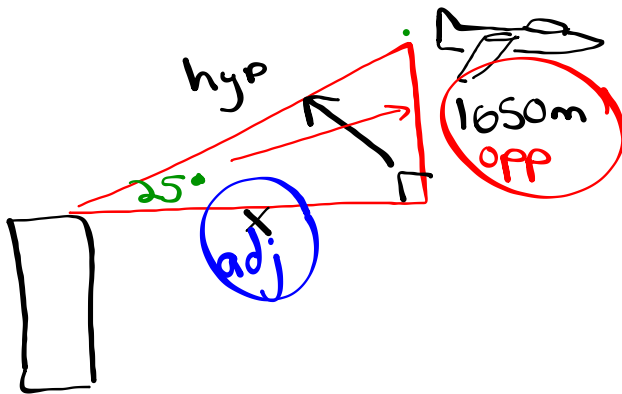


# Warm Up Questions !!

elevation

- #1 The angle of depression from a plane in the air to the top of a tower is  $25^\circ$ . The altitude of the plane is 1650m higher than the top of the tower. What is the horizontal distance from the plane to the tower?



$$\tan \theta = \frac{\text{opp}}{\text{adj}}$$

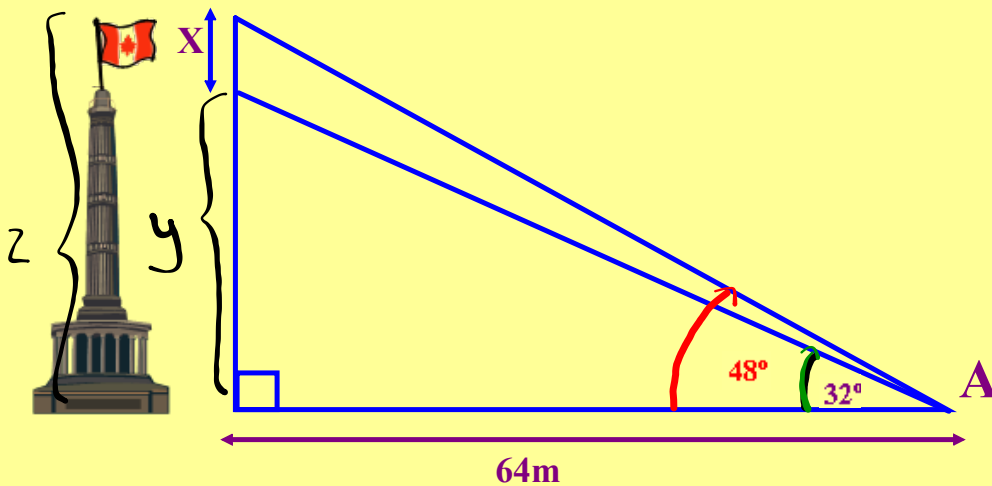
$$\tan 25^\circ = \frac{1650}{x}$$

$$x \cdot 0.4663 = \frac{1650}{x} \cdot x$$

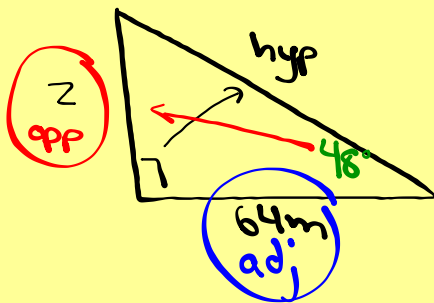
$$\frac{0.4663x}{0.4663} = \frac{1650}{0.4663}$$

$$x = 3538.5 \text{ m}$$

#2 The angle of elevation to the top of a building from point A is  $32^\circ$ . Point A is located 64.0m from the base of the building. A flagpole is on the top of the building. The angle of elevation from point A to the top of the flagpole is  $48^\circ$ . What is the length of the flagpole?



(i) Find z: (Big  $\Delta$ )



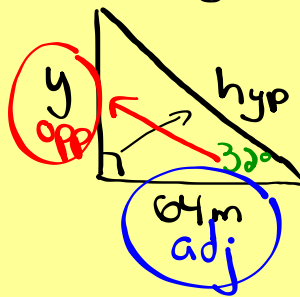
$$\tan \theta = \frac{\text{opp}}{\text{adj}}$$

$$\tan 48^\circ = \frac{z}{64}$$

$$64 \cdot 1.1106 = \frac{z}{64} \cdot 64$$

$$\underline{\underline{71.1\text{m}}} = z$$

(ii) Find y: (Small  $\Delta$ )



$$\tan \theta = \frac{\text{opp}}{\text{adj}}$$

$$\tan 32^\circ = \frac{y}{64}$$

$$64 \cdot 0.6249 = \frac{y}{64} \cdot 64$$

$$\underline{\underline{40\text{m}}} = y$$

(iii) Find x:

