# Inverse of a Relation

An inverse function is a second function which undoes the work of the first one.

Suppose we have a function f that takes x to y, so that

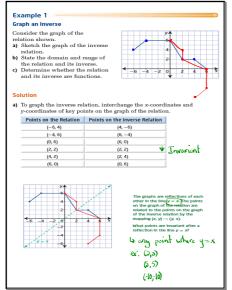
$$f(x) = y$$
.

An inverse function, which we call  $f^{-1}$ , is another function that takes y back to x. So

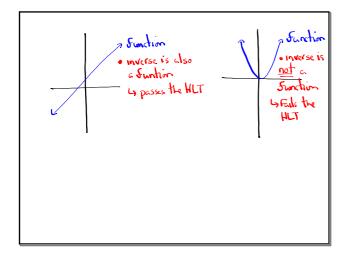
$$f^{-1}(y) = x$$
.

For  $f^{-1}$  to be an inverse of f, this needs to work for every x that f acts upon.

May 9-9:04 AM



May 9-9:12 AM



Sep 20-11:24 AM

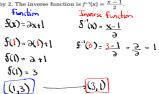
### Inverse of a Relation

The inverse of a relation is found by interchanging the x-coordinates and y-coordinates of the ordered pairs of the relation. In other words, for every ordered pair (x, y) of a relation, there is an ordered pair (y, x) on the inverse of the relation. This means that the graphs of a relation and its inverse are reflections of each other in the line y = x.

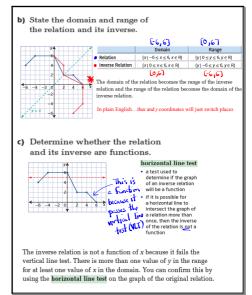
 $(x, y) \rightarrow (y, x)$  In plain English....ther and y coordinates will just switch pl

The inverse of a function y = f(x) may be written in the form x = f(y). The inverse of a function is not necessarily a function. When the inverse of f(x) itself a function, it is denoted as f(x) inverse. When the inverse of a function is not a function; it may be possible to restrict the domain to obtain an inverse function for a portion of the original function. The inverse of a function reverses the processes represented by that function. Functions f(x) and g(x) are inverse of each other if the operations of f(x) reverse all the operations of g(x) in the opposite order.

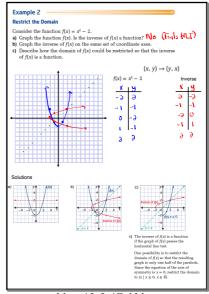
For example, f(x)=2x+1 multiplies the input value by 2 and then adds 1. The inverse function subtracts 1 from the input value and then divides by 2. The inverse function is  $f^{-1}(x)=\frac{x-1}{2}$ .



May 6-8:34 AM



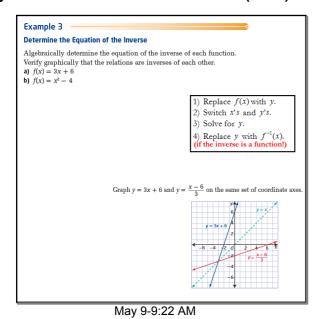
May 9-9:17 AM

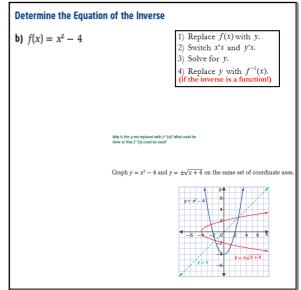


May 10-9:17 AM

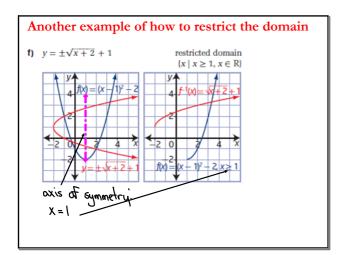
# Day 10 - Intro to Inverse Functions (after).notebook

# September 20, 2017





May 10-9:04 AM



Sep 17-9:29 AM

# Inverse of a Relation ullet You can find the inverse of a relation by interchanging the x-coordinates and y-coordinates of the graph. • The graph of the inverse of a relation is the graph of the relation reflected in the line y = x. The domain and range of a relation become the range and domain, respectively, of the inverse of the relation. • Use the horizontal line test to determine if an inverse will be a function. You can create an inverse that is a function over a specified interval by restricting the domain of a function. When the inverse of a function f(x) is itself a function, it is denoted by f<sup>-1</sup>(x). You can verify graphically whether two functions are inverses of each other.

May 10-9:10 AM

### Homework

Practice Problems...

Pages 51 - 55 #2, 3, 5, 6, 8, 9, 11, 15, 18, 20, 21

# What if given the function algebraically?

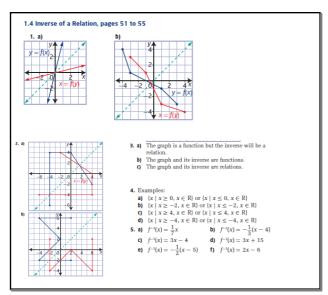
Determine algebraically the equation of the inverse of each function.

**a)** 
$$f(x) = 3x - 6$$

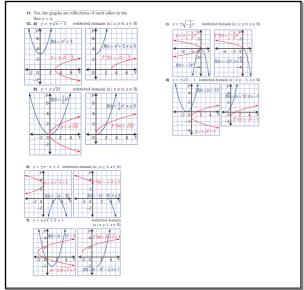
**b)** 
$$f(x) = \frac{1}{2}x + 3$$

**a)** 
$$f(x) = 3x - 6$$
 **b)**  $f(x) = \frac{1}{2}x + 5$  **c)**  $f(x) = \frac{1}{3}(x + 12)$  **d)**  $f(x) = \frac{8x + 12}{4}$ 

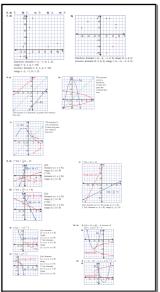
**d)** 
$$f(x) = \frac{8x + 12}{4}$$



May 10-11:11 AM



May 10-11:33 AM



May 10-11:20 AM