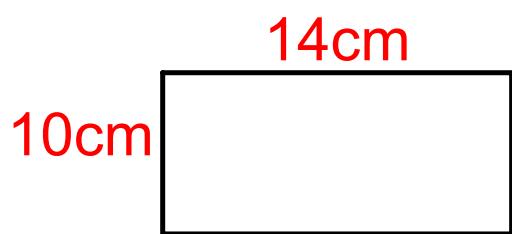
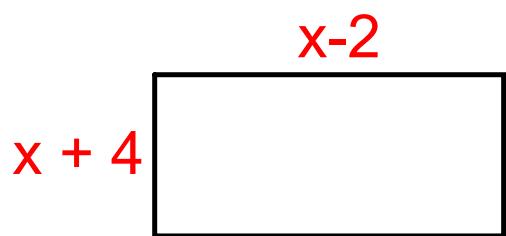


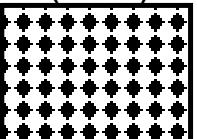
Determine the area:



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$$(2x-3)(5x+1)$$
A rectangular grid of 30 dots arranged in 5 rows and 6 columns. The top row has 5 dots, the second row has 6 dots, the third row has 5 dots, the fourth row has 6 dots, and the bottom row has 5 dots. The grid is enclosed in a thin black border.



Which of the following can be represented by a rectangle?

$$\underline{\quad} + \underline{\quad} = -7$$

$$\underline{\quad} \times \underline{\quad} = -30$$

$$5a^2 - 7a - 6$$

$$5a^2 - 12a - 6$$



$$\underline{\quad} + \underline{\quad} = -12$$

$$\underline{\quad} \times \underline{\quad} = -30$$

Common Factoring

$$\begin{array}{c} 22w^7 - 88z^{14} \\ \hline 4r^8 - 16r^7s^9 + 2r^{10} \\ \hline g^4x^2 - g^9x^5 \end{array}$$

Trinomial

$$\begin{array}{c} 4z^2 + 16z + 7 \\ \hline m^2 - 10m - 9 \end{array}$$

Difference
of
Squares

$$\begin{array}{c} 64v^2 - 81 \\ \hline x^2 - 16 \end{array}$$

$$\begin{aligned} - + &= -9 \\ - \times &= 16 \\ &\quad 16 \\ -1x - 16 \\ -2x - 8 \\ -4x - 4 \end{aligned}$$

$$\begin{array}{c} x^2 - 9x + 16 \\ \hline \end{array}$$

Not Possible

Choose a polynomial
out of the bag
and then determine
which
type of factoring
it is.

How Are Your Factoring Skills?

Factor each of the following:

1. $15m^5n^3p - 30n^7p^3 + 60m^4n^8p^5$
2. $x^2 - 2x - 35$
3. $270xy^2 - 180x^3y - 90xy$
4. $5x^2 + 14xy - 3y^2$
5. $4x^2 - 14x - 8$
6. $4x^2 - 49$

Common factor

$$1. \underline{15m^5n^3p} - \underline{30n^7p^3} + \underline{60m^4n^8p^5}$$

$$\underline{15n^3p} \left(m^5 - 2n^4p^2 + 4m^4n^5p^4 \right)$$

Simple trinomial

2. $x^2 - \underline{2x} - \underline{35}$

$(x+5)(x-7)$.

larger factor is negative

$$\underline{5} + \underline{-7} = \underline{-2} \quad -35$$

$$\underline{5} \times \underline{-7} = \underline{-35} \quad 1 \times -35$$

$$\textcircled{5} \times \textcircled{-7}$$

signs are different

Common Factor

$$3. \underline{270xy^2} - \underline{180x^3y} - \underline{90xy}$$

$$\underline{\underline{90xy}}(3y - 2x^2 - 1)$$

Hard trinomial

$$4. \quad 5x^2 + 14xy - 3y^2$$

$$(x - 1y)(x + 15y)$$

x -1 15

$$(5x - y)(x + 3y)$$

larger factor is positive

$$-1 + 15 = 14$$

$$-15$$

$$-1 \times 15 = -15$$

$$\begin{array}{c} -1 \times 15 \\ \hline -3 \times 5 \end{array}$$

Signs are different

Hard trinomial

5. $4x^2 - \underline{14x} - \underline{8}$

$$(x + \frac{2}{4})(x - \frac{16}{4})$$

$$(x + \frac{1}{2})(x - 4)$$

$$(2x+1)(x-4)$$

larger factor is negative

$$2 + \underline{-16} = -14$$

$$2 \times \underline{-16} = -32$$

-32

$$\begin{array}{r} 1 \\ x - 32 \\ \hline 2x - 16 \\ \hline 4x - 8 \end{array}$$

signs are different

Difference of Squares:

$$6. \underline{4x^2} - \underline{49}$$

$$\sqrt{4x^2} = 2x$$

$$(2x + 7)(2x - 7)$$

$$\sqrt{49} = 7$$

Homework

1. $b^2 - 16$ $(b - 4)(b + 4)$	2. $4x^2 - 9$ $(2x - 3)(2x + 3)$
3. $36y^5x^3 + 20y^3x^3 - 32y^2$ $4y^2(9y^3x^3 + 5y^3x^3 - 8)$	4. $64 + 56b^2 - 32a$ $8(8 + 7b^2 - 4a)$
5. $90u^4v^3 + 9u^4 + 18u$ $9u(10u^3v^3 + v^3 + 2)$	6. $9n^2 - 25$ $(3n - 5)(3n + 5)$