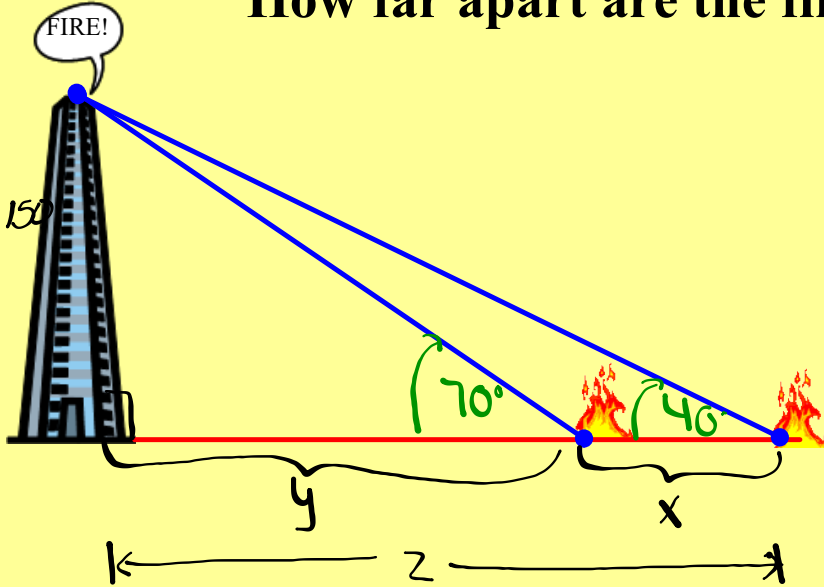
$$x = z - y$$

$$x = 71.1 - 40$$

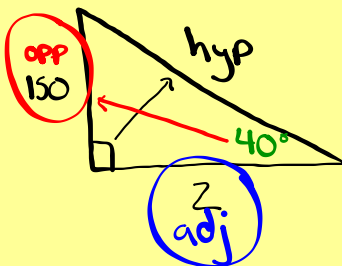
$$\boxed{x = 31.1\text{m}}$$

**Exam Question**

A forest ranger in a tower 150m high sights two fires in the same line of sight with the angles of ~~depression~~<sup>elevation</sup> of 40 and 70 degrees. How far apart are the fires?



(i) Find z: (Big  $\Delta$ )



$$\tan \theta = \frac{\text{opp}}{\text{adj}}$$

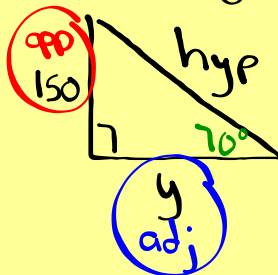
$$\tan 40^\circ = \frac{150}{z}$$

$$z \cdot 0.8391 = \frac{150}{z} \cdot z$$

$$\frac{0.8391z}{0.8391} = \frac{150}{0.8391}$$

$$z = 178.8 \text{ m}$$

(ii) Find y: (Small  $\Delta$ )



$$\tan \theta = \frac{\text{opp}}{\text{adj}}$$

$$\tan 70^\circ = \frac{150}{y}$$

$$y \cdot 2.7475 = \frac{150}{y} \cdot y$$

$$\frac{2.7475y}{2.7475} = \frac{150}{2.7475}$$

$$y = 54.6 \text{ m}$$

(iii) Find x:

$$x = z - y$$

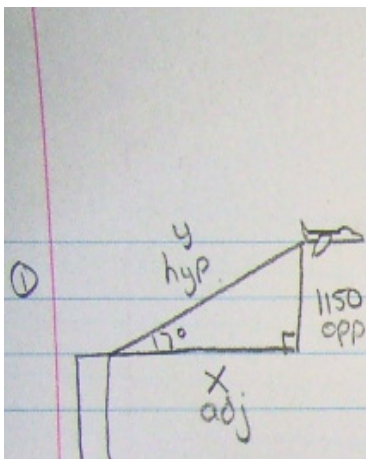
$$x = 178.8 - 54.6$$

$$x = 124.2 \text{ m}$$

# Homework

## Solutions

①



a) Find x:

$$\tan \theta = \frac{\text{opp}}{\text{adj}}$$

$$\tan 17^\circ = \frac{1150}{x}$$

$$0.3057 = \frac{1150}{x}$$

$$0.3057x = 1150$$

$$x = 3761.9\text{m}$$

b) Find y:

$$\sin \theta = \frac{\text{opp}}{\text{hyp}}$$

$$\sin 17^\circ = \frac{1150}{y}$$

$$0.2924 = \frac{1150}{y}$$

$$0.2924y = 1150$$

$$y = 3933\text{m}$$

②

128m

61° 40°

y x z

(i)

128 opp hyp 40°

z adj

$\tan \theta = \frac{\text{opp}}{\text{adj}}$

$\tan 40^\circ = \frac{128}{z}$

$0.9004 = \frac{128}{z}$

$0.9004z = 128$

$z = 142.2\text{m}$

(ii)

