ?$

P = principal  $P = 2000$

r = annual interest rate  $r = 0.0175$

n = number of compounding periods in a year  $n = 1$

t = term of the investment or loan in number of years  $t = 10$

Allison wants to invest \$2000.00. Her bank offers an investment option that earns compound interest at a rate of 1.75% per year compounded annually for 10 years.

$$A = P \left( 1 + \frac{r}{n} \right)^{nt}$$

$$A = \underline{2000} \left( 1 + \frac{\underline{0.0175}}{\underline{1}} \right)^{\underline{(1)}(\underline{10})}$$

$$A = 2000(1 + 0.0175)^{10}$$

$$A = 2000(1.0175)^{10}$$

$$A = 2000(1.18944)$$

$$A = \$2378.89$$

Exponent Button:

$$\boxed{y^x} \text{ or } \boxed{x^y} \text{ or } \boxed{\wedge}$$

Calculate the final value of an initial investment of \$6000.00.  
Interest is paid at 4% per annum, compounded semi-annually, for three years.

$$A = ?$$

$$P = 6000.00$$

$$r = 4\%$$

$$r = 0.04$$

$$n = 2$$

$$t = 3$$

$$A = \underline{P} \left( 1 + \frac{\underline{r}}{\underline{n}} \right)^{\underline{nt}}$$

$$A = 6000 \left( 1 + \frac{0.04}{2} \right)^{(2)(3)}$$

$$A = 6000 (1 + 0.02)^6$$

$$A = 6000 (1.02)^6$$

$$A = 6000 (1.1261624)$$

$$A = \$6756.97$$

Calculate the final value of an initial investment of \$8500.00.  
Interest is paid at 3.75% per annum, compounded semi-annually,  
for three years.

$$A = P \left( 1 + \frac{r}{n} \right)^{nt}$$

## Homework

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Questions 1-7



**the**  
**RULE**  
**of** **72**

**the  
RULE  
of 72**

Quick way to estimate how long it will take your money to double in value.

$$\frac{72}{\text{annual interest rate}}$$

How long will it take an investment to double with an interest rate of 3.00% per annum?

$$\frac{72}{3} = 24 \text{ years}$$