$$7. \quad x^2 - 9$$

$$(x-3)(x+3)$$

$$9. \quad 10p^2 - 17p - 63$$

$$\left(p + \frac{18}{10}\right) \left(p - \frac{35}{10}\right)$$

$$\left(p + \frac{9}{5}\right) \left(p - \frac{7}{2}\right)$$

$$(5p+9)(2p-7)$$

$$-t = -17$$

$$-x = 630$$

$$\begin{array}{r} 14 - 45 \\ 15 - 42 \\ \hline 18 - 35 \\ 2 - 315 \\ 3 - 210 \\ 5 - 126 \\ 6 - 105 \\ 7 - 90 \\ 9 - 70 \\ \hline 10 - 63 \end{array}$$

$$8. \quad 10k^2 + 83k + 24$$

$$-t = 23$$

$$-x = 240$$

$$\begin{array}{r} 1 \\ 240 \end{array}$$

$$\begin{array}{r} 2 \\ 120 \end{array}$$

$$\begin{array}{r} 3 \\ 80 \end{array}$$

$$\begin{array}{r} 4 \\ 60 \end{array}$$

$$\begin{array}{r} 5 \\ 48 \end{array}$$

$$\begin{array}{r} 6 \\ 40 \end{array}$$

$$\begin{array}{r} 8 \\ 30 \end{array}$$

$$\begin{array}{r} 10 \\ 24 \end{array}$$

$$\begin{array}{r} 12 \\ 20 \end{array}$$

$$\begin{array}{r} 15 \\ 16 \end{array}$$

$$(10k+3)(k+8)$$

$$10. \quad 9n^2 + 33n + 28 \quad -+--=33$$

$$(n+12)(n+21) \quad -x-=252$$

9	9
12	21
252	
126	
84	
63	
42	
36	
28	
<u>12 21</u>	
14	18

$$(n + \frac{4}{3})(n + \frac{7}{3})$$

$$(3n+4)(3n+7)$$

$$11. \quad 9a^2 - 92a + 20 \quad -+-=-92 \quad | \quad 12. \quad n^2 - 1$$

$$(a - \frac{2}{9})(a - \frac{90}{9}) \quad -x-=180$$

1	
-1	-180
-2	-90
-3	-60
-4	-45
-5	-36
-6	-30
-7	-25
-8	-20
-9	-18
-10	-15
-12	-12

$$(9a-2)(a-10)$$

$$(9a-2)(a-10)$$

$$\begin{array}{r} \cdot 4 \cdot 45 \\ -5 \cdot 36 \\ -6 \cdot 30 \\ -9 \cdot 20 \\ -10 \cdot 18 \\ -12 \cdot 15 \end{array}$$

$$13. a^2 - 9$$

$$(a-3)(a+3)$$

$$15. 10x^4y^2 + 35xy^6 + 45x^2$$

$$5x(2x^5y^2 + 7y^6 + 9x)$$

$$14. 6b^4a + 3b^2a^2 - 15b$$

$$3b(2b^3a + ba^2 - 5)$$

$$16. 9 - 45b + 45ab$$

$$9(1 - 5b + 5ab)$$

Important

$$17. 6x^2yz + 3xyz^2 - 18xyz \\ 3xyz(2xy + z - 6)$$

$$18. 63g^6p^5r^2 + 21g^5p^4 + 28g^3 \\ 7g^3(9g^3p^5r^2 + 3g^2p^4 + 4)$$

$$19. K^2 - 16 \\ (K-4)(K+4)$$

$$20. 4p^2 + 12p + 9 \quad -+ = 12 \\ -x = 36 \\ (p + \frac{6}{4})(p + \frac{6}{4}) \quad \begin{array}{r} 1 \\ 136 \\ 312 \\ 49 \\ \hline 66 \end{array} \\ (p + \frac{3}{2})(p + \frac{3}{2}) \\ (2p + 3)(2p + 3)$$

OR
 $(2p+3)^2$

21. $K^2 + 2K - 24$

$$(K-4)(K+6)$$

$$\begin{array}{r} -t=2 \\ -x=-24 \\ \hline 1 \\ -1 \\ \hline 24 \\ -2 \\ \hline 12 \\ -3 \\ \hline 8 \\ -4 \\ \hline b \end{array}$$

22. $n^2 + 6n + 8$

$$(n+2)(n+4)$$

$$\begin{array}{r} -t=6 \\ -x=8 \\ \hline 1 \\ -1 \\ \hline 8 \\ -2 \\ \hline 4 \\ -2 \\ \hline 4 \end{array}$$

$$(2p+3)(2p+3)$$

or

$$(2p+3)^2$$

$$23. (4K+5)(5K-5)$$

$$20K^2 - 20K + 25K - 25$$

$$20K^2 + 5K - 25$$

$$24. (5n-2)(5n+1)$$

$$25n^2 + 5n - 10n - 2$$

$$25n^2 - 5n - 2$$

25.

$$7x^4 - 1 + x^2 + \cancel{2x} + 7x^2 + \cancel{8x} + 4$$

$$7x^4 + 3 + 8x^2 + 10x$$

or

$$7x^4 + 8x^2 + 10x + 3$$

$$26. \underline{\underline{2\rho^4}} - \cancel{7\rho^3} - \cancel{4\rho^2} - \underline{8\rho} + \cancel{2\rho} + \underline{\underline{8\rho^4}} + \cancel{7\rho^3}$$

$$10\rho^4 - 4\rho^2 - 6\rho$$