128 opp hyp 61°

y adj

$\tan \theta = \frac{\text{opp}}{\text{adj}}$

$\tan 61^\circ = \frac{128}{y}$

$1.8040 = \frac{128}{y}$

$1.8040y = 128$

$y = 71\text{m}$

(iii)  $x = z - y$

$x = 142.2 - 71$

$x = 71.2\text{m}$

③

$\tan 29^\circ = \frac{26}{x}$   
 $\tan 39^\circ = \frac{y}{46.9}$

(i) Find x:  
 $\tan \theta = \frac{\text{opp}}{\text{adj}}$   
 $\tan 29^\circ = \frac{26}{x}$   
 $0.5543 = \frac{26}{x}$   
 $0.5543x = 26$   
 $x = 46.9\text{m}$

(ii) Find y:  
 $\tan \theta = \frac{\text{opp}}{\text{adj}}$   
 $\tan 39^\circ = \frac{y}{46.9}$   
 $0.8098 = \frac{y}{46.9}$   
 $38\text{m} = y$

(iii) Find z:  
 $z = y + 26$   
 $z = 38 + 26$   
 $z = 64\text{m}$

④

(i) Find  $x$  :

(ii) Find  $y$  :

(iii) Find  $d$  :

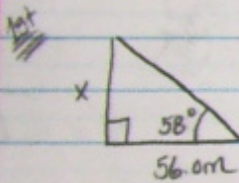
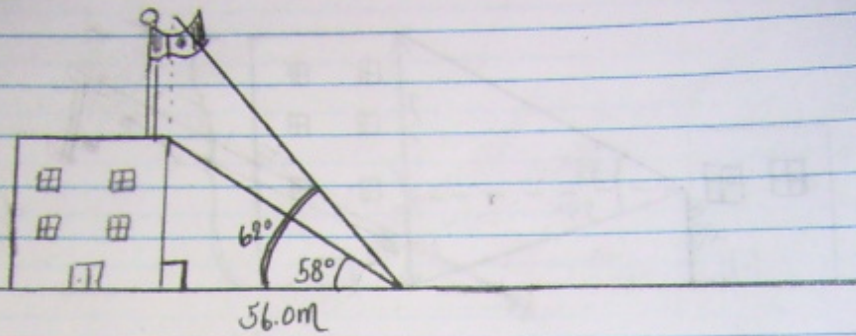
$d = y - x$   
 $d = 450.5 - 275$   
 $d = 175.5 \text{ m}$

$\tan \theta = \frac{\text{opp}}{\text{adj}}$   
 $\tan 38^\circ = \frac{x}{350}$   
 $0.7813 = \frac{x}{350}$   
 $275 \text{ m} = x$

$\tan \theta = \frac{\text{opp}}{\text{adj}}$   
 $\tan 52^\circ = \frac{y}{350}$   
 $1.2799 = \frac{y}{350}$   
 $450.5 \text{ m} = y$

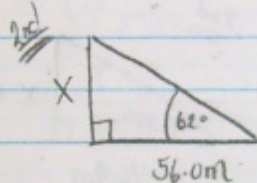


#5.



$$\tan 58^\circ = \frac{x}{56.0}$$

$$x = \underline{\underline{89.6\text{ m}}}$$



$$\tan 62^\circ = \frac{x}{56.0}$$

$$x = \underline{\underline{105.3}}$$

3rd

$$105.3\text{ m}$$

$$- \underline{\underline{89.6\text{ m}}}$$

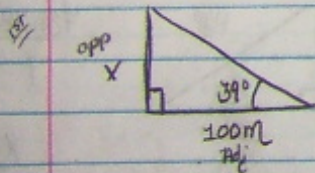
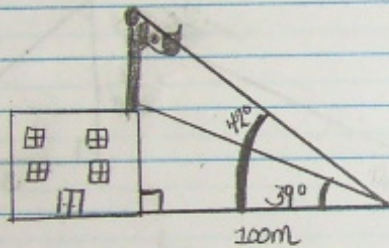
15.7m

\* The flagpole is 15.7m long.

\* The flagpole is 15.7m long.

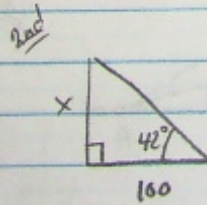
#6.

\* The school is 80.9m high.  
 \* The flagpole is 9.1m tall.



$$\frac{\tan 39^\circ = X}{1 \times 100}$$

$$X = 80.9m$$



$$\frac{\tan 42^\circ = X}{1 \times 100}$$

$$X = 90.0m$$

3rd

$$\begin{array}{r} 90.0m \\ - 80.9m \\ \hline 9.1m \end{array}$$

#7.

1st

$$\tan 13^\circ = \frac{70}{x}$$

$$0.2309x = 70$$

$$x = 303.2 \text{ m}$$

2nd

$$\tan 8^\circ = \frac{70}{x}$$

$$0.1405x = 70$$

$$x = 498.1$$

3rd

$$\begin{array}{r} 498.1 \text{ m} \\ - 303.2 \text{ m} \\ \hline = 194.9 \text{ m} \end{array}$$